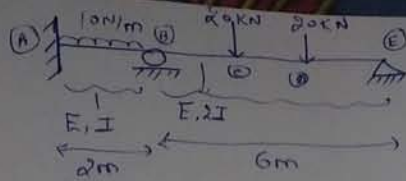


Ans (a)



(Using slope deflection) 12:07

$$\textcircled{1} M_{FAB} = -3.33 \text{ kNm}$$

$$M_{FBA} = +3.33 \text{ kNm}$$

$$\textcircled{2} M_{FDE} = -26.66 \text{ kNm}$$

$$M_{FED} = +26.66 \text{ kNm}$$

$$* M_{AB} = M_{FAB} + \frac{2EI}{l} [\theta_B]$$

$$\sim M_{AB} = -3.33 + EI \theta_B \text{ --- eqn (1)}$$

$$\sim M_{BA} = +3.33 + 2EI \theta_B \text{ --- eqn (2)}$$

$$\sim M_{BE} = -26.66 + \frac{2}{3} EI [2\theta_B + \theta_E] \text{ --- eqn (3)}$$

$$\sim M_{EB} = 26.66 + \frac{2}{3} EI [2\theta_E + \theta_B] \text{ --- eqn (4)}$$

and  $M_{BA} + M_{BE} = 0$  and  $M_{EB} = 0 \Rightarrow -40 \left[ \frac{2\theta_B + \theta_E}{3} \right] EI \text{ --- eqn (5)}$

$$\downarrow$$

$$23.333 = EI [3.33 \theta_B + 0.66 \theta_E] \text{ --- eqn (6)}$$

$$\frac{-40}{EI} - 2\theta_E = \theta_B$$

from eqn (5) and eqn (6)

$$23.333 = 3.333 \left[ \frac{-40}{EI} - 2\theta_E \right] EI + 0.66 \theta_E$$

$$\frac{156.666}{EI} = - \dots EI$$

$$\theta_E = -26.111 / EI$$

$$\theta_B = 12.222 / EI$$

So  $M_{AB} = 8.888 \text{ kNm}$

$M_B = 27.777 \text{ kNm}$

$M_{BE} = -27.777$

$M_{EB} = 0$

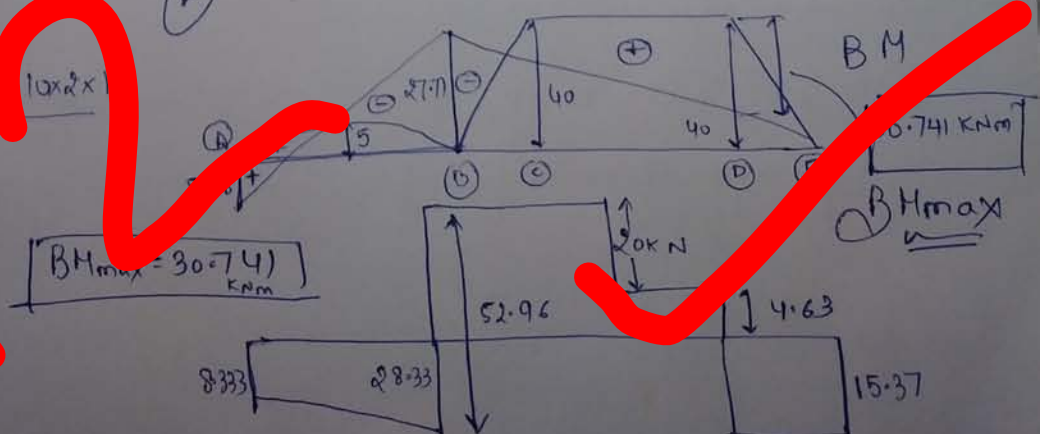


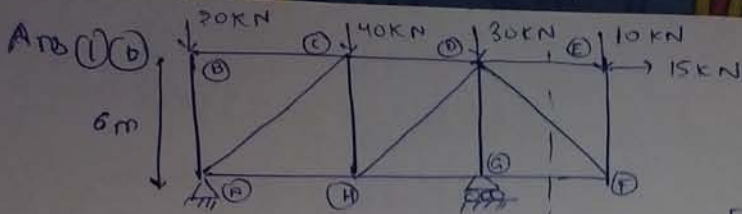
$$R_A = \frac{8.888 + 27.777}{2} + 10 \times 2 \times \dots$$

