

2017

**MADE EASY**  
**WORKBOOK**



**Detailed Explanations of  
Try Yourself Questions**

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**Electrical Engineering  
Power Electronics**



**MADE EASY**  
Publications

# 1

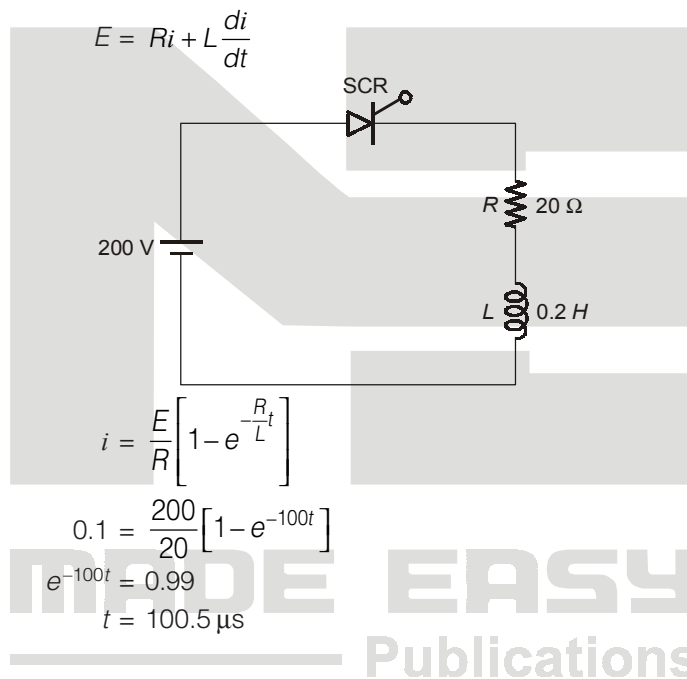
## Power Semiconductor Devices



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

The voltage equation for  $RL$  load is



#### T2 : Solution

(c)

The equation of the straight line

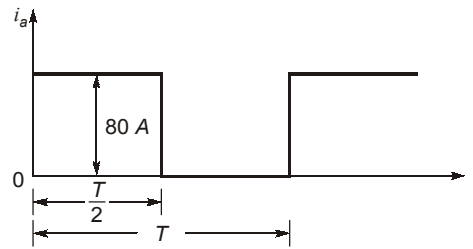
$$y = mx + c$$

$$m = 83.33; \quad C = -66.64$$

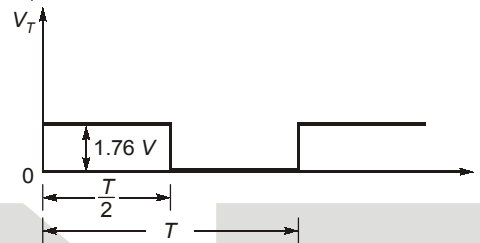
$\therefore$

$$V_T = 0.8 + 0.12 i_a$$

the load condition is a constant current of 80 A for one half cycle.



Voltage drop across thyristor is  $V_T = 0.8 + (0.012 \times 80) = 1.76 \text{ V}$



Average on state powerloss in thyristor is

$$P_{av} = \frac{1}{T} \int_0^{T/2} V_T \cdot i_a dt = \frac{1}{T} \int_0^{T/2} 1.76 \times 80 dt = \frac{1.76 \times 80 \times T}{2T}$$

$$= 70.4 \text{ W}$$

rms current rating of thyristor is,

$$I_{Th,rms} = \sqrt{\frac{(80)^2 \times T}{2T}} = 56.57 \text{ A}$$

**T3 : Solution**

(d)

$$\left(\frac{di}{dt}\right)_{\max} = \left(\frac{V_{s\max}}{L}\right)$$

$$= \frac{\sqrt{2} \times 230}{15 \times 10^{-6}} = 21.685 \text{ A}/\mu\text{s}$$

$$\left(\frac{dv}{dt}\right)_{\max} = R_s \left(\frac{di}{dt}\right)_{\max} = 10 \times 21.685$$

$$= 216.85 \text{ V}/\mu\text{sec}$$

**T4 : Solution****(d)**

KVL in the loop is,

$$-V + L \frac{di}{dt} = 0$$

$$V = L \frac{di}{dt}$$

$$dt = \frac{L}{V} di$$

Integrating on both sides,

$$\int dt = \int \frac{L}{V} di$$

$$t_{\min} = \frac{0.1}{100} \times 4 \times 10^{-3}$$

$$t_{\min} = 4 \mu\text{s}$$

∴ The minimum width of the gating pulse required to properly turn on the SCR is 4 μs.

