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## ESE 2020 : Mains Test Series

UPSC ENGINEERING SERVICES EXAMINATION

### Electrical Engineering

#### Test-3 : Power Systems

Electrical Circuits-1 + Microprocessors-1

Digital Electronics-2 + Control Systems-2

Name : \_\_\_\_\_

Roll No : 

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#### Test Centres

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#### Student's Signature

#### Instructions for Candidates

1. Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
2. Answer must be written in English only.
3. Use only black/blue pen.
4. The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
5. Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
6. Last two pages of this booklet are provided for rough work. Strike off these two pages after completion of the examination.

#### FOR OFFICE USE

Question No.	Marks Obtained
Section-A	
Q.1	
Q.2	
Q.3	
Q.4	
Section-B	
Q.5	
Q.6	
Q.7	
Q.8	
<b>Total Marks Obtained</b>	

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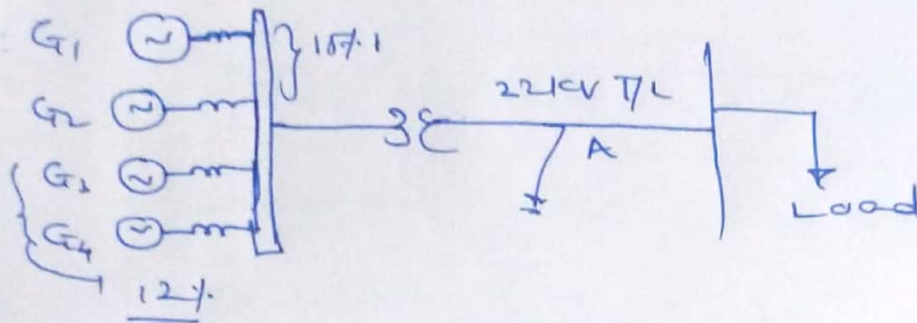
Q1) a) A power plant has four generators feeding a common bus with following rating

$G_1 \& G_2$ : 20 MVA, 15% reactance each

$G_3 \& G_4$ : 15 MVA, 12% reactance each

A 15 MVA transformer steps up the voltage and feeds a 22 kV transmission line. Determine the safe minimum reactance of transformer such that the fault level on the secondary bus of the transformer may not exceed 150 MVA, Base MVA = 20 MVA.

Sol<sup>n</sup>.



→ let us consider Base MVA = 20 MVA

∴ for  $G_1 \& G_2$ , reactances are 15%

for  $G_3 \& G_4$ , reactances will be  $\frac{15}{20} \times 12\% = 9\%$

→ If fault occurs at point A location the fault level may not exceed 150 MVA.

→ As we know that

$$\text{Short ckt MVA} = \frac{V_{LL}^2}{Z_{eq}} \times (\text{MVA})_{\text{base}}$$

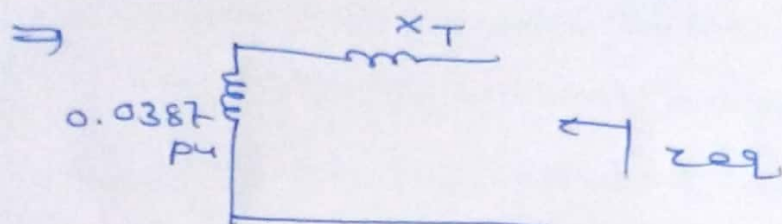
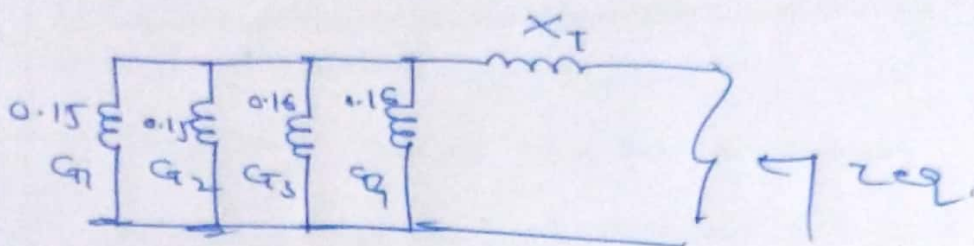
substituting given values we get

$$150 \geq \frac{1}{Z_{eq}} \times 20$$

$$\therefore \boxed{Z_{eq} \leq \frac{20}{150} \text{ pu}} \rightarrow \text{①}$$



→ let us find  $Z_{eq}$  across fault point



$$Z_{eq} = 0.0387 + X_T \text{ pu} \quad (2)$$

substituting eq<sup>n</sup> (2) in eq<sup>n</sup> (1) we get

$$(0.0387 + X_T) \leq \frac{10}{150}$$

$$\therefore X_T \leq 0.0946 \text{ pu}$$

$\therefore$  The safe minimum reactance of T/F

$$= 0.0946 \text{ pu} = 0.0946 \times \frac{(22)^2}{20}$$

$$= \underline{\underline{2.289 \Omega}}$$

- Q.1 (b) In a 132 kV system, the inductance and capacitance per phase up to the location of the circuit breaker is 10 H and 0.02  $\mu\text{F}$  respectively. If the circuit breaker interrupts to a magnetizing current of 20 A (instantaneous), current chopping occurs. Determine the voltage (in rms) which will appear across the contacts of the circuit breaker. Also calculate the value of the resistance which would be connected across the contacts to eliminate the transient restriking voltage.

[12 marks]

→ Given:- In a 132 kV system

inductance upto Location of C.B = 10 H

capacitance upto Location of C.B = 0.02  $\mu\text{F}$

Magnetizing current = 20 A

To find (i) The voltage (in rms) which will appear across the C.B.

(ii) The value of resistance

Soln.

As we know that

Energy delivered by L

= Energy stored by C

$$\therefore \frac{1}{2} Li^2 = \frac{1}{2} C V^2$$

$$\therefore V = i \sqrt{\frac{L}{C}}$$

(a) Voltage appearing across the C.B contacts after current interruption is

$$V = 20 \sqrt{\frac{10}{0.02 \times 10^{-6}}} \text{ V}$$

$$\boxed{V = 447.213 \text{ kV}}$$

$$V_{\text{rms}} = \frac{447.213}{\sqrt{2}} = \underline{\underline{316.227 \text{ kV}}}$$



(ii) The value of resistance which would be connected across the contact to eliminate the transient re-emitting voltage.

$$R = \frac{1}{2} \sqrt{\frac{L}{C}} = \frac{1}{2} \sqrt{\frac{10}{0.02 \times 10^{-6}}}$$

$$R = 11.18 \text{ K}\Omega$$

- Q.1 (c) (i) A 400 MVA synchronous machine has  $H_1 = 4.6$  MJ/MVA and 1200 MVA machine has  $H_2 = 3.0$  MJ/MVA. The two machines operate in parallel in a power plant. Find out  $H_{eq}$  relative to a 100 MVA base.
- (ii) Write down the methods of improving the transient stability limit of a power system. [8 + 4 = 12 marks]

→ (i) Given:-

Machine ①:  $G_1 = 400$  MVA,  
 $H_1 = 4.6$  MJ/MVA

Machine ②:  $G_2 = 1200$  MVA  
 $H_2 = 3.0$  MJ/MVA

To find:  $H_{eq}$  relative to 100 MVA base

Soln:

Let us first of all find out total kinetic energy present in system

$$\therefore (K.E.)_T = G_1 H_1 + G_2 H_2$$

substituting given values we get

$$\begin{aligned} (K.E.)_T &= 400 \times 4.6 + 1200 \times 3 \\ &= 5440 \text{ MJ} \end{aligned}$$

As we know that

$$(K.E.)_T = G_{eq} \cdot H_{eq}$$

$$5440 = 100 \cdot H_{eq}$$

$$\therefore H_{eq} = \frac{5440}{100} \text{ MJ/MVA}$$

$$\therefore \boxed{H_{eq} = 54.40 \text{ MJ/MVA}}$$

$\therefore$  The  $H_{eq}$  relative to 100 MVA base is  
 $H_{eq} = 54.40 \text{ MJ/MVA}$

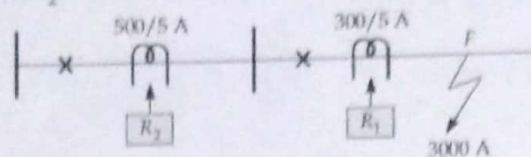


② Methods of improving the transient stability limit of a power system

$$M \frac{d^2 \delta}{dt^2} = P_m - P_{m_{\max}} \sin \delta = P_m - \left| \frac{V_s V_R}{x_L} \right| \sin \delta$$

- $P_e$  is controlled by controlling voltage and line reactance using series capacitance, double circuit line & bundle conductor for improvement of system stability
- Fast acting governing valve controls  $P_m$   
Fast operating excitation controls generator voltage
- by using dynamic breaking [resistance switching] during fault condition the difference of  $P_m$  &  $P_e$  is reduced
- Single pole switching
- Generator with neutral resistance.
- FACT devices, SVCs & compensators
- HVDC line along with HVAC line improve the stability.

Q.1 (d) Two relays  $R_1$  and  $R_2$  are connected in two sections to a feeder as shown in figure below.



Relay  $R_1$  : CT ratio = 300/5,  $P_s = 50\%$ , TMS = 0.3

Relay  $R_2$  : CT ratio = 500/5,  $P_s = 75\%$

PSM	2	4	5	8	12	20
Operating time in seconds	10	5	4.7	3	2.8	2.4

A fault at 'F' results in a fault current of 3000 A. Find TMS of  $R_2$  to give time grading margin of 0.5 sec between the relays.

[12 marks]

Soln.