$R_A = 8.333 (\downarrow)$

$R_E = 15.37 \text{ kN}$

$R_B = 52.96 \text{ kN}$



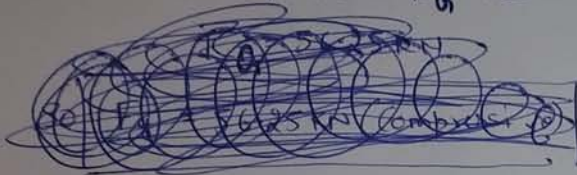


For cut in (5) cutting the sec and conserving force at

# for force in (4)

$$\sum H_A = 0$$

$$40 \times 6 + 30 \times 0 + 10 \times 16.5 + 15 \times 6 = R_B \times 12$$



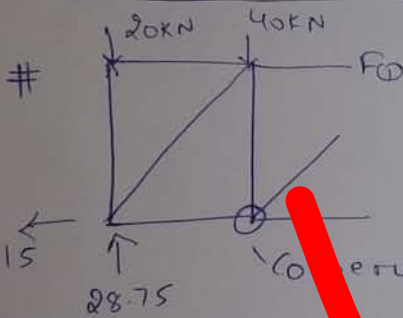
$$F_{(5)} \times 6 = 10 \times 4.5$$

$$F_{(5)} = 7.5 \text{ kN (compressive)}$$

$$R_B = 71.25$$

$$F_{(4)} = 71.25 \text{ (Comp)}$$

$$* F_3 = F_5 = 7.5 \text{ kN (Compressive)}$$



so

$$F_{(1)} \times 6 = 40 \times 0 + 20 \times 6 - 28.75 \times 6$$

$$F_{(1)} = 8.75 \text{ kN compressive}$$

$$F_2 \cos 45^\circ = (8.75 + 7.5) \times 6$$

$$F_2 = 16.25 \sqrt{2} + 15 \sqrt{2}$$

$$F_2 = 31.25 \sqrt{2} \text{ kN}$$

Area (c)  $m_{mass} = 10 \text{ kg}$

$K = 100 \text{ N/m}$  - damply coef =  $5 \text{ Ns/m}$

$$\omega_n = \sqrt{\frac{100}{10}} = \sqrt{10}$$

and [damply factor =  $c/c_{cr} = \frac{5}{20\sqrt{10}} = \frac{1}{4\sqrt{10}}$ ]

$$c_{cr} = 2 \times 10 \times \sqrt{10} = 20\sqrt{10}$$

$$(b) \omega_d = \omega_n \sqrt{1 - (\frac{1}{4\sqrt{10}})^2} = 3.152 \text{ rad/sec} \Rightarrow t_0 = \frac{3.152}{\omega_d} = 0.501$$

$$(c) \text{ logarithmic decrement } \left[ \frac{\ln x_i}{\ln x_{i+1}} \right] = \frac{2\pi \times 0.079}{\sqrt{1 - 0.079^2}} = 0.499$$

$$(d) e^{0.499} = 1.647$$

Ans ① ②  $\bar{P} = \frac{112+178+95+139+101}{5} = 125$

$\bar{P}^2 = \frac{112^2+178^2+95^2+139^2+101^2}{5} = 16555$

$\sigma = \sqrt{\frac{\sum (P_i - \bar{P})^2}{n-1}} = \sqrt{\frac{5 [16555 - 125^2]}{4}}$

$\sigma = 34.095 \text{ cm}$   
 $C_v = \frac{\sigma}{\bar{P}} \times 100 = \frac{34.095}{125} \times 100 = 27.276\%$

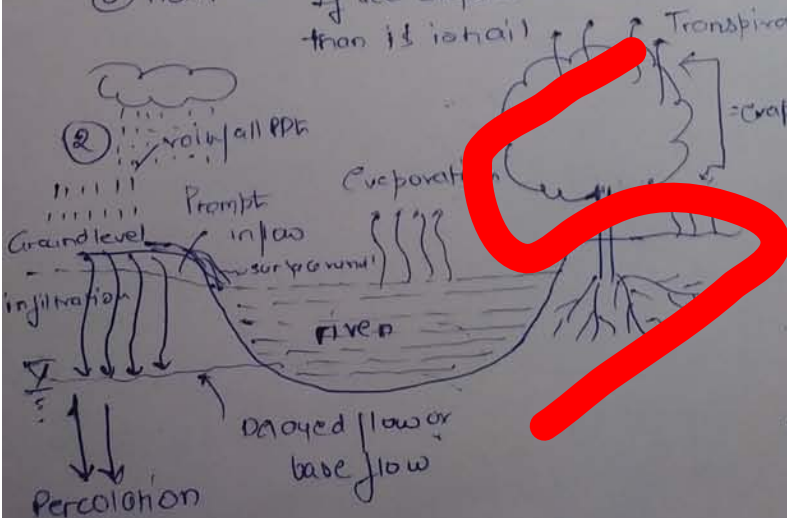
opt No.  $\log_{10} \frac{C_v}{E} = \left( \frac{C_v}{E} \right)^2 = \left( \frac{27.276}{8} \right)^2 = 11.625 = 12$

So 12 stations required. So 7 more stns are required

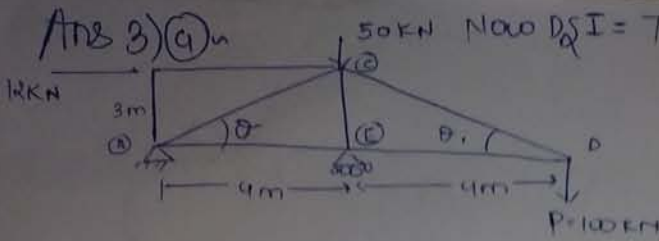
Recording type =  $\frac{10}{100} \times 12 = 1.2$  So no of recording type and 10 no of non-recording type.

Ans ③ ① Precipitation is Precipitation is any form of liquid or solid water particle to fall from the atmosphere and reach the surface of the earth. Various type of precipitation are.

- ① Rainfall is when precipitation comes in the form of water droplets varying from 0.5mm to 5mm when rainfall > 5mm considered as rain fall.
- ② Snow is when water droplets freeze and fall with snow flakes having density less than 0.19 gm/cc
- ③ drizzle is light rain fall with intensity less than 1mm/hr.
- ④ Glaze is when rain comes into contact with freezing ground, ice coating is formed.
- ⑤ sleet is If ice frozen droplet. If falling rain converts into ice crystal of freezing temperature considered as sleet.
- ⑥ Hail is If ice crystal converts into a lump of size more than 8mm than is hail.



\* The cloud when condensed precipitates in form of rain which then converted into infiltration and surface runoff. No evaporation and transpiration happens on surface of river and banks. Evaporated water forms clouds again. This cycle repeat itself continuously as shown in diagram.



50kN Now D.S.I = 7+3-2x5=0 so determinate  
 \* Now let us find forces in the members.