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Publications

# 2

## Controlled and Uncontrolled Rectifiers



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

(b)

Average current rating of SCR,

$$I_{TA} = \frac{I_0}{3} = \frac{36}{3} = 12 \text{ A}$$

Average power dissipated in each SCR

$$\begin{aligned} &= I_{TA} \times V_T \\ &= 12 \times 1.4 = 16.8 \text{ W} \end{aligned}$$

#### T2 : Solution

(b)

Average output voltage

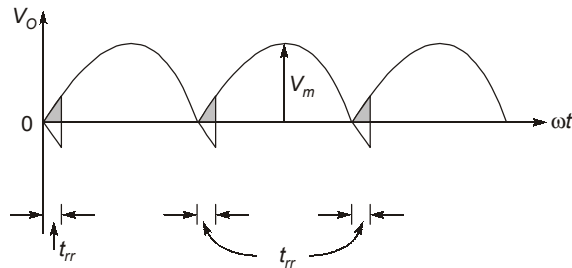
$$V_0 = \frac{2V_m}{\pi} \cos \alpha = \frac{2\sqrt{2} \times 230}{\pi} \cos 45^\circ = 146.42 \text{ V}$$

$$I_0 = \frac{V_0}{R} = \frac{146.42}{10} = 14.642 \text{ A}$$

reactive power input to the converter is

$$\begin{aligned} Q_i &= \frac{2V_m}{\pi} I_0 \sin \alpha \\ &= \frac{2\sqrt{2} \times 230}{\pi} \times 14.642 \times \sin 45^\circ \\ Q_i &= 2143.92 \text{ VAR} \end{aligned}$$

**T3 : Solution**



If reverse recovery time is taken into consideration, the diodes  $D_1$  and  $D_2$  will not be off at  $\omega t = \pi$ , but will continue to conduct until

$$t = \frac{\pi}{\omega} + t_{rr}$$

the reduction in output voltage is given by cross hatched area. Average value of this reduction in output voltage is given by

$$V_r = \frac{1}{\pi} \int_0^{t_{rr}} V_m \sin \omega t \, d(\omega t)$$

$$V_r = \frac{V_m}{\pi} (1 - \cos \omega t_{rr})$$

with zero reverse recovery time, average output voltage

$$V_0 = \frac{2V_m}{\pi} = \frac{2\sqrt{2} \times 230}{\pi} = 207.07 \text{ V}$$

for  $f = 2500 \text{ Hz}$ , the reduction in the average output voltage,

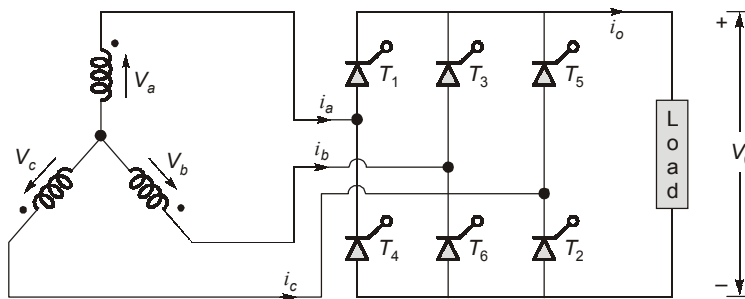
$$V_r = \frac{V_m}{\pi} (1 - \cos \omega t_{rr})$$