Here fault current in relay  $R_1$  is

$$\therefore I_{R_1} = \frac{3000 \times 5}{300} = 50 \text{ A}$$

Now,

Relay operating current =  $\frac{\text{current} \times \text{Rated secondary setting}}{\text{current of CT}}$

$$= \frac{50}{100} \times 5$$

$$= 2.5 \text{ A}$$

$$\text{PSM} = \frac{I_{R_1}}{\text{Relay operating current}} = \frac{50}{2.5} = 20$$

Since, operating time corresponding to a PSM of 20 is 2.4 sec

$$\therefore \text{Actual operating time of Relay } R_1 (t_{R_1})$$

$$= (\text{PSM})_1 \times 2.4 = 0.3 \times 2.4 = \underline{\underline{0.72 \text{ sec}}}$$



Fault current in relay  $R_2$  is

$$(I_{R_2}) = \frac{3000}{500} \times 5 = 30 \text{ A.}$$

$$\begin{aligned} \text{PSM of this current} &= \frac{I_{R_2}}{\text{Relay operating current}} \\ &= \frac{30 \text{ A}}{\text{C.S. X Rated secondary current of C.T.}} \\ &= \frac{30 \text{ A}}{0.75 \times 5} \end{aligned}$$

$$\therefore \text{PSM} = 8$$

Since operating time corresponding to a PSM of 8 is 3 sec and as the relay  $R_2$  should operate 0.5 sec after the operation of relay  $R_1$  therefore operating time of relay  $R_2$  is

$$t_{R_2} = 0.72 \times 0.5 = \underline{\underline{1.22 \text{ sec}}}$$

Also, TMS for relay  $R_2$

$$R_2 = \frac{1.22}{3} = \underline{\underline{0.406}}$$

$$\therefore \text{TMS for relay } R_2 \text{ is } \underline{\underline{0.406}}$$

- Q.1 (e) (i) A 100 MVA, two-pole, 50 Hz generator has a moment of inertia  $40 \times 10^3 \text{ kg-m}^2$ . What is the energy stored in the rotor at the rated speed? What is the corresponding angular momentum? Determine the inertia constant  $H$ ?
- (ii) The inertia constant for a 60 Hz, 100 MVA generator is 5.5 MJ/MVA. Determine the acceleration (in  $^\circ/\text{s}^2$ ) imparted to the rotor if the input to generator is suddenly increased by 30 MVA.

[8 + 4 = 12 marks]

→ Given: MVA ratings = 100 MVA

Moment of Inertia ( $J$ ) =  $40 \times 10^3 \text{ kg-m}^2$

To find: (i) (K.E.)<sub>T</sub>

(ii) Angular momentum

(iii) Inertia constant ( $H$ )

Sol<sup>n</sup>

Energy stored in rotor at rated speed =  $\frac{1}{2} J \omega^2$

$$= \frac{1}{2} \times J \times (2\pi f)^2$$

$$(K.E.)_T = \frac{1}{2} \times 40 \times 10^3 \times (2\pi \times 50)^2$$

$$\therefore (K.E.)_T = 1973.92 \text{ MJ}$$

→ Angular momentum =  $J \omega$

$$= 40 \times 10^3 \times 2\pi \times 50$$

$$= 12.5663 \text{ M kg-m}^2/\text{sec}$$

$$\therefore \text{Angular momentum} = 12.5663 \text{ M kg-m}^2/\text{sec}$$

→ Inertia constant  $H = \frac{(K.E.)_T}{\text{MVA}}$

$$\therefore H = \frac{1973.92 \text{ MJ}}{100 \text{ MVA}}$$

$$\therefore H = 19.7392 \text{ MJ/MVA}$$



(ii) Given:-  $H = 5.5 \text{ MJ/MVA}$   
 $C_F = 100 \text{ MVA}$ ,  $\Delta P = 30 \text{ MVA}$   
 $F = 60 \text{ Hz}$   
To find:- Acceleration (in  $\text{degree/s}^2$ )

Soln:-

According to swing equation

$$M \frac{d^2 \delta}{dt^2} = P_m - P_e$$

$$\frac{GH}{180 \cdot F} \frac{d^2 \delta}{dt^2} = P_m - P_e \quad \text{--- (1)}$$

As it is given that generator input is suddenly increased by 30 MVA

by substituting given value in eqn (1), we get

$$\begin{aligned} \frac{d^2 \delta}{dt^2} &= \frac{\Delta P_m \times 180 \times F}{C_F \times H} \\ &= \frac{30 \times 180 \times 60}{100 \times 5.5} \end{aligned}$$

$$\boxed{\frac{d^2 \delta}{dt^2} = 589.09 \text{ degree/s}^2}$$

∴ The acceleration (in  $\text{degree/s}^2$ ) imparted due to the rotor if the  $\Delta P$  to generator is suddenly increased by 30 MVA is 589.09 degree/s<sup>2</sup>

Q.4 (a) A 60 Hz, 4-pole turbogenerator rated 100 MVA, 13.8 kV has an inertia constant of 10 MJ/MVA:

- Find the stored energy in the rotor at synchronous speed.
- If the input to the generator is suddenly raised to 60 MW for an electrical load of 50 MW, find rotor acceleration in rpm/sec.
- If the rotor acceleration calculated in part (ii) is maintained for 12 cycles, find the change in torque angle and rotor speed in rpm at the end of this period.

[20 marks]

→ Given:- 4 pole, 60 Hz,  $S_{MVA} = 100 \text{ MVA}$ ,  
 $H = 10 \text{ MJ/MVA}$

(i) Stored kinetic energy in rotor at synchronous speed

$$KE = H \cdot S_{MVA} = 100 \times 10 = 1000 \text{ MJ}$$

$$\therefore \boxed{KE = 1000 \text{ MJ}}$$

(ii) By using swing equation

$$\frac{2H}{s} \frac{d^2\delta}{dt^2} = P_m - P_e = P_a$$

$P_m$  - Initial mechanical input

$P_e$  - Electrical developed power

$P_a$  - Accelerating power

$$M = \frac{H \cdot S}{\pi \cdot f} = \frac{1000 \text{ MJ}}{\pi \times 60} = 6.366 \text{ MJ-sec/elect. rad.}$$

$$P_a = 60 - 50 = 10 \text{ MW}$$

$$\therefore \frac{d^2\delta}{dt^2} = \frac{P_a}{M}$$

$$= \frac{10 \text{ MW}}{6.366 \text{ MJ-sec/elect. rad}}$$



$$\frac{d^2\delta}{dt^2} = \frac{10}{6.366} = 1.57 \text{ rad/sec}$$

$$\omega = \frac{60}{2\pi} (\omega) \times \frac{2}{P}$$

$$\alpha = \frac{d^2\delta}{dt^2} = \frac{60}{2\pi} \times 1.57 \times \frac{2}{4} = 7.5 \text{ rpm/sec}$$

$$\therefore \boxed{\alpha = 7.5 \text{ RPM/sec}}$$

(ii) Acceleration is constant for a 12 cycles

$$12T = 12 \times \frac{1}{60} = 0.2 \text{ sec.}$$

New load angle  $\Rightarrow \delta = \delta_0 + \Delta\delta$

change in angle  $\Rightarrow \Delta\delta = \frac{1}{2} \alpha t^2$

$$\Delta\delta = \frac{1}{2} \times 1.57 \times (0.2)^2$$

$$\therefore \boxed{\Delta\delta = 0.0314 \text{ rad}}$$

$\therefore$  The change in torque angle is

$$\underline{\underline{0.0314 \text{ rad.}}}$$

(iii) New speed of rotor

$$N = N_0 + \Delta N \quad \rightarrow (1)$$

$N_0 \rightarrow$  Initial rotating synchronous speed of rotor

$$N_0 = \frac{120F}{P} = \frac{120 \times 60}{4} = \underline{\underline{1800 \text{ rpm}}}$$

$$\Delta N = \alpha t = 1.57 \times 7.5 \times 10^{-2}$$

$$\boxed{\Delta N = 1.5 \text{ rpm}}$$

Substituting this value in eq<sup>n</sup> (1) we get

$$N = 1800 + 1.5$$

$$\boxed{N = 1801.5 \text{ rpm}}$$

$\therefore$  The rotor speed in rpm at the end of this period is

$$\boxed{N = 1801.5 \text{ rpm}}$$

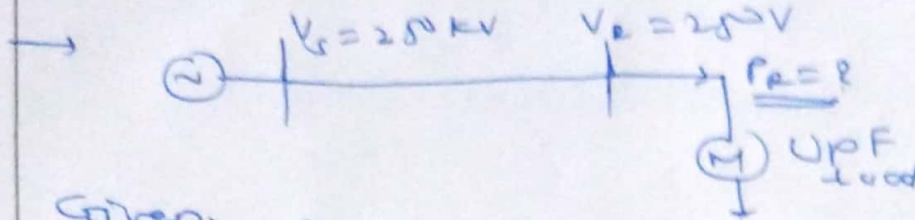


Q.4 (b) A 250 kV transmission line has line constants as shown below:

$$A = 0.80 \angle 2^\circ \text{ and } B = 190 \angle 78^\circ \Omega$$

If the voltage at receiving and sending end is maintained at 250 kV, then determine power which can be received at unity power factor. What value of compensation will be required for a load of 180 MW at unity power factor with the same voltage profile?

[20 marks]



Given:

$$A = 0.80 \angle 2^\circ = |A| \angle \alpha$$

$$B = 190 \angle 78^\circ = |B| \angle \beta$$

To find:  $P_R$

Sol<sup>n</sup>: As the load, operating at receiving end is at unity power factor.

$$\therefore \underline{Q_R = 0}$$

As we know that

$$Q_R = \left| \frac{V_S V_R}{B} \right| \sin(\beta - \delta) - \frac{|A| |V_R|^2}{|B|} \sin(\beta - \alpha)$$

Substituting given value we get ( $V_S = V_R$ )

$$Q_R = \left| \frac{(V_R)^2}{B} \right| \sin(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) = 0$$

$$\frac{V_R^2}{B} \sin(\beta - \delta) = \frac{A V_R^2}{B} \sin(\beta - \alpha)$$

$$\sin(78 - \delta) = 0.8 \sin(78 - 2)$$

$$\delta = 78 - \sin^{-1}(0.8 \sin 76)$$

$$\therefore \boxed{\delta = 27.082^\circ}$$

As we know that

$$P_R = \left| \frac{V_S V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

$$= \left| \frac{(250)^2}{190} \right| \cos(78^\circ - 27.65^\circ) - \left| \frac{0.8 \times (250)^2}{190} \right| \cos(78^\circ - 2^\circ)$$

→ substituting given values

$$P_R = 143.70 \text{ MW}$$

∴ The power which can be received at unity power factor is 143.70 MW

- ② As from above value of  $P_R$  given value of  $P_R = 180 \text{ MW}$  is more due to which power factor will change but we will have maintain constant. for that we will have to inject reactive power.