\*  $F_{CD} \sin \theta = 100\text{kN}$  - eqn 1  
 and  $F_{CD} \cos \theta = F_{ED}$  - eqn 2

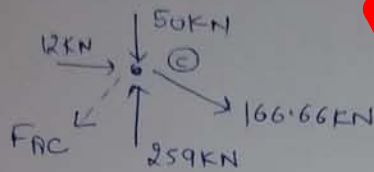
So  $F_{CD} = 166.67$  (tensile)  
 $F_{ED} = 133.33$  (compressive)

and now considering moment from at  
 (A) we get  $F_E = \frac{100 \times 8 + 50 \times 4 + 12 \times 3}{4}$

So  $F_E = 259\text{kN}$

So  $F_{CE} = 259\text{kN}$  (compressive)  
 $F_{BC} = 12\text{kN}$  (compressive)  
 $F_{BA} = +50\text{kN}$  (compressive)

and  $F_{AC} =$



so considering force in x and y direction

$F_{AC} \times \frac{3}{5} = 259 - 50 - 166.67 \times \frac{3}{5}$

$F_{AC} = 94.583$  (tension) +  $86.8103$

So  $F_{AC} = 181.66\text{kN}$  (tension) - eqn 3

So now forces in all member are known.

Then K should be fixed as 1kN downward.

So for K=1 downward at D forces in members are

$F_{BC} = 0, F_{BA} = 0.$

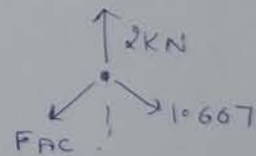
$F_{CE} = 2\text{kN}$  (compressive)

$F_{CD} = 1.667$  (tensile)

$F_{ED} = 1.334$  (compressive)

$F_{AE} = 1.334$  (compressive)

$F_{AC} =$



So  $F_{AC} \times \frac{3}{5} + 1.667 \times \frac{3}{5} = 2$

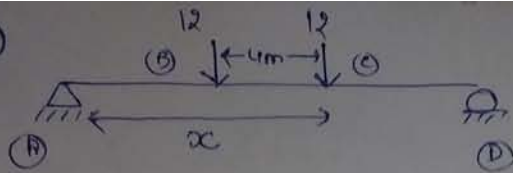
$F_{AC} = 1.6667$  (tensile)

Member	Force	K	$\frac{KPL}{AE}$
AB	-50	0	0
BC	-12	0	0
CD	+166.67	+1.667	$4.516 \times 10^{-3}$
DE	-133.33	-1.334	$2.3124 \times 10^{-3}$
EA	-133.33	-1.334	$2.3124 \times 10^{-3}$
EC	-259	-2	$5.053 \times 10^{-3}$
AC	+181.66	+1.667	$4.924 \times 10^{-3}$

So  $\sum \text{total} = 19.1178 \times 10^{-3}$  (downward)

20

Ans (3) (b) (1)



Now moment

$$R_A \times 15 = 12(15-x) + 12[19-x]$$

$$R_A = \frac{408 - 24x}{15}$$

$$M = \left( \frac{408 - 24x}{15} \right) x - 12(4)$$

$$\text{So } M = \frac{-24x^2 + 408x - 720}{15} \quad \text{--- eqn (1)}$$

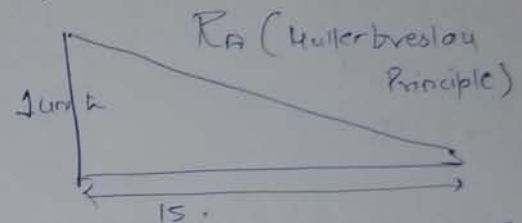
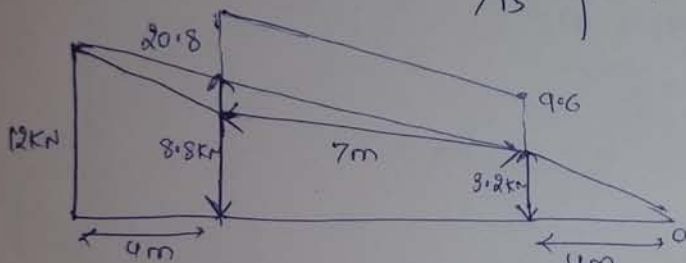
$$\text{Now } \frac{\partial M}{\partial x} = 0 \quad \text{So } -48x + 408 = 0$$

$$\boxed{x = 8.5 \text{ m}}$$

(b) Influence line for support reaction at A

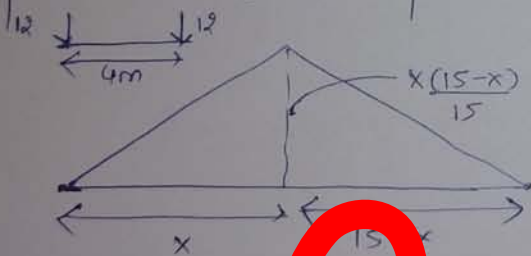
$$R_A \times 15 = 12x + 12(x+4)$$

$$R_A = \frac{24x + 48}{15} \quad (\text{for } x=0 \text{ to } x=11)$$



$$\boxed{\text{Maximum value} = 20.8 \text{ kN}}$$

(c) from Muller Breslau principle



$$\frac{m}{x} + \frac{m}{15-x} = 1$$

$$\frac{m(15-x) + m \cdot x}{x(15-x)} = 1$$

$$\text{So } m(15) = x(15-x)$$

$$\text{So } \boxed{m = \frac{x(15-x)}{15}}$$

\* Maximum BM at (c)