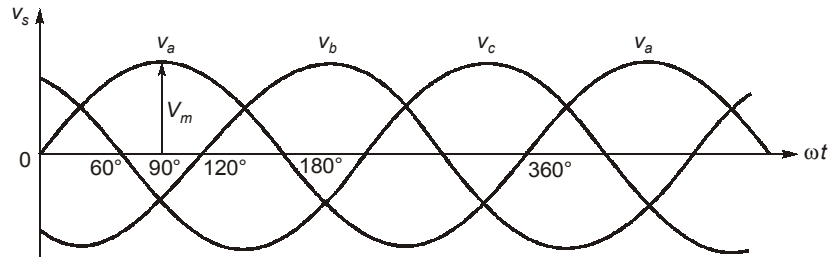
$$= \frac{\sqrt{2} \times 230}{\pi} \left( 1 - \cos 2\pi \times 2500 \times 40 \times 10^{-6} \times \frac{180}{\pi} \right) = 19.77 \text{ V}$$

percentage reduction in average output voltage =  $\frac{19.77}{207.07} \times 100 = 9.55\%$

**T4 : Solution**

(a)





$$V_A = V_m \sin \omega t$$

Phase A will get maximum voltage at  $\omega t = 90^\circ$ . At this instant

$$V_0 = V_A - V_B$$

$$V_0 = V_m \sin \omega t - V_m \sin(\omega t - 120^\circ)$$

$$= V_m - V_m \sin(-30^\circ) \quad [\because \omega t = 90^\circ]$$

$$V_0 = 1.5 V_m$$

**T5 : Solution**

(a)

The average output voltage for continuous ripple free output current is,

$$V_{0(av)} = \frac{3\sqrt{3} V_m}{2\pi} \cos \alpha$$

Here  $V_m$  is peak value of supply phase voltage. We have

$$V_{line(rms)} = 440 \text{ V}$$

$\therefore$

$$V_{ph(rms)} = \frac{V_{line}}{\sqrt{3}} = \frac{440}{\sqrt{3}} = 254.03 \text{ V}$$

$\therefore$

$$V_m = \sqrt{2} V_{ph(rms)} \\ = \sqrt{2} \times 254 = 359.21 \text{ V}$$

$\therefore$

$$V_{0(av)} = \frac{3\sqrt{3} \times 359.21}{2\pi} \cos 30^\circ = 257.26 \text{ V}$$

Average output current,

$$I_{0(av)} = \frac{V_{0(av)}}{R} = \frac{257.26}{20} = 12.86 \text{ A}$$

**T6 : Solution**

The half-wave diode rectifier uses a step-up transformer therefore, ac voltage applied to rectifier  
 $= 230 \times 460 \text{ V} = V_s$

Average value of load voltage

$$V_0 = \frac{V_m}{\pi} = \frac{\sqrt{2} \times 460}{\pi} = 207.04 \text{ V}$$

Output dc power,

$$P_{dc} = \frac{V_0^2}{R} = \frac{207.04^2}{60} = 714.43 \text{ W}$$

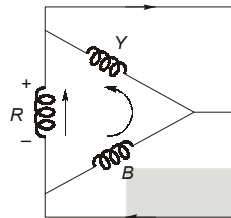
It is seen from the table that  $TUF$  for 1-phase half-wave diode rectifier is 0.2865.

$$\therefore \text{VA rating of transformer} = \frac{P_{dc}}{TUF} = \frac{714.43}{0.2865} = 2493.65 \text{ VA}$$

So choose a transformer with 2.5 kVA (next round figure) rating.

**T7 : Solution**

(b)

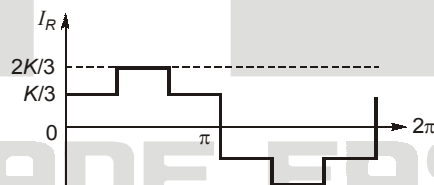


The currents are divided into  $R$  and  $YB$  winding.