→ First of all we find  $\delta$ .

$$P_R = \left| \frac{V_S V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

$$180 = \frac{(250)^2}{190} \cos(78^\circ - \delta) - \frac{0.8 \times 250^2}{190} \cos(76^\circ)$$

$$\therefore \frac{(250)^2}{190} \cos(78^\circ - \delta) = 243.66$$

$$\therefore \boxed{\delta = 35.794^\circ}$$



Now let us find  $Q_R$  at this  $\delta$

$$Q_R = \left| \frac{V_S V_R}{B} \right| \sin(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha)$$

$$Q_R = \frac{(250)^2}{190} \sin(76 - 35.79) - \frac{0.8 \times 250^2}{190} \sin 76^\circ$$

$$\therefore Q_R = -34.355 \text{ MVAR}$$

→ So to maintain constant unity power factor we have to inject 34.355 MVAR reactive power into system through shunt capacitor

$$Q_{\text{injected}} = 34.355 \text{ MVAR}$$

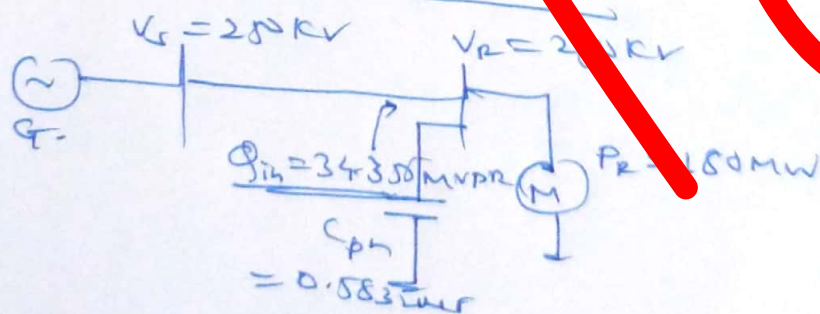
$$\rightarrow Q_C = 34.355 \quad Q_{Cph} = \frac{34.355}{3} = 11.45 \text{ MVAR}$$

$$\frac{V^2}{X_C} = 11.45 \text{ MVAR}$$

$$V^2 \omega C = 11.45 \text{ MVAR}$$

$$C_{ph} = \frac{11.45}{(250)^2 \times 4\pi \times 10^{-6}}$$

$$\therefore C_{ph} = 0.5832 \mu\text{F}$$



- Q.4 (c) A 3- $\phi$ , 50 Hz transmission line of length of 100 km is delivering 20 MW at 0.9 p.f. lagging at 110 kV. The resistance and reactance of the line per phase per km are 0.2 and 0.4  $\Omega$  respectively, while capacitance admittance is  $2.5 \times 10^{-6}$  Siemen/km/phase.

Determine:

- the current and voltage at sending end
- efficiency of transmission

Using nominal T-method, also obtain equivalent T-model and phasor diagram.

[20 marks]

→ Soln,

$$Z = R + j\omega L = (0.2 + j0.4) \times 100$$

$$\therefore |Z| = 20 + j40 \Omega/\text{ph} = 44.721 \angle 63.434^\circ$$

$$Y = 2.5 \times 10^{-6} \times 100 = j2.5 \times 10^{-4} \text{ Siemen/ph}$$

As here we have to use nominal T-method

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 + \frac{YZ}{2} & Z \left(1 + \frac{YZ}{2}\right) \\ Y & 1 + \frac{YZ}{2} \end{bmatrix}$$

$$\rightarrow A = 1 + \frac{YZ}{2} = 1 + \frac{(20 + j40)(j2.5 \times 10^{-4})}{2}$$

$$\therefore A = 0.995 \angle 0.143^\circ$$

$$\rightarrow B = Z \left(1 + \frac{YZ}{2}\right) = 44.721 \angle 63.434^\circ \times 0.995 \angle 0.143^\circ$$

$$B = 44.497 \angle 63.434^\circ$$



$$C = Y = 2.5 \times 10^{-4} \angle 90^\circ$$

$$D = 1 + \frac{YZ}{\Delta} = 0.995 \angle 0.143^\circ$$

$$V_S = A V_R + B I_R \quad \text{--- (1)}$$

$$I_S = C V_R + D I_R \quad \text{--- (2)}$$

$$= 0.995 \angle 0.143^\circ \times$$

$$\rightarrow V_R = \frac{110}{\sqrt{3}} = 63.508 \text{ kV}$$

$$\rightarrow I_R = \frac{P_R}{\sqrt{3} \times V_L \times 0.9} = \frac{104.972}{0.9} \angle -25.841^\circ$$

substituting values in eqn (1) & (2)  $= 114.635^\circ$   
 $\angle -25.841^\circ$

$$\rightarrow V_S = 0.995 \angle 0.143^\circ \times 63.508 \angle 0^\circ \text{ kV}$$

$$+ 44.497 \angle 63.435^\circ \times \frac{104.972}{0.9} \angle -25.841^\circ$$

$$V_{S_{ph}} = 66.958 \angle 2.574^\circ \text{ kV}$$

$$V_{ph} = 67.384 \angle 2.827^\circ \text{ kV}$$

$$\rightarrow I_S = 2.5 \times 10^{-4} \angle 90^\circ \times 63.508 \text{ kV}$$

$$+ 0.995 \angle 0.143^\circ \times \frac{104.972}{0.9} \angle -25.841^\circ$$

$$I_S = 98.605 \angle -17.35^\circ \text{ A}$$

$$I = 114.1 \angle -18.231^\circ \text{ A}$$

$$\rightarrow P_S = 3 V_{ph} I_{ph} \cos \phi$$

$$P_S = 3 \times 66.956 \times 98.605 \times 10^3$$

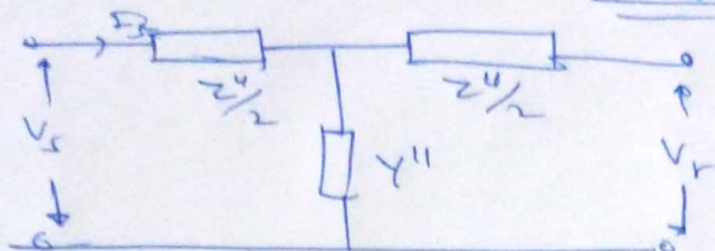
$$\cos (19.924)$$

$$P_S = 18.62 \text{ MW} = 20.77 \text{ MW}$$

$$\text{efficiency} = \frac{P_R}{P_S} \times 100 = \frac{20}{20.77} \times 100$$

$$\text{efficiency} = 96.29\%$$

→ Equivalent T-model  $r = \sqrt{ZY} = 0.1057$



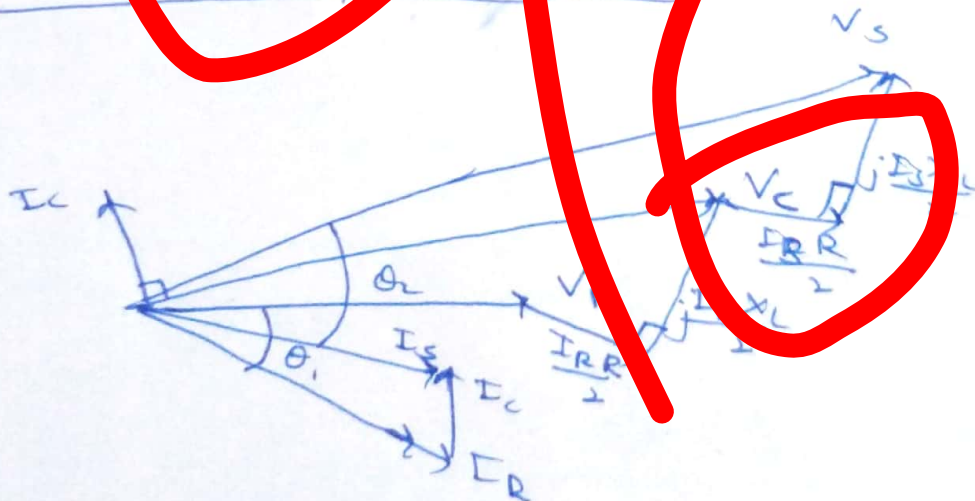
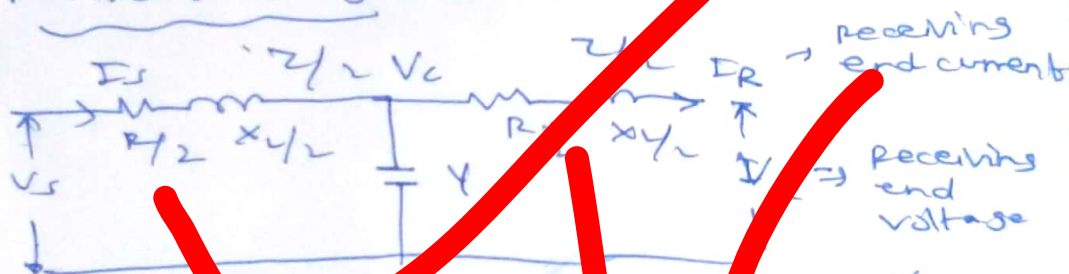
$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 + \frac{Y'' Z''}{2} & Z'' \left(1 + \frac{Y'' Z''}{2}\right) \\ Y'' & 1 + \frac{Y'' Z''}{2} \end{bmatrix} \begin{bmatrix} V_r \\ I_r \end{bmatrix}$$

$$\frac{Z''}{2} = \frac{Z}{2} \frac{\tanh(r l / 2)}{(r l / 2)} = \underline{4.230 \angle 63.43^\circ}$$

$$Y'' = Y \frac{\sinh r l}{r l} = \frac{2.5 \times 10^{-4} \angle 90^\circ \sinh(0.1057 \times 200)}{0.1057 \times 200}$$

$$\underline{Y'' = 4.3386 \times 10^{-6} \angle 90^\circ}$$

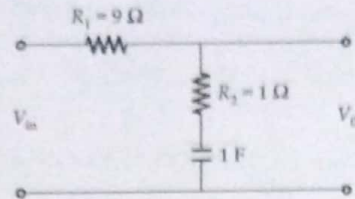
Phasor diagram





Section B : Power Systems + Electrical Circuits-1 + Microprocessors-1  
+ Digital Electronics-2 + Control Systems-2

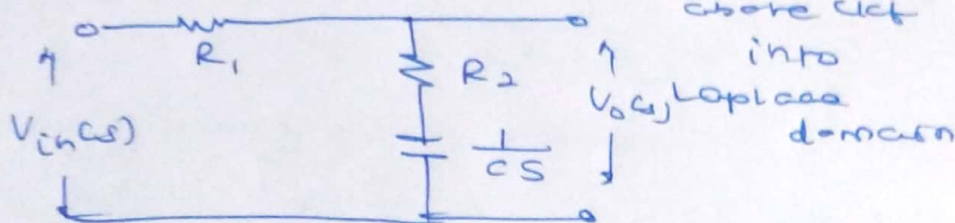
Q.5 (a) For the network shown in the figure below:



Find the frequency (in rad/sec) at which the maximum phase lag occurs?