$$M = \frac{-24x^2 + 408x - 720}{15} \quad (\text{from eqn (1)})$$

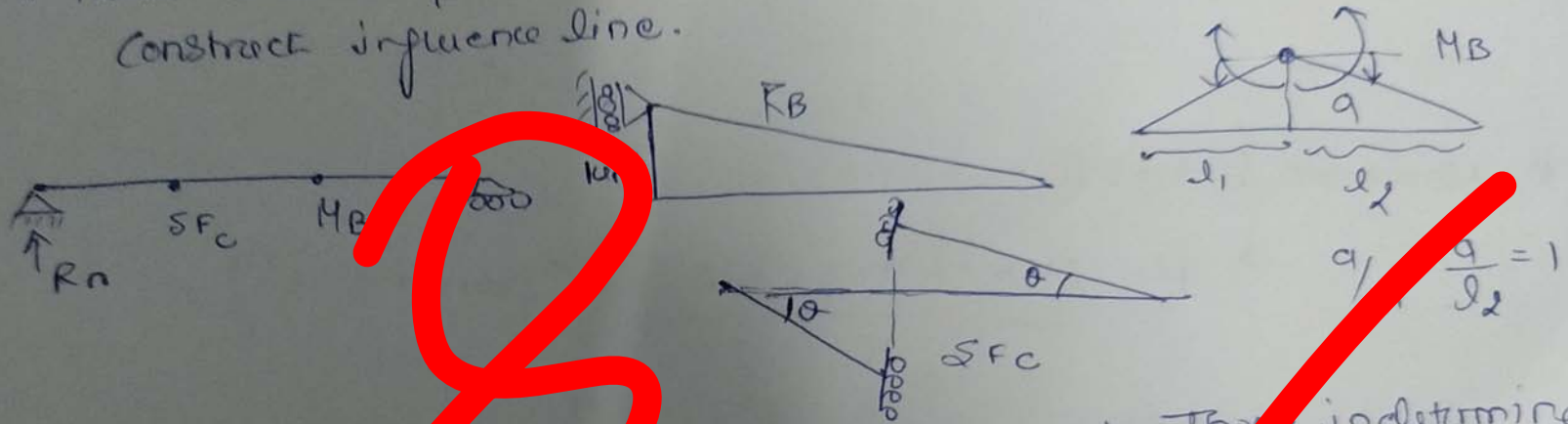
at 8.5m

$$M = \frac{-24(8.5)^2 + 408(8.5) - 720}{15}$$

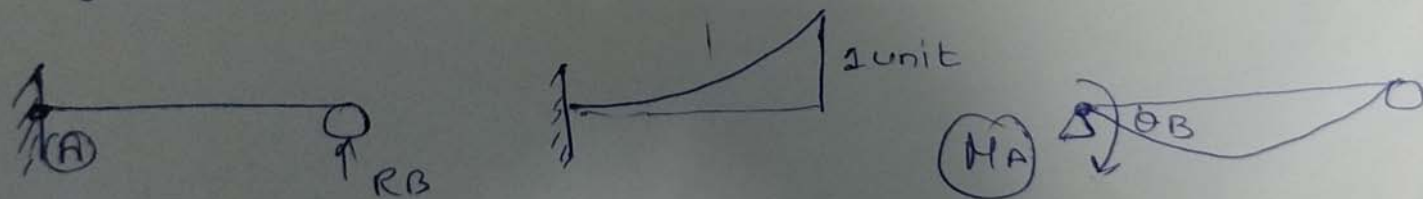
$$\boxed{M = 67.6 \text{ kNm}}$$

Ans (3)(b)(ii)

- \* Muller breslau principle: If an internal stress component or a reaction component is considered to act through some small distance and there be to deflect or displace a structure, the curve of the deflected or displaced structure will be, to some scale, the influence line for the stress or rx component.
- \* Muller-breslau principle uses Betti's law of virtual work to construct influence line.



- \* Muller-breslau principle is applicable to only those indeterminate structure which are elastic and follow Hooke's law. All other indeterminate structure cannot be solved by this principle.



Ans (3) (c)

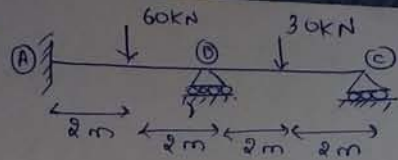
Time hrs	0	2	4	6	8	12	16	30
(m <sup>3</sup> /p)	0	2.044	8.1	13.5	11.34	6.75	2.7	0.0

So first unit hydrograph corresponding to 4hrs should be known  
So 1cm rainfall given and we have to find for 1cm So dividing  
of 10cm.

* Time	Hydrograph (10cm) (m <sup>3</sup> /p)	Unit Hyd. (m <sup>3</sup> /p)	(1) For (4hrs 5cm) (m <sup>3</sup> /p)	(2) For (4hrs 7.5cm) (m <sup>3</sup> /p)	Σ (1) + Σ (2)
0	0	0	0	0	0
2	2.044	0.2044	0.2044 × 5		1.022
4	8.1	0.81	0.81 × 5	0	4.05
6	13.5	1.35	1.35 × 5	0.44 × 7.5	8.283
8	11.34	1.134	1.134 × 5	0.81 × 7.5	11.745
10	9.045	0.9045	0.9045 × 5	1.35 × 7.5	14.6475
12	6.75	0.675	0.675 × 5	1.134 × 7.5	11.88
14	4.725	0.4725	0.4725 × 5	0.9045 × 7.5	9.1125
16	2.7	0.27	0.27 × 5	0.675 × 7.5	5.4125
18	1.35	0.135	0.135 × 5	0.4725 × 7.5	4.21875
20	0	0	0	0.27 × 7.5	2.025
				0.135 × 7.5	1.0125
				0	0

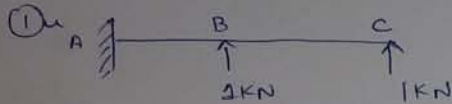
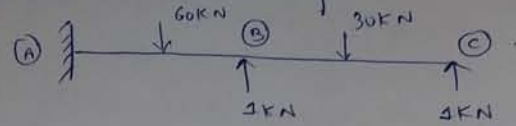
So Maximum  $Q = 14.6475 \text{ m}^3/\text{p}$  at  $t_w = 10 \text{ hrs}$