Current through, 
$$R = \frac{I_0 \times 2R}{3R} = \frac{2I_0}{3}$$

Current through, 
$$BY = \frac{I_0 R}{3R} = \frac{I_0}{3}$$

Current through primary, 
$$I_p = KI_s$$





# 3

## Inverters



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

[Ans. : (a)]

#### T2 : Solution

The rms value of load current,

$$I_{O1} = \frac{230}{\sqrt{[2^2 + (8 - 6)^2]}} = 81.31 \text{ A}$$

phase angle,

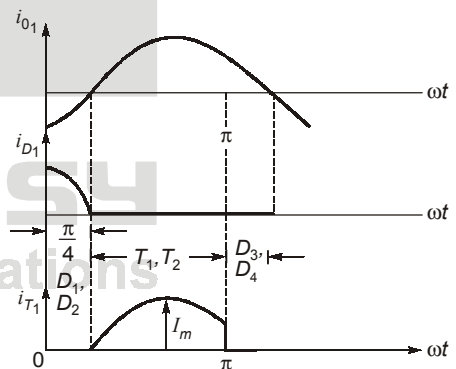
$$\phi_1 = \tan^{-1} \left( \frac{X_L - X_C}{R} \right) = 45^\circ$$

for  $R = 2 \Omega$ ,  $X_L = 8 \Omega$  and  $X_C = 6 \Omega$ , the fundamental component of load current lags the output voltage by  $45^\circ$ ,

$$\therefore I_{T1} = \sqrt{\left[ \frac{1}{2\pi} \int_0^{3\pi/4} (I_m \sin \omega t)^2 \cdot d(\omega t) \right]}$$

$$= \frac{I_m}{2\sqrt{\pi}} \left[ \omega t - \frac{\sin 2\omega t}{2} \right]_0^{3\pi/4}$$

$$\begin{aligned} &= 0.47675 I_m \\ &= 0.47675 \times \sqrt{2} \times 81.317 \\ &= 54.82 \text{ A} \end{aligned}$$



**T3 : Solution**

(d)

$$V_{03} = \frac{4V_s}{3\pi} \sin 3(\omega t) = \frac{4 \times 230}{3 \times \pi} \sin 3(\omega t) = 97.6150 \sin(942.47t)$$

$$\begin{aligned} Z_3 &= R + j\left(3\omega L - \frac{1}{3\omega C}\right) \\ &= 4 + j\left(3 \times 2\pi \times 50 \times 35 \times 10^{-3} - \frac{1}{3 \times 2\pi \times 50 \times 155 \times 10^{-6}}\right) \\ &= 4 + j(32.986 - 6.8453) \\ &= \sqrt{4^2 + (26.1407)^2} \end{aligned}$$

$$Z_3 = 26.44 \Omega$$

$$I_0 = \frac{97.6150}{\sqrt{2}} \times \frac{1}{26.44} = 2.61 \text{ A}$$

**T4 : Solution**

- (a) The load voltage waveform  $v_0$  and its fundamental component  $v_{01}$ .  
Rms value of load voltage,

$$V_{01} = \frac{4V_s}{\pi\sqrt{2}} = \frac{4 \times 230}{\pi\sqrt{2}} = 207.1 \text{ V}$$

Rms value of current,  $I_{01} = \frac{V_{01}}{Z_1}$

$$= \frac{V_{01}}{\left[R^2 + \left(\omega L - \frac{1}{\omega L}\right)^2\right]^{1/2}} = \frac{207.1}{\left[1^2 + (-1)^2\right]^{1/2}} = \frac{207.1}{\sqrt{2}} = 146.46 \text{ A}$$

$$\phi_1 = \tan^{-1} \frac{X_L - X_C}{R} = \tan^{-1}(-1) = -45^\circ$$

The fundamental component of current  $i_{01}$  as a function of time is

$$\begin{aligned} i_{01} &= \sqrt{2} I_{01} \sin(\omega t - \phi_1) \\ &= \sqrt{2} \frac{207.1}{\sqrt{2}} \sin(\omega t - 45^\circ) = 207.1 \sin(\omega t + 45^\circ) \end{aligned}$$

Load current  $i_{01}$  and source current  $i_s$  and the conducting components are also indicated.