[12 marks]

→ First of all let us find our transfer function of the system.



→ Applying voltage division rule, we get

$$V_o(s) = \frac{R_2 + \frac{1}{Cs}}{R_1 + R_2 + \frac{1}{Cs}} \times V_i(s)$$

$$\therefore \frac{V_o(s)}{V_i(s)} = \frac{1 + R_2Cs}{1 + (R_1 + R_2)Cs} = \frac{R_2C \left[ s + \frac{1}{R_2C} \right]}{(R_1 + R_2)C \left[ s + \frac{1}{(R_1 + R_2)C} \right]}$$

$$\therefore \frac{V_o(s)}{V_i(s)} = \left( \frac{R_1}{R_2 + R_1} \right) \left( \frac{s + \frac{1}{R_2C}}{s + \frac{1}{(R_1 + R_2)C}} \right)$$

$$\therefore \text{T.F.} = \left( \frac{R_1}{R_2 + R_1} \right) \left[ \frac{s + \frac{1}{R_2C}}{s + \frac{1}{(R_1 + R_2)C}} \right]$$

→ As we know that the frequency at which the maximum phase lag occurs is given by ~~where~~

$$\omega^2 = \text{product of locations of poles \& zeros}$$

$$\therefore \omega^2 = \frac{1}{R_2 C} \times \frac{1}{(R_1 + R_2) C}$$

$$\therefore \omega = \sqrt{\frac{1}{R_2 C (R_1 + R_2) C}}$$

substituting given values

$$R_1 = 9 \Omega, R_2 = 1 \Omega, C = F \text{ we get}$$

$$\omega = \frac{1}{\sqrt{1 \times 10 \times 1}}$$

$$\omega = 0.316 \text{ rad/sec}$$

$\therefore$  The frequency at which the maximum phase lag occurs = 0.316 rad/sec



Q.5(b) Design and implement a mod-10 asynchronous up counter using T-flip-flops.

[12 marks]

→ To implement Mod-10 counter, At 10<sup>th</sup> counter All Flip Flops should be reset.

→ For implementation of mod-10 counter we will require 4 Flip-flops.

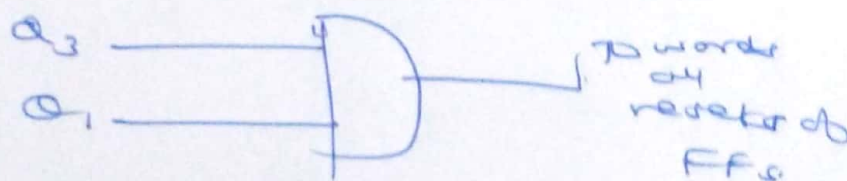
→ Truth Table,

	$Q_3$	$Q_2$	$Q_1$	$Q_0$
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10	1	0	1	0

Mod 10  
Counter

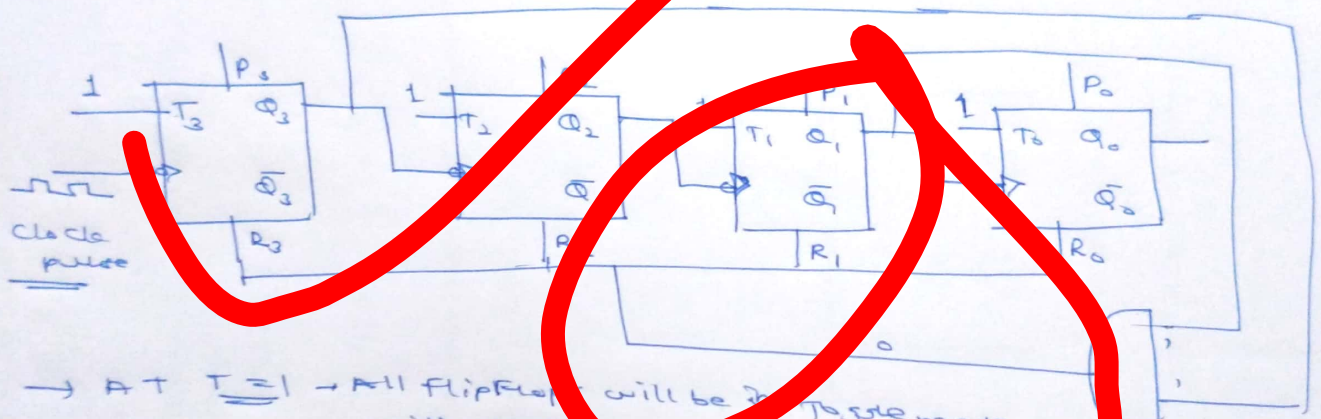
→ At this count all FF should be reset

→ Logic ckt



design

## Mod 10 Asynchronous counter



- At  $T=1$  → All flip-flops will be in Toggle mode will work as counter.
- output of one FF is given to input of other flip-flop → Asynchronous.
- Negative edge triggering with  $Q$  connected to  $\neg F$ . → Up counter



- Q.5 (c) Find the solution of state equation, state transition matrix and output of the system having state model is as given below and taking input as unit step.

$$\dot{x} = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u \text{ and } y = [1 \quad 1] x$$

and

$$x(0) = [1 \quad 0]^T$$

[12 marks]

→ Comparing above equation with following state equations

$$\dot{x} = A x + B u, \quad y = C x + D u$$

we get

$$A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad C = [1 \quad 1]$$

→ let us find state transition matrix

$$[sI - A]^{-1} = \begin{bmatrix} s-1 & 0 \\ -1 & s-1 \end{bmatrix}$$

$$[sI - A]^{-1} = \frac{\begin{bmatrix} s-1 & 0 \\ 1 & s-1 \end{bmatrix}}{(s-1)^2} \rightarrow \text{①}$$

State transition matrix =  $\phi(t)$

$$= L^{-1} (sI - A)^{-1}$$

$$= L^{-1} \begin{bmatrix} \frac{1}{s-1} & 0 \\ \frac{1}{(s-1)^2} & \frac{1}{(s-1)} \end{bmatrix}$$

$$\phi(t) = \begin{bmatrix} e^t u(t) & 0 \\ t e^t u(t) & e^t u(t) \end{bmatrix}$$

→ As we know that

$$\dot{x} = Ax + Bu \quad \text{--- (1)} \quad y = Cx + Du \quad \text{--- (2)}$$

Taking Laplace Transform on eq<sup>n</sup> (1) →

$$sX(s) - x(0) = AX(s) + BU(s)$$

$$X(s) = [sI - A]^{-1} B U(s) + [sI - A]^{-1} x(0)$$

substituting value from eq<sup>n</sup> (2) we get

$$X(s) = \begin{bmatrix} \frac{1}{s-1} & 0 \\ \frac{1}{(s-1)^2} & \frac{1}{s-1} \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} U(s) + \begin{bmatrix} \frac{1}{s-1} & 0 \\ \frac{1}{(s-1)^2} & \frac{1}{(s-1)} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$X(s) = \begin{bmatrix} \frac{1}{s-1} \\ \frac{1}{(s-1)^2} + \frac{1}{(s-1)} \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} U(s) + \begin{bmatrix} \frac{1}{s-1} \\ \frac{1}{(s-1)^2} \end{bmatrix}$$

$$X(s) = \begin{bmatrix} \frac{1}{s} \frac{1}{(s-1)} + \frac{1}{(s-1)} \\ \frac{1}{s} \left( \frac{1}{(s-1)^2} + \frac{1}{(s-1)} \right) + \frac{1}{(s-1)^2} \end{bmatrix}$$

Taking Inverse Laplace Transform we get

$$x(t) = \begin{bmatrix} (e^t - 1)u(t) + e^t u(t) \\ 2te^t u(t) \end{bmatrix}$$

$$y(s) = [1 \quad 1] X(s)$$

$$y(s) = \frac{1}{s} \frac{1}{(s-1)} + \frac{1}{(s-1)} + \frac{1}{s(s-1)^2} + \frac{1}{s(s-1)} + \frac{1}{(s-1)^2}$$

Taking inverse Laplace Transform we get

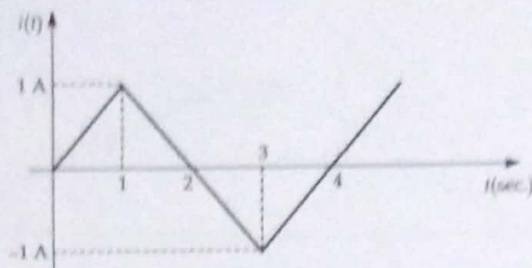
$$y(t) = e^t u(t) - u(t) + e^t u(t) + u(t) + e^t u(t) + te^t u(t) + te^t u(t)$$