Ans (4) (a)



$\Delta_B = 12 \text{ mm (downward)}$   
 $\Delta_C = 6 \text{ mm (downward)}$

So first creating flexibility matrix assuming



then flexibility matrix can be

$\Delta_{BB} = \frac{(4)^3}{3EI}$

$\Delta_{CB} = \frac{(4)^3}{3EI} + \frac{(4)^2}{2EI} \times 4$

and  $\Delta_{CC} = \frac{(8)^3}{3EI}$

and now  $EI = 20 \times 10^{12} \text{ N-mm}^2$  or  $20 \times 10^6 \text{ N-m}^2$

so  $\Delta_{BB} = 1.0666 \times 10^{-6}$

$\Delta_{BC} = \Delta_{CB} = 2.6666 \times 10^{-6}$

$\Delta_{CC} = 8.5333 \times 10^{-6}$

$[f] = \begin{bmatrix} 1.0666 \times 10^{-6} & 2.6666 \times 10^{-6} \\ 2.6666 \times 10^{-6} & 8.5333 \times 10^{-6} \end{bmatrix}$

and now we have to find  $[f]^{-1}$

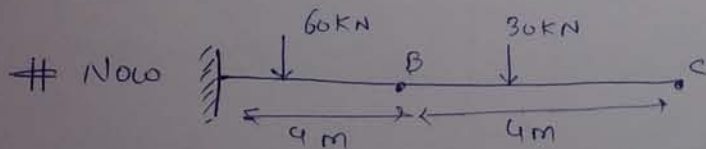
$|f| = 1.999 \times 10^{-12}$

so  $[f]^{-1} = \frac{1}{1.999 \times 10^{-12}} \begin{bmatrix} 1.0666 \times 10^{-6} & -2.6666 \times 10^{-6} \\ -2.6666 \times 10^{-6} & 8.5333 \times 10^{-6} \end{bmatrix}$

↙ interchange ↘

so  $[f]^{-1} = 502234.94 \begin{bmatrix} 1.0666 & -2.6666 \\ -2.6666 & 8.5333 \end{bmatrix} = 502234.94 \begin{bmatrix} 8.5333 & -2.6666 \\ 2.6666 & 1.0666 \end{bmatrix}$

↙ interchange ↘

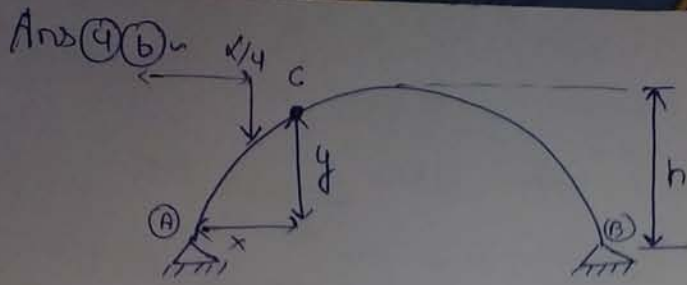


$\Delta_B = \frac{60 \times 10^3 \times (2)^3}{3EI} + \frac{60 \times 10^3 \times 2^2 \times 2}{2EI} + \frac{30 \times 10^3 \times (4)^3}{3EI} + \frac{60(4)^2 \times 10^3}{2EI}$

$\Delta_C = \frac{60 \times 10^3 \times 2^3}{3EI} + \frac{60 \times 10^3 \times 2^2 \times 6}{2EI} + \frac{30 \times 10^3 \times 6^3}{3EI} + \frac{30 \times 10^3 \times 6^2 \times 2}{2EI}$







\* Now reaction at (A) is given by  $\sum M_B = 0$

$$R_A \cdot l = P \cdot l/4$$

$$\text{So } \boxed{R_A = 3P/4}$$

Now conserving momentum at C

$$3P/4 (x) - P(x - l/4) = H(y)$$

$$\text{So } H(y) = -Px/4 + Pl/4 \text{ so } \frac{P(l-x)}{4}$$

$$\text{and } y = \frac{4hx(l-x)}{l^2} \text{ so } \boxed{H = \frac{Px^2}{16hx}}$$

\* So maximum moment in arch is given by  $H_{max}$  and  $\frac{dH}{da} = 0$

So  $H = \frac{P}{4} (a) - \frac{Px^2}{16hx} (y)$

$$= \frac{P}{4} (a) - \frac{Px^2}{16hx} \left[ \frac{4ha(h-a)}{l^2} \right]$$

$$H = \frac{3P(a)}{4} - \frac{Px^2}{16hx} y$$

$$\text{So } H = \frac{3Pa}{4} - \frac{Pah}{4x} + \frac{Pa^2}{4x}$$

$$H = \frac{P}{4} \left[ 1 - \frac{(h-a)}{x} \right] = \frac{Pa}{4} - \frac{Pah}{4x} + \frac{Pa^2}{4x}$$

$$\text{So } \frac{dH}{da} = 0 \text{ so } \frac{3P}{4} - \frac{Ph}{4x} + \frac{2Pa}{4x} = 0$$

$$\frac{dH}{da} = 0 \text{ so } \frac{3P}{4} - \frac{Ph}{4x} + \frac{2Pa}{4x} = 0$$