- (b) Power delivered to load =  $I_{01}^2 R = \left(\frac{207.1}{\sqrt{2}}\right)^2 \times 1 = 21.445 \text{ kW}$

This must be equal to the power  $P_s$  delivered by the source

$$\therefore P_s = V_s I_s \text{ watts}$$

where  $I_s$  = average value of the fundamental component of source current

$$= \frac{1}{\pi} \int_0^{\pi} \sqrt{2} I_{01} \sin(\omega t + 45^\circ) d(\omega t)$$

$$= \frac{207.1}{\pi} \left[ -\cos(\omega t + 45^\circ) \right]_0^{\pi} = \frac{207.1}{\pi} [2 \cos 45^\circ] = 93.23 \text{ A}$$

$$\therefore P_s = 230 \times 93.23 = 21.443 \text{ kW}$$

- (c) Figure reveals that  $v_{T1}$  is negative for some time before  $T3$ ,  $T4$  are triggered. Thus circuit turn-off time can be obtained from

or

$$\omega t_c = \frac{\pi}{4}$$

$$t_c = \frac{1}{4} \cdot \frac{T}{2} = 0.125 \text{ ms} = 125 \mu\text{s}$$

As voltage drop in diodes D1, D2 reverse biases T1, T2 for 125  $\mu\text{s}$ , which is more than the thyristor turn-off time of 100  $\mu\text{s}$ , no forced commutation is required.

**T5 : Solution**

- (a) Here  $V_s = 220 \text{ V}$ ,  $f = 50 \text{ Hz}$ ;  $R = 6 \Omega$ ,  $L = 30 \text{ mH}$  and  $C = 180 \mu\text{F}$

$$X_L = 2\pi \times 50 \times 30 \times 10^{-3} = 9.425 \Omega \text{ and } X_C = \frac{10^6}{2\pi \times 50 \times 180} = 17.684 \Omega$$

$$Z_n = \left[ 6^2 + \left( 9.425n - \frac{17.684}{n} \right)^2 \right]^{1/2} \text{ and } \phi_n = \tan^{-1} \left[ \frac{9.425n - \frac{17.684}{n}}{6} \right]$$

(a) Rms value of output voltage,  $V_{or} = V_s = 220 \text{ V}$

Rms value of fundamental component of output voltage,

$$V_{01} = \frac{4 + 220}{\sqrt{2} \times \pi} = 198.07 \text{ V}$$

Rms value of all harmonic voltages,  $V_{oh} = \sqrt{V_{or}^2 - V_{01}^2} = \sqrt{220^2 - 198.07^2} = 95.751 \text{ V}$

$$\text{THD} = \frac{V_{oh}}{V_{01}} = \frac{95.751}{198.07} = 0.4834 \text{ or } 48.34\%$$

Distortion factor,  $\mu = \frac{V_{01}}{V_{or}} = \frac{198.07}{220} = 0.9$

- (b) Fundamental component of load current,

$$I_{01} = \frac{V_{01}}{Z_1}$$

$$\therefore I_{01} = \frac{198.07}{[6^2 + (9.425 - 17.684)^2]^{1/2}} = 19.403 \text{ A}$$

and 
$$\phi_1 = \tan^{-1} \left[ \frac{9.425 - 17.684}{6} \right] = -54^\circ$$

$$I_{03} = \frac{V_{03}}{Z_3} = \frac{4 \times 220}{3\pi \times \sqrt{2}} \times \frac{1}{\left[ 6^2 + \left( 9.425 \times 3 - \frac{17.684}{3} \right)^2 \right]^{1/2}} = 2.849 \text{ A}$$

and 
$$\phi_3 = \tan^{-1} \left[ \frac{9.425 \times 3 - \frac{17.684}{3}}{6} \right] = 75^\circ$$

$$I_{05} = \frac{V_{05}}{Z_5} = \frac{4 \times 220}{5\pi \times \sqrt{2}} \times \frac{1}{\left[ 6^2 + \left( 9.425 \times 5 - \frac{17.684}{5} \right)^2 \right]^{1/2}} = 0.9 \text{ A}$$

and 
$$\phi_5 = \tan^{-1} \left[ \frac{9.425 \times 5 - \frac{17.684}{5}}{6} \right] = 82.16^\circ$$