$$y(t) = (2e^t + 2te^t - 1)u(t)$$



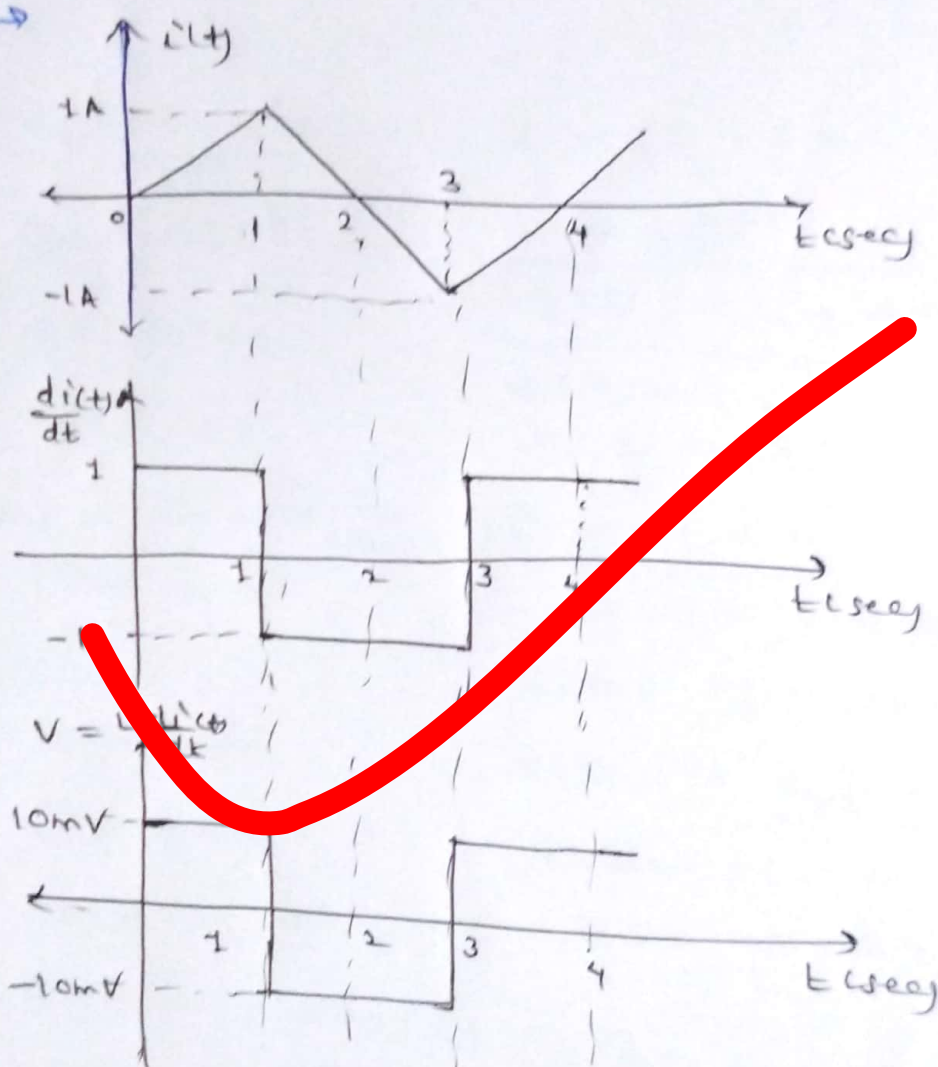
Q.5 (d) A current source, having waveform shown below is connected across the terminals of an inductor of 10 mH.

Draw: (i) The voltage waveform and  
(ii) The charge waveform through the device.



Assume the initial conditions through the inductor to be zero.

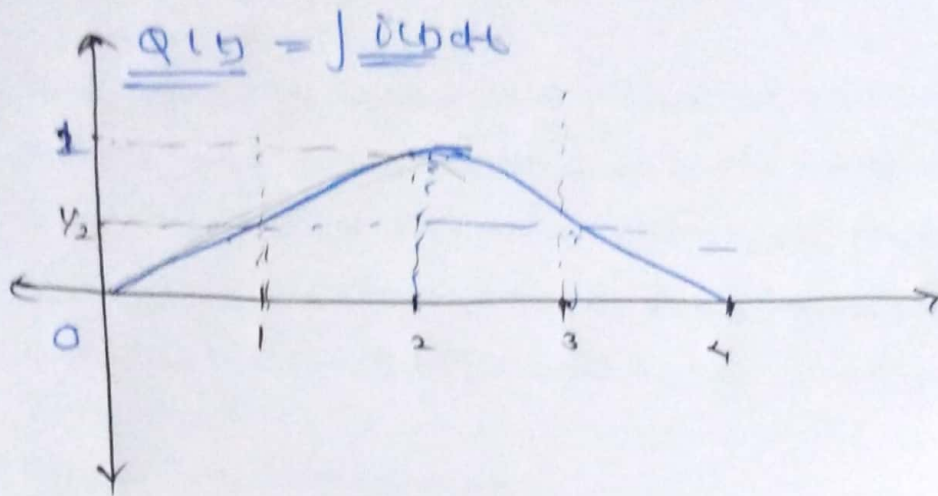
[12 marks]



As we know that In case of inductor

$$V = L \frac{di}{dt}$$

→ ② The charge  $Q = \int i dt$



→ ①  $0 < t < 2$

$$Q = \int i dt$$

$$Q = \int t dt$$

$$Q = \frac{t^2}{2} + C$$

As initial cond<sup>n</sup>s are zero

$$Q = \frac{t^2}{2} + C$$

$$Q(1) = \frac{1}{2} C$$

②  $2 < t < 4$

$$Q(t) = \int i dt$$

$$Q(t) = \int (-t + 2) dt$$

$$Q(t) = -\frac{t^2}{2} + 2t + C$$

$$\text{At } t=1, Q(1) = \frac{1}{2}$$

$$\therefore \frac{1}{2} = -\frac{1}{2} + 2 + C$$

$$\therefore C = 1$$

$$\therefore Q(t) = -\frac{t^2}{2} + 2t + 1$$

$$Q(2) = 1$$

$$Q(3) = 0.5 C$$

③  $3 < t < 4$

$$Q(t) = \int i dt$$

$$Q(t) = \int (t - 4) dt$$

$$Q(t) = \frac{t^2}{2} - 4t + C$$

$$Q(3) = 0.5 C$$

$$\therefore 0.5 = 4.5 - 12 + C$$

$$C = 8$$

$$Q(t) = \frac{t^2}{2} - 4t + 8$$

$$Q(4) = 0 C$$



Q.5 (e) Write about the flag register in 8085 microprocessor.

[12 marks]

- The flag register is a special purpose register.
- Depending upon the value of result after any arithmetic & logical operation the flag bits become set (1) or reset (0).
- In 8085 microprocessor, flag register consists of 8 bits and only 5 of them are useful.
- The five flags are

D7	D6	D5	D4	D3	D2	D1	D0
S	Z	X	A	X	P	X	CY

### ① Sign flag (S) :

After any operation, if the MSB (Bit 7) of the result is 1, it indicates the number is negative and the sign bit becomes set i.e. 1. If the MSB is 0, it indicates the number is positive and the sign flag becomes reset i.e. 0.

From 00H to 7FH, sign flag is 0.

From 80H to FFH, sign flag is 1.

### ② Zero flag (Z)

After any arithmetic or logical operation if the result is 0 (0000H), the zero flag becomes set i.e. 1. otherwise it becomes reset i.e. 0.

i.e. for 00H - zero flag is 1  
from 01H to FFH, - zero flag is 0  
→ zero flag = 1 - zero result  
0 - non-zero result

### ③ Auxiliary carry flag (AC)

→ This flag is used in BCD number system  
→ If after any arithmetic or logical operation  
BCD generated any carry and passed on to  
BC4 this flag becomes set, i.e. 1,  
otherwise it becomes reset i.e. 0.  
→ This is the only flag register which is  
not accessible by programs

### ④ Parity flag (P)

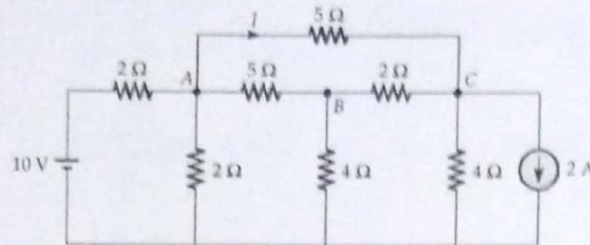
→ If after any arithmetic or logical operation  
the result has even parity, an even number  
of 1 bits, the parity register becomes set  
i.e. 1, otherwise it becomes reset i.e. 0.  
→ 1 → Accumulator has even number of 1 bits  
0 → accumulator has odd number of 1 bits

### ⑤ Carry flag (CF)

→ Carry is generated when performing binary  
operations and the result is more than  $2^n$   
bits then this flag becomes set i.e. 1  
otherwise it becomes reset i.e. 0  
→ Carry flag is also called borrow flag



- Q.6 (a) (i) A constant voltage at a frequency of 1 MHz is applied to an inductor in series with a variable capacitor. When the capacitor is set to 500 pF, the current has its maximum value while, it is reduced to one-half when the capacitance is 600 pF. Find resistance, inductance and Q-factor of inductor.
- (ii) Calculate the current flowing in 5  $\Omega$  branch AC of the circuit shown in figure using nodal analysis.



[10 + 10 = 20 marks]

Soln  
(i)



V, 1 MHz freq.

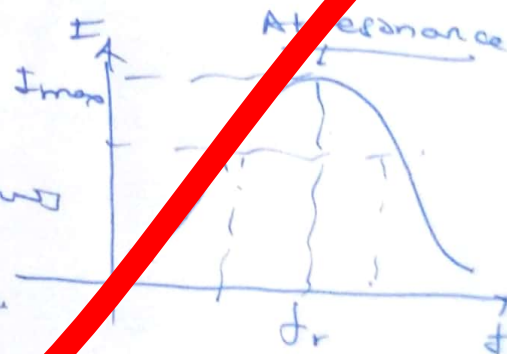
when  $C = 500 \text{ pF} \rightarrow I = I_{\text{max}}$

$C = 600 \text{ pF} \rightarrow I = \frac{I_{\text{max}}}{2}$

To find  $R, L$  &  $Q$  coil

Soln:-

As we know that  
At resonance, the  
maximum current flows  
through the circuit &  
impedance is resistive.