$$\boxed{\frac{(l-3x)}{2} = a}$$

\* Now putting in H

$$H = \frac{P}{4} \frac{a}{x} [3x - l + a]$$

$$H = \frac{Pa}{4x} \left[ \frac{3x-l}{2} \right]$$

$$H = \frac{P}{4x} [3x - l + a]$$

$$\text{So } \frac{dH}{dx} = 0 \text{ then}$$

$$\boxed{l/3 = x}$$

\* Now putting in H

$$H = \frac{P}{4} \frac{a}{4x} - \frac{Pa}{4x} \frac{l}{4x} + \frac{Pa^2}{4x}$$

$$H = \frac{Pa}{4x} [x - l + a]$$

$$H = \frac{P}{4x} \left( \frac{l-x}{2} \right) \left[ \frac{3x-l}{2} \right]$$

$$H = -\frac{P}{16x} (l-x)$$

$$\text{So } \frac{dH}{dx} = 0 \text{ then } \boxed{x = l/3}$$

Ans (4)(a) Area of lake = 5000 hectare

$$\text{So } Q_{\text{inflow}} = 6 \text{ m}^3/\text{sec} = \frac{6 \times 3600 \times 24 \times 30}{5000 \times 10^4}$$

$$= 311.04 \text{ mm}$$

$$Q_{\text{outflow}} = 336.96 \text{ mm}$$

Acc to water budget eqn

$$Q_{\text{inflow}} - Q_{\text{outflow}} = \pm \Delta \text{Storage}$$

$$\rightarrow [145 + 311.04] - [336.96 + 1] = \Delta \text{Storage}$$

$$5.08 \text{ mm} = \Delta \text{Storage (↑)}$$

$$\text{So final surface elev} = 103.2 \text{ m} + 0.05808 = 103.25808 \text{ m}$$

Ans (4)(b)



Given  $v = (0.5 \ln d + 0.03) \text{ m/sec}$

$$\text{So } w_1 = \frac{[1 + \frac{2}{2}]^2}{2 \times 1} = 2 \text{ m}$$

Distance from left	Depth	$d \ln d$	Width	$w_1 \left[ \frac{2}{2} + \frac{2}{2} \right] = 2 \text{ m}$
0	0	0	0	0
1	1.1	-2289	2	0.5088
3	2.0	-3258	2	1.3032
5	2.5	-4108	2	0.054
7	2.0	-336	2	1.44
9	1.7	-2595	2	0.8823
11	1	-183	2	0.366
12	0	0	0	0

$$\Sigma \phi = 6.45308 \text{ m}^2$$

Ans (5) (a) Bulk modulus is the property of fluid which resist the compression on the fluid's body. Bulk modulus is given by

$$K = -\frac{\partial P}{\left(\frac{\partial V}{V}\right)}$$

So unit of bulk modulus =  $N/m^2$

Factors affecting bulk modulus of elasticity

- (1) Temperature
- (2) Entrained air content
- (3) Pressure applied.

\* Liquid generally have high bulk modulus of elasticity. They resist compression. So when force or pressure is applied on fluid, i.e. (liquid) then

$$K = -\frac{\partial P}{\left(\frac{\partial V}{V}\right)}$$

so for  $K$  value very high  $\left(\frac{\partial V}{V}\right)_{\text{lim}} \rightarrow 0$  w so  $\partial V$  is very small hence considered incompressible

Ans (5) (b)  $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$  } continuity eqn

$$(u = 3x + y), (v = 2x - 3y)$$

$$3 - 3 = 0$$

so it satisfy continuity eqn so flows possible.

$$\left[ \frac{\partial \phi}{\partial x} = u \text{ and } \frac{\partial \phi}{\partial y} = v \right] \text{ for potential funcn}$$

(1)  $d\phi = u dx \Rightarrow d\phi = (3x + y) dx$

so  $\phi = 3x^2/2 + xy + f(y)$  - eqn (1)

(2)  $d\phi = v dy \Rightarrow d\phi = (2x - 3y) dy$

so  $\phi = 2xy - 3y^2/2 + f(x)$

so velocity potential funcn do not exist for rotational flow

(3)  $\omega_z = \frac{1}{2} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) = \frac{1}{2} [2 - 1] = \frac{1}{2}$  so rotational

\* Stream function on other hand can be written by

$$\frac{\partial \psi}{\partial y} = 0 \quad \text{on} \quad \frac{\partial \psi}{\partial x} = -v$$

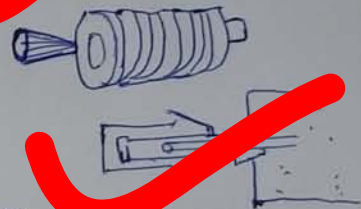
$$\psi = 3xy + \frac{y^2}{2} + f(x) \quad \psi = 3xy - x^2 + f(y)$$

$$\text{So } \boxed{\psi = \frac{y^2}{2} + 3xy - x^2}$$

Ans (3) (c) Freyssinet system introduced by french engineer Freyssinet and it was the 1st method to be introduced.

(2) High strength steel wire of 5mm or 7mm, numbering (16, 24) are grouped into a cable with a helical spring inside. spacing of wires cable is inserted in the duct.

(3) Anchorage device consists of a concrete cylinder with conical socket and conical plug carrying grooves on its surface. Steel wires are carried along these grooves at the ends. Concrete cylinder is heavily reinforced.



(4) Wires are pulled by Freyssinet double acting jacks which can pass through suitable grooves of the wires in table at a time.

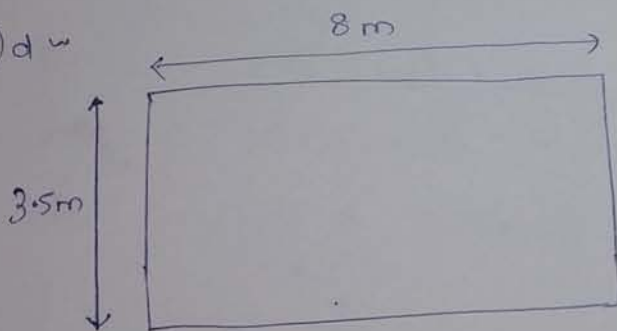


Freyssinet system

So it will be one way slab and depth can be given

$$d = \frac{3500}{35 \times 0.8} = 125 \text{ mm}$$

Ans (5) d =



So assuming clear cover of 20mm and 12mm  $\phi$

$$\text{So effective width} = 125 + 3500 = 3625 \text{ mm}$$

$$* \text{ Now } D = 125 + 20 + 6 = 151 \text{ mm}$$

$$\text{Now total } \omega = 5 \text{ kN/m}^2 \quad \text{and } P_L = 25 \times 151 \times \frac{1}{1000} = 3.775$$