Similarly,  $I_{07} = 0.444 \text{ A}$  and  $\phi_7 = 84.6^\circ$

Therefore, load current expression in Fourier series is

$$\begin{aligned} i_0(t) &= \sqrt{2} [19.403 \sin(\omega t + 54^\circ)] + 2.849 \sin(3\omega t - 75^\circ) \\ &\quad + 0.9 \sin(\omega t - 82.16^\circ + 0.444 \sin(7\omega t - 84.6^\circ) + \dots] \\ &= 27.44 \sin(\omega t + 54^\circ) + 4.03 \sin(3\omega t - 75^\circ) \\ &\quad + 1.273 \sin(5\omega t - 82.16^\circ) + 0.628 \sin(7\omega t - 84.6^\circ) + \dots \end{aligned}$$

$\therefore$  Fundamental rms load current,  $I_{01} = 19.403 \text{ A}$

(c) Peak load current, 
$$I_m = [27.44^2 + 4.03^2 + 1.273^2 + 0.628^2]^{1/2} = 27.77 \text{ A}$$

Rms value of harmonic load current,

$$I_{oh} = \left[ \frac{I_m^2 + I_{m1}^2}{2} \right]^{1/2} = \left[ \frac{27.77^2 - 27.44^2}{2} \right]^{1/2} = 3.0182 \text{ A}$$

$$\text{THD} = \frac{I_{oh}}{I_{01}} = \frac{3.0182}{19.403} = 0.1555 \text{ or } 15.55\%$$

Rms load current, 
$$I_{or} = \frac{I_m}{\sqrt{2}} = \frac{27.77}{\sqrt{2}} = 19.64 \text{ A}$$

Distortion factor, 
$$\mu = \frac{I_{01}}{I_{or}} = \frac{19.403}{19.64} = 0.988$$

(d) Load power,  $P_o = I_{or}^2 \times R = 19.64^2 \times 6 = 2314.4 \text{ W}$

Average value of source current =  $\frac{P_o}{V_s} = \frac{2314.4}{220} = 10.52 \text{ A}$

(e) Expression for fundamental component of load current,  $i_{o1} = 27.44 \sin(\omega t + 54^\circ)$ . It shows that current leads the voltage by  $54^\circ$ .

$\therefore$  Conduction time of each transistor =  $(180 - 54) \times \frac{\pi}{180} \times \frac{1}{2\pi \times 50} = 7.0 \text{ ms}$

Conduction time of each diode =  $\frac{1}{2f} - 7.0 \times 10^{-3} = \frac{1}{100} - 7 \times 10^{-3} = 3 \text{ ms}$

(f) Peak transistor current,  $I_p = I_{o1m} = 27.44 \text{ A}$

Since each transistor conducts for  $126^\circ$  for every  $360^\circ$  or output cycle, rms value of transistor current,

$$I_{T1} = \frac{I_{o1m}}{2\sqrt{\pi}} \left[ 126 \times \frac{\pi}{180} - \frac{\sin 252^\circ}{2} \right] = 0.46135 I_{o1m}$$

$$= 0.46135 \times 27.44 = 12.66 \text{ A}$$

■■■■

# 4

# Choppers



## Detailed Explanation of Try Yourself Questions

### T1 : Solution

(a)

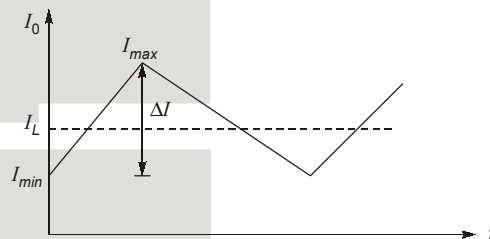
Given chopper is a buck chopper so,  $V_0 = \alpha V_s$

$$\Delta I = \frac{V_0 T_{OFF}}{L}$$

$$\Delta I = 2I_L = 2I_0$$

This is applicable only at boundary of continuous and discontinuous condition

$$L_C = \frac{\alpha V_s (1 - \alpha)}{2I_0 f}$$



### T2 : Solution

Average load current,  $I_0 = \frac{I_1 + I_2}{2} = \frac{12 + 16}{2} = 14 \text{ A}$