$Z_R = R, X_L = X_C$  ← At resonance

so here at  $f = 1 \text{ MHz}, I = I_{\text{max}}$

$\therefore X_L = X_C \Rightarrow \omega L = \frac{1}{\omega C}$

$$\therefore Q = \frac{1}{\omega^2 C}$$

$$\therefore L = \frac{1}{(2\pi f)^2 \times C} = \frac{1}{(2\pi \times 1 \times 10^6)^2 \times 500 \times 10^{-12}}$$

$$\therefore L = \frac{1}{4\pi^2 \times 500} = 50.66 \mu\text{H}$$

$$\therefore \boxed{L = 50.66 \mu\text{H}} \rightarrow (1)$$

$$\rightarrow \text{At } \frac{I_{\text{max}}}{2} = I, C = 600 \text{ pF}$$

$$\therefore |Z| = \frac{|V|}{|I|} = \frac{|V|}{\frac{I_{\text{max}}}{2}} = 2 \frac{|V|}{I_{\text{max}}} = 2R$$

As we know that At resonance

$$\boxed{\frac{|V|}{I_{\text{max}}} = R}$$

$$\therefore 2R = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\therefore 4R^2 = R^2 + (X_L - X_C)^2 \rightarrow \text{Taking square on both sides}$$

$$\therefore R = \frac{(X_L - X_C)}{\sqrt{3}} = \frac{(\omega L - \frac{1}{\omega C})}{\sqrt{3}}$$

$$\therefore R = \frac{(2\pi f \times 50.66 \mu - \frac{1}{2\pi f \times 600 \times 10^{-12}})}{\sqrt{3}}$$

$$\therefore \boxed{R = 30.627} \rightarrow (2)$$

$$\rightarrow Q_{\text{coil}} = \frac{\omega L}{R} = \frac{2\pi f \times L}{R}$$

$$\therefore Q_{\text{coil}} = \frac{2\pi \times 10^6 \times 50.66 \times 10^{-6}}{30.627} \rightarrow \text{substitution from eq (2) for } R$$

$$\therefore \boxed{Q_{\text{coil}} = 10.392}$$



② Applying KCL At node A, we get

$$\therefore \frac{V_A - 10}{2} + \frac{V_A}{2} + \frac{V_A - V_B}{5} + \frac{V_A - V_C}{5} = 0$$

$$\therefore V_A(1.4) + (-0.2)V_B + (-0.2)V_C = 5 \quad \rightarrow (1)$$

Applying KCL at node B, we get

$$\therefore \frac{V_B - V_A}{5} + \frac{V_B}{4} + \frac{V_B - V_C}{2} = 0$$

$$(-0.2)V_A + (0.95)V_B + (-0.5)V_C = 0 \quad \rightarrow (2)$$

Applying KCL at node C, we get

$$\frac{V_C - V_B}{2} + \frac{V_C}{4} + \frac{V_C - V_A}{5} + 2 = 0$$

$$V_A(-0.2) + (-0.5)V_B + (0.95)V_C = -2 \quad \rightarrow (3)$$

Solving eq's (1), (2) & (3) we get

$$V_A = 3.365 \text{ V}$$

$$V_B = -0.0376 \text{ V}$$

$$V_C = -1.416 \text{ V}$$

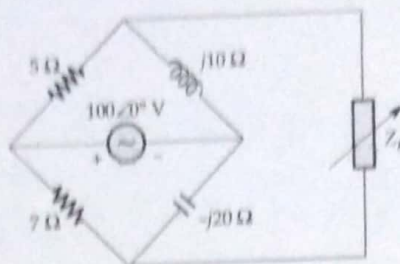
We can find out value of I

$$I = \frac{V_A - V_C}{5} = \frac{3.365 + 1.416}{5}$$

$$\therefore I = 0.9558 \text{ A}$$

$\therefore$  The value of current flowing in switch  
AC of the circuit shown is 0.9558 A

- Q.6 (b) Find the value of  $Z_L$  for maximum power transfer in the network shown and find maximum power.

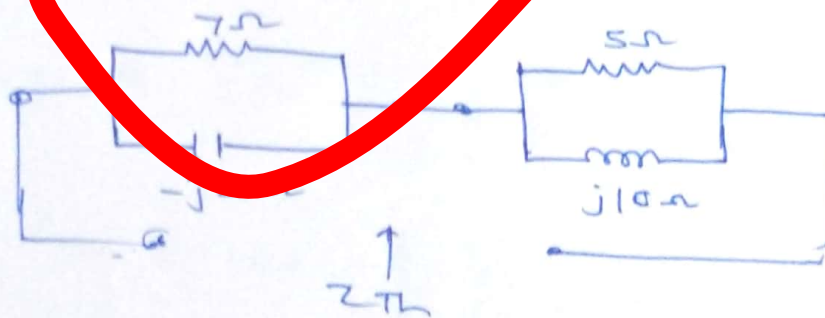


[20 marks]

→ for finding out the value of  $Z_L$  we will apply thevenin's theorem for above ckt.

→ According to thevenin's theorem we can replace a network by its equivalent  $Z_{th}$  &  $V_{th}$ . where  $Z_{th}$  is thevenin's resistance, can be found out by deactivating sources. &  $V_{th}$  can be found out by find voltage across load terminals.

① Let us find  $Z_{th}$



$$\therefore Z_{th} = \frac{7 \times (-j20)}{7 - j20} + \frac{5 \times j10}{5 + j10}$$

$$\therefore Z_{th} = \frac{(-140j)(7 + j20)}{49 + 400} + \frac{j50(5 - j10)}{25 + 100}$$



$$Z_{Th} = \frac{2800 - 980j}{449} + \frac{500 + j250}{125}$$

$$Z_{Th} = 10.236 - j0.1826 = 10.237 \angle -1.022^\circ$$

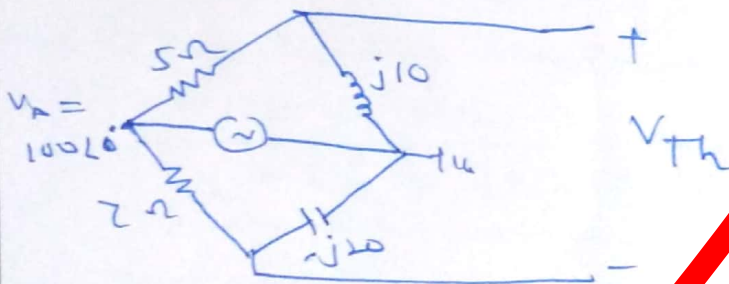
$$\therefore \boxed{Z_{Th} = 10.237 \angle -1.022^\circ \Omega}$$

$\therefore$  The value of  $Z_L$  for maximum power transfer in the network shown is

$$Z_L = Z_{Th}^* = 10.237 \angle +1.022^\circ \Omega$$

① Let us find maximum power

(i) Let us find  $V_{Th}$



$$V_{Th} = V_A \times \frac{j10}{5+j10} - V_A \times \frac{(-j20)}{7-j20}$$

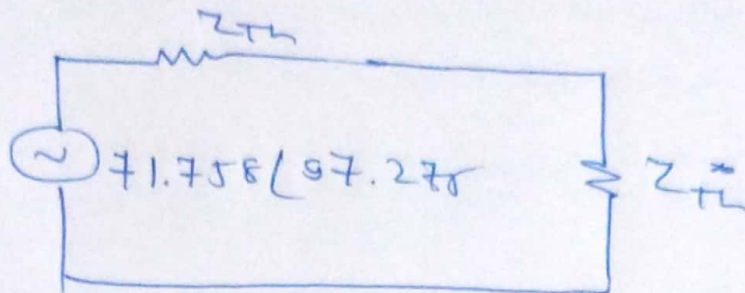
$$\therefore V_{Th} = 100\angle 0^\circ \left[ \frac{j10}{5+j10} + \frac{j20}{7-j20} \right]$$

$$\therefore \boxed{V_{Th} = 71.758 \angle 97.275^\circ \text{ V}}$$

$$\boxed{V_{Th} = -9.086 + j71.1804 \text{ V}}$$

→ let us draw thevenin ckt.

for maximum power transfer  $Z_L = Z_{th}^*$



$$\therefore P_{Lmax} = \frac{V^2}{4 R_{th}} = \frac{(71.758)^2}{4 \times 10.236}$$

$$\therefore P_{Lmax} = 125.7622 \text{ W}$$

→  $\therefore$  The  $Z_L$  for maximum power transfer is  $Z_L = Z_{th}^*$

$$Z_L = Z_{th}^* = 10.237 \angle 1.02^\circ$$

The maximum power is

$$P_{Lmax} = 125.7622 \text{ W}$$



Q.6 (c) Design and implement a BCD counter using J-K flip-flops.

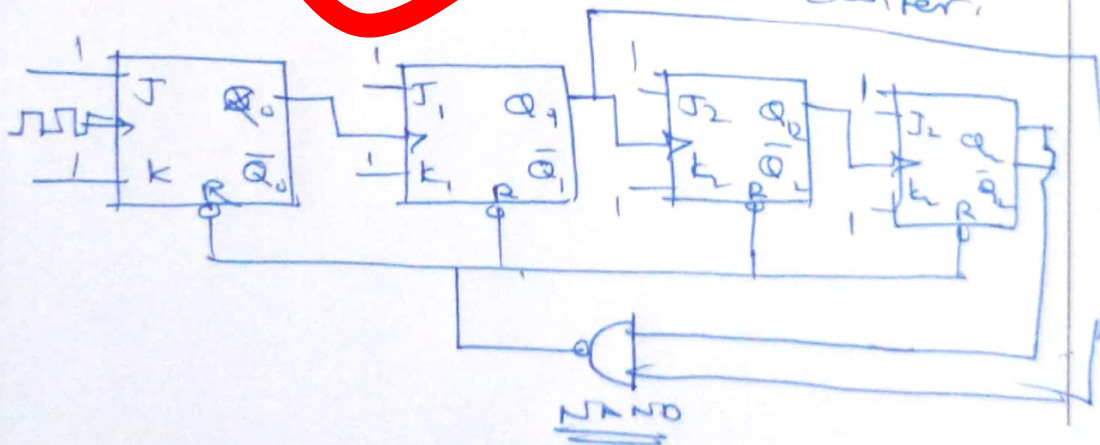
[20 marks]

→ Here it is not mentioned whether the counter is synchronous or asynchronous so we will design both counters

→ ① Asynchronous BCD counter using JK-FF.

<u>Input pulses</u>	$Q_3$	$Q_2$	$Q_1$	$Q_0$
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10	0	0	0	0 ← Reset

Design:  $J = K = 1$  Toggle mode - with working counter.