$$\omega_{\text{total}} = 1.5(5 + 3.775) = 13.1625$$

$$M_{\text{max}} = \frac{13.1625 \times 3.5^2}{8} = 20.155 \text{ kN/m}$$

$$\text{So } M_{ue2} = 0.138 \times 25 \times 1000 \times d^2$$

$$\text{or } 20.155 \times 10^6 = 0.138 \times 25 \times 1000 \times d^2$$

$$d = 76.433 \text{ mm}$$

Take  $d = 85 \text{ mm}$  then  $D = 110 \text{ mm}$

$$\# \text{ Now } A_{st} = \frac{0.5 \times 20 \times 1000 \times 85}{415} \left[ 1 - \sqrt{1 - \frac{4.6 \times 20.155 \times 10^6}{25 \times 1000 \times 85^2}} \right]$$

$$A_{st} = 619.279 \text{ mm}^2$$

$$\text{Minimum } A_{st} = \frac{0.12 \times 1000 \times 85}{100} = 102 \text{ mm}^2$$

\* Now providing  $12 \text{ mm } \phi$

$$\text{Spacing} = \frac{1000 \times \pi/4 \times 12^2}{619.279} = 182.627$$

So Provide

$12 \text{ mm } \phi @ 180 \text{ mm c-c}$

# Distribution bars in longer direction

$$\text{Spacing} = \frac{1000 \times \pi/4 \times 10^2}{770} = 770 \text{ mm}$$

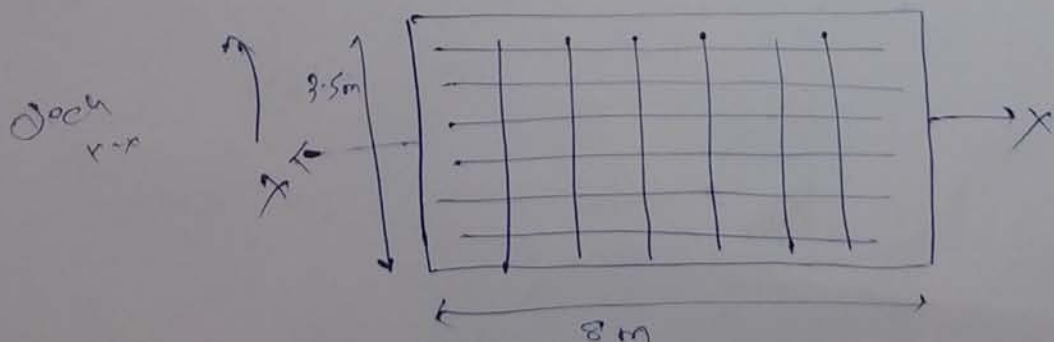
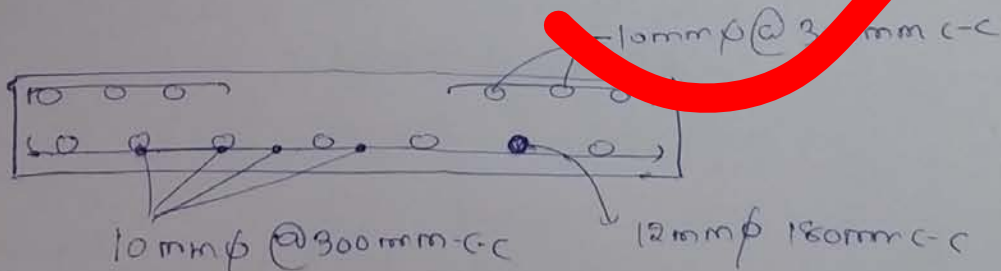
$$\text{Minimum} = 3d \text{ or } 3d = 255$$

$$\text{for Distribution} = 5d \text{ or } 450 \text{ mm c-c}$$

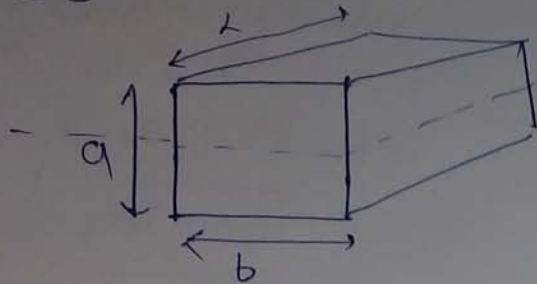
revised  $\rightarrow 5d \text{ or } 300 \text{ mm}$

So Providing  $10 \text{ mm } \phi @ 300 \text{ mm c-c}$

\*



Ans (5) (c)



$$\text{now } GM = \frac{I}{V} - BG$$

$$I_{\text{minimum (rolling)}} = \frac{1}{12} \times l \times b^3$$

$$\text{So } BG = a/2 - as/2$$

$$\text{So } (ab \cdot l) \cdot s \cdot g = (b \cdot l) \cdot x \cdot g$$

$$\text{So } \boxed{x = as}$$

$$\text{So } GM > 0 \text{ for stable eqm}$$

$$\text{So } \frac{\frac{1}{12} \times l \times b^3}{as \times b \times l} - \left[ a/2 [1-s] \right] > 0$$

$$\text{So } \frac{b^2}{12sa} > a/2 [1-s]$$

$$\text{So } \frac{b^2}{a^2} > 6s(1-s)$$

$$\text{So } \frac{b}{a} > \sqrt{6s(1-s)}$$

Ans 8(a)  $E =$  roughness coefficient,  $t =$  time.