Average load voltage,  $V_0 = I_0 R = 14 \times 10 = 140 \text{ V}$

$$V_0 = \alpha V_s$$

$\therefore$  Duty cycle,  $\alpha = \frac{T_{ON}}{T_{ON} + T_{OFF}} = \frac{V_0}{V_s} = \frac{140}{200} = 0.7$

$$0.3 T_{ON} = 0.7 T_{OFF}$$

$$\frac{T_{ON}}{T_{OFF}} = \frac{0.7}{0.3} = 2.33$$

**T3 : Solution**

Circuit turnoff time,

$$t_c = \frac{CV_s}{I_0} = \frac{8 \times 10^{-6} \times 250}{20} = 1 \times 10^{-4} \text{ s}$$

Maximum value of duty cycle,

$$\begin{aligned} \alpha_{\max} &= (1 - 2ft_c) \\ &= (1 - 2 \times 250 \times 1 \times 10^{-4}) \\ \alpha_{\max} &= 0.95 \end{aligned}$$

maximum load or output voltage,

$$\begin{aligned} V_{0, \max} &= V_s[\alpha_{\max} + 2ft_c] \\ &= 250[0.95 + (2 \times 250 \times 1 \times 10^{-4})] \\ V_{0, \max} &= 250 \text{ V} \end{aligned}$$

**T4 : Solution**

(a)

The circuit shown in the figure is a step down chopper therefore, average output voltage,  $V_0 = \alpha V_s$

$$\Rightarrow V_0 = 0.8 \times 100 = 80 \text{ V}$$

$$I_0 = \frac{V_0}{R} = \frac{80}{8} = 10 \text{ A} \quad (\text{output current is ripple free})$$

At  $t = 0$ , capacitor is charged upto  $V_s$  with right plate positive. Now,  $T_A$  is turned on immediately after  $T_A$  is on, capacitor voltage  $V_s$  applies a reverse voltage across  $T_m$  and  $T_m$  is turned off.

So  $|V_{T_m}| = |V_c|$  Capacitor voltage

Maximum allowable reapplied  $dV/dT$  on  $T_m$  is  $50 \text{ V}/\mu\text{s}$

$$\frac{dV_c}{dt} = \frac{dV_{T_m}}{dt} = 50 \text{ V}/\mu\text{s} \quad (i)$$

$$C \frac{dV_c}{dt} = I_0$$

From equation (i),

$$C \times \left( 50 \frac{\text{V}}{\mu\text{s}} \right) = 10 \Rightarrow C = 0.2 \mu\text{s}$$



# 5

## Resonant Converters and Power Electronics Applications (Drives & SMPS)



### Detailed Explanation of Try Yourself Questions

#### T1 : Solution

(c)

The fundamental rms value of output voltage is

$$V_{0, \text{rms}} = V_{ph} \left( \frac{m}{\pi} \right) \sin \left( \frac{\pi}{m} \right) = 200 \left( \frac{3}{\pi} \right) \sin \left( \frac{\pi}{3} \right) = 165.4 \text{ V}$$

option 'c' is,  $\frac{300\sqrt{3}}{\pi} \text{ V} = 165.4 \text{ V}$

#### T2 : Solution

(b)

Peak value of output voltage for a 6 pulse converter is

$$V_{d0} = \sqrt{2} V_L \left( \frac{m}{\pi} \right) \sin \left( \frac{\pi}{m} \right) = \sqrt{2} \times 400 \times \left( \frac{6}{\pi} \right) \sin \left( \frac{\pi}{6} \right)$$

Reduction in voltage due to source inductance, for a 6 pulse converter is  $\frac{3\omega L_s}{\pi} I_0$