## ② Synchronous BCD counter using JK FF

Truth Table → 4 FF will be required  
mod 10 counter

Counter state Present state				Next state				Excitation Table of JK Flip Flop																				
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3^+$	$Q_2^+$	$Q_1^+$	$Q_0^+$																					
0	0	0	0	0	0	0	1	<table> <tr><th><math>Q</math></th><th><math>Q^+</math></th><th>J</th><th>K</th></tr> <tr><td>0</td><td>0</td><td>0</td><td>X</td></tr> <tr><td>0</td><td>1</td><td>1</td><td>X</td></tr> <tr><td>1</td><td>0</td><td>X</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>X</td><td>0</td></tr> </table>	$Q$	$Q^+$	J	K	0	0	0	X	0	1	1	X	1	0	X	1	1	1	X	0
$Q$	$Q^+$	J	K																									
0	0	0	X																									
0	1	1	X																									
1	0	X	1																									
1	1	X	0																									
0	0	0	1	0	0	1	0																					
0	0	1	0	0	0	1	1																					
0	0	1	1	0	1	0	0																					
0	1	0	0	0	1	0	1																					
0	1	0	1	0	1	1	0																					
0	1	1	0	0	1	1	1																					
0	1	1	1	1	0	0	0																					
1	0	0	0	1	0	0	1																					
1	0	0	1	0	0	0	0																					

$J_0$	$K_0$	$J_1$	$K_1$	$J_2$	$K_2$	$J_3$	$K_3$
1	X	0	X	0	X	0	X
X	1	1	X	0	X	0	X
1	X	X	0	0	X	0	X
X	1	X	1	1	X	0	X
1	X	0	X	X	0	0	X
X	1	1	X	X	0	0	X
1	X	X	0	X	0	0	X
X	1	X	1	X	1	1	X
1	X	0	X	0	X	X	0
X	1	0	X	0	X	X	1



Knap's

$Q_3 Q_2$   $J_0 = 1$

$Q_1$	1	1	1	1
$Q_0$	1	1	1	1
	1	1	1	1
	1	1	1	1

$Q_3 Q_2$   $K_0 = 1$

$Q_1$	1	1	1	1
$Q_0$	1	1	1	1
	1	1	1	1
	1	1	1	1

$Q_3 Q_2$   $J_1 = Q_0 Q_3$

$Q_1$	0	0	1	0
$Q_0$	1	1	1	0
	1	1	1	0
	1	1	1	0

$Q_3 Q_2$   $K_1 = Q_0$

$Q_1$	1	1	1	1
$Q_0$	1	1	1	1
	1	1	1	1
	1	1	1	1

$Q_3 Q_2$   $J_2 = Q_0 Q_1$

$Q_1$	0	1	1	0
$Q_0$	0	1	1	0
	1	1	1	0
	0	1	1	0

$Q_3 Q_2$   $K_2 = Q_0 Q_1$

$Q_1$	1	0	1	1
$Q_0$	1	0	1	1
	1	0	1	1
	1	0	1	1

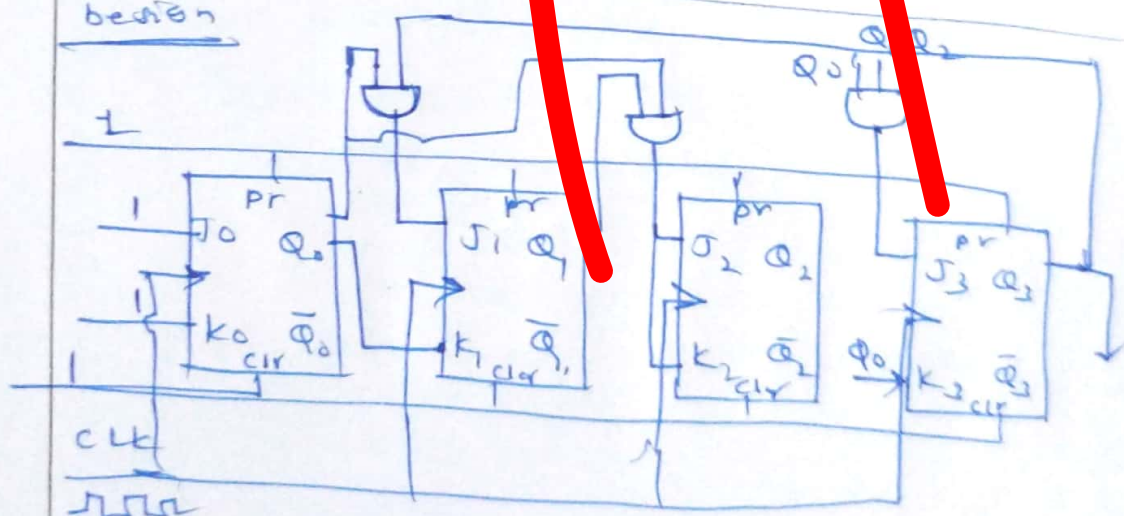
$Q_3 Q_2$   $J_3 = Q_0 Q_1 Q_2$

$Q_1$	0	0	1	1
$Q_0$	0	1	1	1
	0	1	1	1
	0	1	1	1

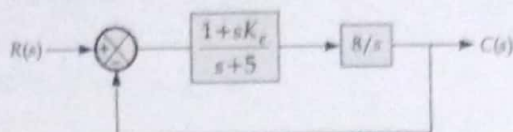
$Q_3 Q_2$   $K_3 = Q_0$

$Q_1$	1	1	1	1
$Q_0$	1	1	1	1
	1	1	1	1
	1	1	1	1

circuit



- Q.8 (a) Consider the block diagram shown below which employs proportional plus error rate control mechanism. Determine the value of error rate constant  $K_e$  so that the damping ratio of the system is 0.90.



What will be the value of settling time and maximum overshoot? If the input provided is unit ramp signal then calculate the value of steady error.

[20 marks]

→ Sol<sup>n</sup>: ① let us find value of  $K_e$ .

open loop t/f function =  $G(s)H(s)$

$$= \left( \frac{1 + sK_e}{s + 5} \right) \left( \frac{8}{s} \right)$$

characteristic equation =  $1 + G(s)H(s) = 0$

$$1 + \frac{8(1 + sK_e)}{s(s + 5)} = 0$$

$$\therefore s^2 + 5s + 8 + 8sK_e = 0$$

$$\therefore s^2 + (5 + 8K_e)s + 8 = 0$$

Comparing above eq<sup>n</sup> with  $s^2 + 2\zeta\omega_n s + \omega_n^2 = 0$   
we get

$$\omega_n^2 = 8, \quad 2\zeta\omega_n = 5 + 8K_e$$

$$\therefore \boxed{\omega_n = \sqrt{8} \text{ rad/s}} \quad 2 \times 0.9 \times \sqrt{8} = 5 + 8K_e$$

$$\rightarrow \text{As } \zeta = 0.9 \text{ (given)}$$

$$\therefore 2 \times 0.9 \times \sqrt{8} = 5 + 8K_e$$

$$5.0911 = 5 + 8K_e$$

$$\therefore \boxed{K_e = 0.0113}$$

$\therefore$  The value of error rate constant  $K_e$  is

$$\therefore \boxed{K_e = 0.0113}$$



② As we know that

$$\text{settling time of } 2\% \text{ error band} = \frac{4}{\xi \omega_n}$$

$$\therefore \text{settling time} = \frac{4}{0.9 \times \sqrt{8}} \rightarrow \text{substituting from eqn ①}$$

$$\therefore \boxed{\text{settling time} = 1.571 \text{ sec}}$$

→ Maximum overshoot

$$\begin{aligned} \therefore \text{Maximum overshoot} &= e^{-\frac{\pi \xi}{\sqrt{1-\xi^2}}} \\ &= e^{-\frac{\pi \times 0.9}{\sqrt{1-0.9^2}}} \\ &= 0.1523 \% \end{aligned}$$

$$\therefore \boxed{\text{Maximum overshoot} = 0.1523 \%}$$

③ If input signal is ramping i.e.

$$R(s) = \frac{1}{s^2} \Rightarrow \left( \frac{1}{s^2} = R(s) \right)$$

As we know that

$$e_{ss} = \lim_{s \rightarrow 0} \frac{R(s)}{(1+G(s))H(s)}$$

$$e_{ss} = \lim_{s \rightarrow 0} \frac{s \times \frac{1}{s^2}}{1 + \left( \frac{(1+s k_e)}{(s+5)} \right) \frac{8}{s}}$$

$$e_{ss} = \lim_{s \rightarrow 0} \frac{1}{s + \frac{8(1+s k_e)}{(s+5)}}$$

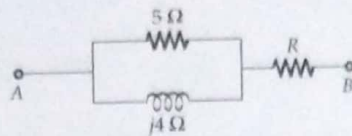
$$\boxed{e_{ss} = \frac{5}{8} = 0.625}$$

Thus the value of steady state error  
 $= 0.625$ .

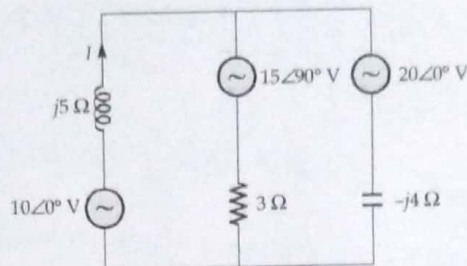
✓ 18



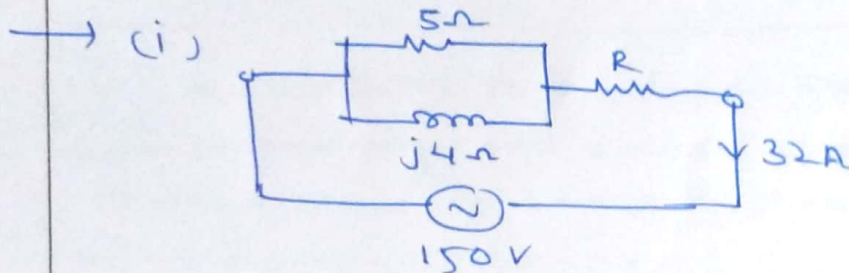
- Q.8 (b) (i) If a voltage of 150 V applied between terminals A and B produces a current of 32 A for the circuit shown below. Calculate the value of resistance R and power factor of the circuit.



- (ii) Find current I through  $j5\Omega$  branch using superposition theorem for the network shown below.