$$\text{So } E = Kt + C$$

So at  $f = 0.02$  and  $t = 0$   $\frac{1}{\sqrt{0.02}} = 2 \log_{10} \left[ \frac{300}{E_1} \right] + 1.74$

$$E_1 = 0.648$$

$$\text{So } C = 0.648$$

\* at  $f = 0.025$   $\sim t = 10 \text{ Yrs}$   $\frac{1}{\sqrt{0.025}} = 2 \log_{10} \left[ \frac{300}{E_2} \right] + 1.74$

So  $1.5305 = K [10^{0.648}] - 1.5305 \text{ mm}$

$$K = 0.8825$$

Now at  $t = 25 \text{ Yrs}$

$$E = 0.8825 \times 25 + 0.648 = 22.5 \text{ mm}$$

# Now

$$\frac{1}{\sqrt{f}} = 2 \log_{10} \left[ \frac{300}{2.85425} \right] + 1.74$$

$$f = 0.0298$$

Ans 8(b) total load =  $4 \text{ kN/m}$  (live, imposed load)

$$D.L = 25 \text{ kN/m}^3 \times 0.25 \times 0.4 = 2.5 \text{ kN/m}$$

$$\text{So Total load} = 4 + 2.5 = 6.5 \text{ kN/m}$$

(1) When beam is fully loaded  $\sim$  Moment =  $W \times l^2 / 8 = \frac{6.5 \times 7^2}{8} = 45.703 \text{ kNm}$

\* Now at suff.  $\frac{\text{force}}{\text{Area}} = 0$

$$\sigma_{\text{suff}} = \frac{P}{A} - \frac{M \times y_{\text{suff}}}{I} \quad (\sigma_{\text{suff}} = 0)$$

$$\text{So } \frac{45.703 \times 10^6}{\frac{1}{12} \times 250 \times 400^3} \times 200 \times 400 \times 250 = 85.545 \text{ kN}$$



$$\textcircled{ii} \quad \sigma_{\text{bottom}} = 0 = \sigma_{\text{uniform}} = \frac{P_2}{A} + \frac{P \cdot e \cdot Y}{I} - \frac{H \cdot Y}{I}$$

$$\Rightarrow P \left[ \frac{Y}{A} + \frac{e \cdot Y}{I} \right] = \frac{H \cdot Y}{I}$$

$$P \frac{45.70 \times 200}{12 \times (250) \times 400^3} \times \left[ \frac{1}{100 \times 250} + \frac{60 \times 200 \times 12}{250 \times 400^3} \right]$$

$$\boxed{P = 860.813 \text{ kN}}$$

⑧ Ans a-① So total no of variables (T, D, N, μ, ρ)

So and fundamental dimension = 3

$$\text{No of } \pi\text{-terms} = 5 - 3 = 2$$

$$\text{So } \pi_1 = [D]^{a_1} [N]^{b_1} [\rho]^{c_1} T$$

$$\pi_2 = [D]^{a_2} [N]^{b_2} [\rho]^{c_2} \mu$$

$$D = L$$

$$\rho = ML^{-3}$$

$$N = T^{-1}$$

$$T = ML^2 T^{-2}$$

$$\mu = \frac{MLT^{-2} \times T}{L^2} = ML^{-1} T^{-1}$$

$$\text{So } \pi_1 = [L]^{a_1} [T^{-1}]^{b_1} [ML^{-3}]^{c_1} ML^2 T^{-2}$$

$$\pi_1 = [L]^{a_1 - 3c_1 + 2} [T]^{-b_1 - 2} [M]^{c_1 + 1}$$

$$\text{So } a_1 - 3c_1 + 2 = 0 \quad \text{So } a_1 = -5 \quad b_1 = -2 \quad c_1 = -1$$

$$-b_1 - 2 = 0$$

$$c_1 + 1 = 0$$

$$\text{So } \pi_1 = \left[ \frac{1}{D^5} \times \frac{1}{N^2} \times \frac{1}{\rho} \right] \times T \quad \text{--- eqn (1)}$$

$$\pi_2 = [L]^{a_2} [T^{-1}]^{b_2} [ML^{-3}]^{c_2} \times ML^{-1} T^{-1}$$

$$\pi_2 = [L]^{a_2 - 3c_2 - 1} [T]^{-b_2 - 1} [M]^{c_2}$$

$$\text{So } a_2 - 3c_2 - 1 = 0$$

$$-b_2 - 1 = 0$$

$$c_2 + 1 = 0$$

$$a_2 = -2$$

$$b_2 = -1$$

$$c_2 = -1$$

$$\left[ \pi_2 = \left[ \frac{1}{D^2 N \rho} \right] \times \mu \right] \quad \text{--- eqn (2)}$$

So from eq (1) and (2)

$$\Pi = \left[ \frac{T}{D^5 N^2 \rho g} \right], \left[ \frac{\omega}{D^2 N \rho} \right]$$

$$\text{So } T = D^5 N^2 \rho g \phi \left[ \frac{\omega}{D^2 N \rho} \right]$$

$$\text{Ans c (ii)} \quad T_{\text{critical}} = 2 \times L / C = \frac{2 \times 3500}{1483.23} = 4.719 \text{ sec.}$$

$$C = \sqrt{\frac{K}{\rho}} = \sqrt{\frac{2.2 \times 10^9}{10^3}} = \sqrt{2.2} \times 10^3 = 1483.23 \text{ m/s}$$

and if it is closed in 4s then rapid closure

$$p = \rho \omega C = 10^3 \times 0.8 \times 1483.23 = 1186.584 \text{ kPa}$$

$$\text{Ans c (ii)} = 1483.23 \times 4 = 5932.92 \text{ m}$$

$$\times (1000 - 5932.92) = \underline{1067.08 \text{ m}}$$