∴ Peak value of output voltage,

$$V_{0, \text{max}} = \left( \sqrt{2} \times 400 \times \frac{6}{\pi} \sin 30^\circ \right) - \left( \frac{3 \times 2\pi \times 50 \times 1.2 \times 10^{-3}}{\pi} \times 40 \right)$$

$$V_{0, \text{max}} = 525.789 \text{ V}$$

∴ Rms value of voltage =  $\frac{525.789}{\sqrt{2}} = 371.788 \text{ V}$



**T3 : Solution**

(b)

$$\text{Input p.f.} = \sqrt{k} = \sqrt{\frac{n}{n+m}} = \sqrt{\frac{8}{8+6}} = 0.75 \text{ lagging}$$

$$I_m = \frac{230\sqrt{2}}{15} = 21.68 \text{ A}$$

Average value of thyristor current,

$$I_{TA} = \frac{kI_m}{\pi} = \frac{0.57 \times 21.68}{\pi} = 3.93 \text{ A}$$

**T4 : Solution**

(a)

Minimum braking speed is

$$\omega_{min} = \frac{I_a r_a}{K_m} = \frac{300 \times 0.2}{1.2} = 50 \text{ rad/s or } 477.46 \text{ rpm}$$

Maximum braking speed is

$$\omega_{max} = \frac{V_s + I_a r_a}{K_m} = \frac{400 + 300 \times 0.2}{1.2} = 383.33 \text{ rad/s or } 3660.56 \text{ rpm}$$

**T5 : Solution**

At  $t = 0$ , steady state exists and therefore, generated torque = load torque

$$T_e = T_L$$

In general, the dynamic equation for the motor load combination is

generated torque = inertia torque + friction torque + load torque

$$T_e = J \frac{d\omega_m}{dt} + D\omega_m + T_L$$

As friction torque is zero,

$$D\omega_m = 0$$

The differential equation, governing the speed of the drive at  $t > 0$ ,

$$T_e = J \frac{d\omega_m}{dt} + T_L$$

$$100 = 0.01 \frac{d\omega_m}{dt} + 40 \quad \dots(i)$$

$$\frac{d\omega_m}{dt} = 6000$$

$$dt = \frac{d\omega_m}{6000}$$

Its integration gives,  $t = \frac{\omega_m}{6000} + A \quad \dots(ii)$

Initial speed at  $t = 0^+$  remains 500 rpm. Therefore,

$$\omega_{m0} = \frac{2\pi \times 500}{60} = \frac{100\pi}{6} \text{ rad/sec}$$

Substituting this value in equation (ii),

$$0 = \frac{1}{6000} \times \frac{100\pi}{6} + A \text{ or } A = \frac{-\pi}{360}$$

$$t = \frac{\omega_m}{6000} - \frac{\pi}{360}$$

Final speed,  $\omega_m = \frac{2\pi \times 1000}{60} = \frac{200\pi}{6} \text{ rad/sec}$

$$t = \frac{200\pi}{6000 \times 6} - \frac{\pi}{360} = \frac{\pi}{360} \text{ sec} = 0.0873 \text{ sec}$$

$\therefore$  Time taken for the speed to reach 1000 rpm = 0.0873 sec.

#### T6 : Solution

under rated operating conditions of the separately excited dc motor,

$$V_t = E_a + I_a r_a = k_m \omega_m + I_a r_a$$

$$220 = k_m \frac{2\pi \times 1500}{60} + 10 \times 1 = 50\pi k_m + 10$$

$\therefore$  motor constant,  $k_m = \frac{220 - 10}{50\pi} = 1.337 \text{ V-s/rad}$

for a torque of 5 Nm, motor armature current,

$$I_a = \frac{5}{1.337} = 3.74 \text{ A}$$

The equation giving the operation of converter motor is

$$V_0 = V_t = E_a + I_a r_a$$

$$\frac{2V_m}{\pi} \cos \alpha = k_m \omega_m + I_a r_a$$

$$\frac{2\sqrt{2} \times 230}{\pi} \cos 30^\circ = 1.337 \omega_m + 3.74 \times 1$$

$$\omega_m = 131.33 \text{ rad/sec}$$

$$\frac{2\pi N}{60} = 131.33 \text{ rad/sec}$$

$$N = 1254 \text{ rpm}$$

#### T6 : Solution

[Ans. : (a)]

#### T6 : Solution

[Ans. : (c)]