[10 + 10 = 20 marks]



$$\rightarrow Z_{AB} = \frac{5 \times j4}{5 - j4} + R$$

$$Z_{AB} = \frac{20j}{5 - j4} + R$$

$$Z_{AB} = \frac{20j(5 + j4)}{25 + 16} + R = \frac{80 + j100}{41} + R$$

$$Z_{AB} = \left( \frac{80}{41} + R \right) + j \left( \frac{100}{41} \right) \quad \text{--- (3)}$$

$$|Z_{AB}| = \sqrt{\left( \frac{80}{41} + R \right)^2 + \left( \frac{100}{41} \right)^2} \quad \text{--- (1)}$$

from given information

$$|Z_{AB}| = \frac{|V|}{|I|} = \frac{150}{32} \quad \text{--- (2)}$$

→ on comparing eq (4) we get

$$\left(\frac{150}{32}\right)^2 = \left(\frac{80}{41} + R\right)^2 + \left(\frac{100}{41}\right)^2$$

Solving above eq we get  $R = 2.051 \Omega$

∴ The value of resistance  $R = 2.051 \Omega$

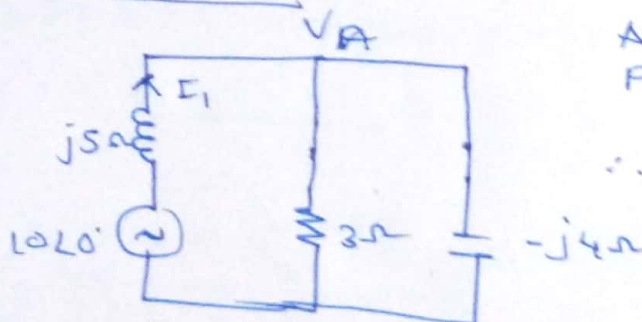
$$\rightarrow \text{P.F.} = \cos\left(\tan^{-1} \frac{\left(\frac{80}{41} + 2.051\right)}{\left(\frac{100}{41}\right)}\right)$$

$$\therefore \text{PF} = \cos(58.625) = 0.5203 \text{ lag.}$$

∴ The power factor of circuit is 0.5203 lag

(ii) According to Superposition theorem ~~we~~ Activate only one source at a time & replace other v/s source by short ckt & current source by open ckt & find response due to it. And at last add all the responses to get resultant output.

① case (i) :-



Apply KCL at point A

$$\therefore \frac{V_A - 10 \angle 0^\circ}{j5} + \frac{V_A}{3} + \frac{V_A}{-j4} = 0$$

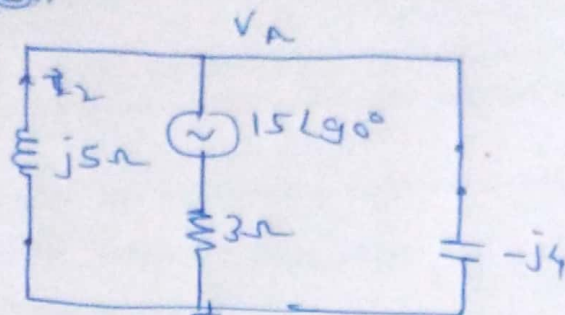
$$\therefore V_A = \left(\frac{10}{j5}\right) / \left(\frac{1}{j5} + \frac{1}{3} + \frac{1}{-j4}\right) = 5.933 \angle -98.53^\circ \text{ V}$$

$$\therefore I_1 = \frac{10 \angle 0^\circ - 5.933 \angle -98.53^\circ}{j5} = 2.472 \angle -61.66^\circ$$

$$\therefore \boxed{I_1 = 2.472 \angle -61.66^\circ \text{ A}} \rightarrow \text{①}$$



Case ②,



Applying KCL at point A we get

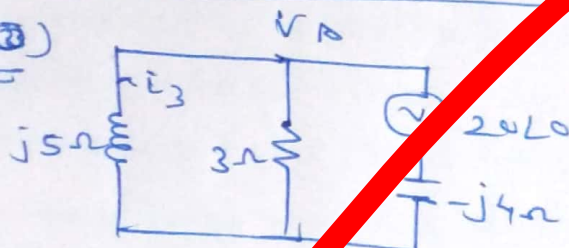
$$\frac{V_A}{j5} + \frac{V_A - 15\angle 90^\circ}{3} + \frac{V_A}{-j4} = 0$$

$$\therefore V_A = \left( \frac{15\angle 90^\circ}{3} \right) / \left( \frac{1}{j5} + \frac{1}{3} + \frac{1}{-j4} \right)$$

$$\therefore V_A = 14.834 \angle 81.469^\circ \text{ V}$$

$$\therefore I_2 = \frac{0 - V_A}{j5} = 2.966 \angle 171.469^\circ \text{ A} \quad \text{--- ①}$$

Case ③)



Applying KCL at point A we get

$$\frac{V_A}{j5} + \frac{V_A}{3} + \frac{V_A - 20\angle 0}{-j4} = 0$$

$$\therefore V_A = \left( \frac{20\angle 0}{-j4} \right) / \left( \frac{1}{j5} + \frac{1}{3} + \frac{1}{-j4} \right)$$

$$\therefore V_A = 14.834 \angle 81.469^\circ \text{ V}$$

$$I_3 = \frac{0 - V_A}{j5} = 2.966 \angle 171.469^\circ \text{ A} \quad \text{--- ②}$$

Adding eqn ①, ②, ③ we get

$$I = I_1 + I_2 + I_3 = 4.869 \angle -164.572^\circ \text{ A}$$

- Q.8 (c) Write an 8085 assembly language program to check whether the 8-bit number at location, D200H is palindrome or not, write comments for each instruction of program? [20 marks]

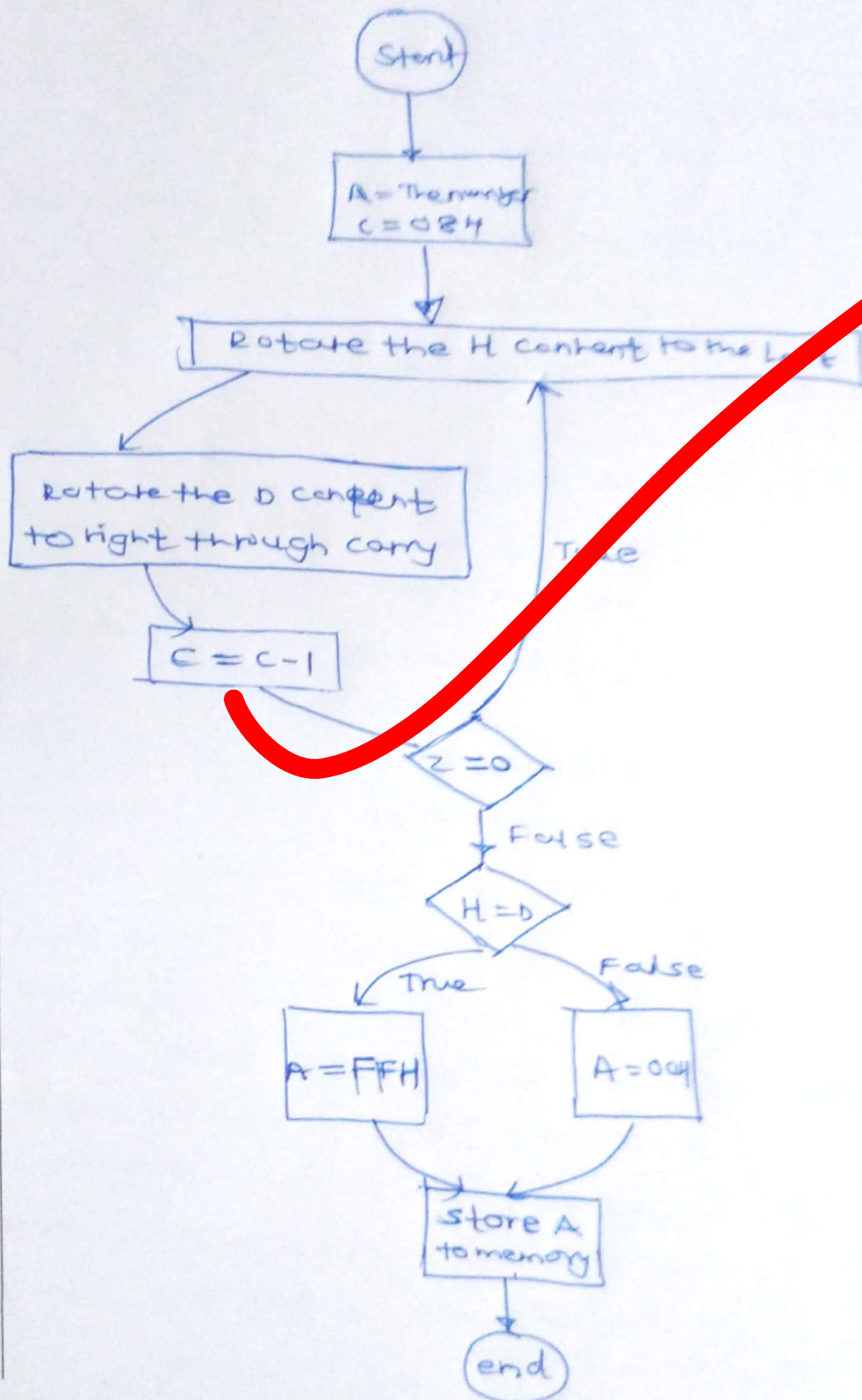
→ In this program, we are taking the number from location D200H. The program will return 00H if the number is not palindrome otherwise it will return FFH.

→ Let the input is 18H so the binary value is (0001, 1000) this is a palindrome. The number 52H (0101 0010) it is not a palindrome.

→ In this problem, we are taking the first number into Accumulator, then shifting it to the left; when it is left shifted the MSB will be placed at MSB and also in the carry flag. This carry flag is inserted into the D register by right shifting. Thus the bit pattern will be reversed now by comparing the value of actual number & the reversed number we can determine it is palindrome or not.



Flow diagram



Program:-

LDA D200H      Load the number  
into A

MOV H, A      Move content of Accumulator  
to Register H

~~MOV~~ MVI C, 08H      Initialize Counter

Loop MOV A, H      Load H to Acc

RLC      Rotate left without  
carry

MOV H, A      Get back Acc to H

MOV A, D      Load D content to  
accumulator

RRC      Rotate Right through  
carry

MOV D, A      Get back Acc to D

DCR      Decrement C

JNZ Loop      Jump to Loop if  $C \neq 0$

MOV A, H      Load H data to A

CMP D      Compare A with Accumulator

JZ TRUE      If both are same it is parindrom

MVI A, 00H      Load 00H into A

JMP Exit      Jump to Exit

TRUE MVI A, FFH      Load FFH into A  
0000

EXIT STA 8050H      Store the result at  
memory location 8050H

HLLT      Terminate the program