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NAME -

ROLL N -

TEST -

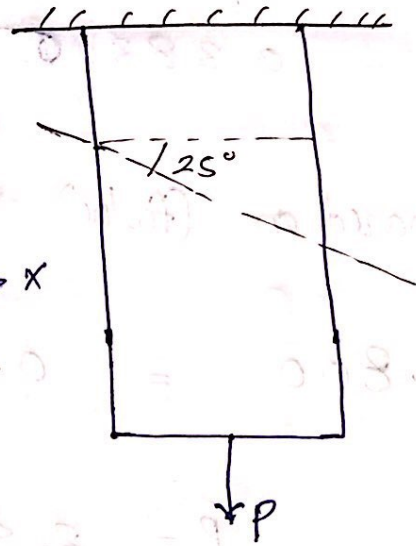
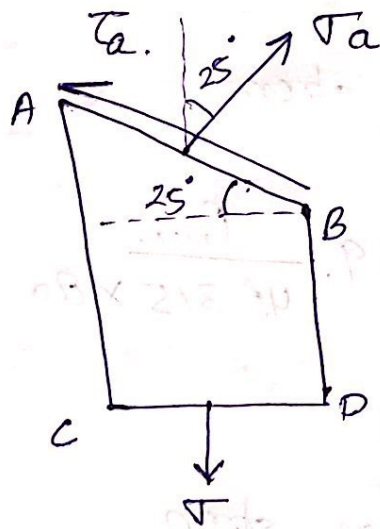
SUB - FULL SYLLABUS

Paper - IF

Total marks=234

Q-1 a)

FBD of lower portion.



$$\cancel{\sigma} = \cancel{\frac{P}{A}} = \cancel{\frac{P}{50 \times 80}} \quad \text{--- (1)}$$

$AB = 50 \text{ mm}$

$w = 80 \text{ mm}$

$CD = AB \cos 25^\circ$
 $= 45.315 \text{ mm}$

Balance force in x-direction

$$T_a AB (\text{width}) \sin 25^\circ - T_a AB (\text{width}) \cos 25^\circ = 0$$

$$T_a \sin 25^\circ - T_a \cos 25^\circ = 0$$

$$\boxed{\frac{T_a}{T_a} = 2.1445} \quad \text{--- (1)}$$

force balance in y direction.

$$\cos 25^\circ \times T_a AB \cdot w + T_a AB \cdot w \sin 25^\circ = \sigma \cdot CB \cdot w$$

$$T_a \cos 25^\circ + T_a \sin 25^\circ = \sigma \frac{CB}{AB}$$

$$0.9063 T_a + 0.4226 T_a = 0.9063 \sigma$$

solving (1) & (2)

$$\sigma_a = 0.82139 \sigma \quad \text{--- ①}$$

$$\tau_a = 0.3830 \tau \quad \text{--- ②}$$

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① based on (failure) Normal stress

$$0.800 = 0.82139 \cdot \frac{P_{max}}{45.315 \times 80}$$

$$P_{max} = 3.53 \text{ kN}$$

Good

② failure based on shear stress

$$0.6 = 0.3830 \cdot \frac{P_{max}}{45.315 \times 80}$$

$$P_{max} = 5.679 \text{ kN}$$

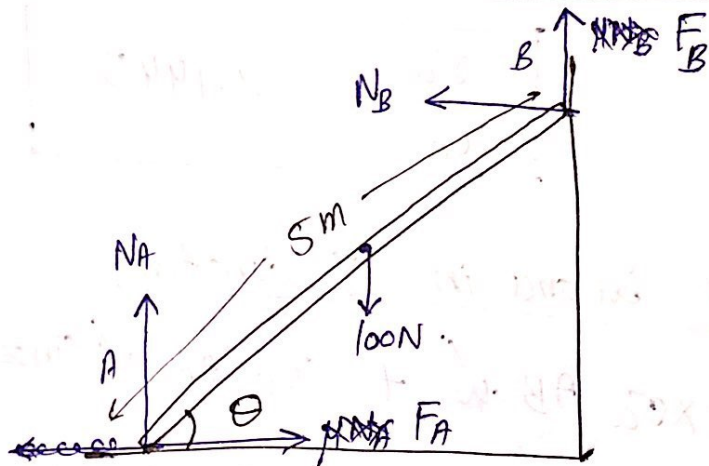
so Max^m centric load $P_{max} = 3.53 \text{ kN}$

1 ⑥

$$W = 100 \text{ N}$$

$$\mu = 0.3$$

$$L = 5 \text{ m}$$



N_A & $N_B \rightarrow$ Normal force at A & B resp.

$$\sum M_A = 0$$

For θ_{min} [frictional force will be max^m]

Limiting cond.

$$F_B = \mu N_B \quad \& \quad F_A = \mu N_A$$

$$\sum F_y = 0$$

$$100 = \mu N_B + N_A \quad \text{--- (1)}$$

$$\sum F_x = 0$$

$$\mu N_A = N_B \quad \text{--- (2)}$$

solving (1) & (2) taking $\mu = 0.3$

$$N_A = 91.743 \text{ N}, \quad N_B = 27.523 \text{ N.}$$

$$\sum M_A = 0$$

$$100 \times \frac{\cancel{\sin}}{2} \cos \theta_{min} = 27.523 \times \cancel{\sin} \sin \theta_{min} + 0.3 \times 27.523 \times \cancel{\cos} \cos \theta_{min}$$

$$41.743 \cos \theta_{min} = 27.523 \sin \theta_{min}$$

$$\theta_{min} = 56.6^\circ$$

for $\theta = 45$

using eqⁿ (1) & (2)

$$100 = \mu N_B + \frac{N_B}{\mu}$$

$$N_B = \frac{100 \mu}{1 + \mu^2}$$

$$100 \times \frac{\cancel{\sin}}{2} \cos 45 = \frac{100 \mu}{1 + \mu^2} \times \cancel{\sin} \sin 45 + \frac{100 \mu^2}{1 + \mu^2} \times \cancel{\cos} \cos 45$$

$$(1 + \mu^2) 50 = 100 (\mu^2 + \mu) \quad \Rightarrow \quad 50 \mu^2 + 100 \mu - 50 = 0$$

$$\mu = 0.4142$$

Q-1 (c)

(i) Cycloidal Profile in Cams :-

- These profile are used for very high speed applications ^{and have} minimize the jerk.
- Cycloidal velocity profile consist of cam having smooth rise and return operation.

Advantages :-

- * No impact stresses so it can be used for the high speed applications.
- * Least jerk at the cam which avoid the surface stresses at cam profile.

Disadvantages :-

- * the cost of manufacturing of this profile is very high.
- * It require ~~proper~~ exact dimensioning (lower tolerance).

(ii) Considering the outstroke.

$$x_o = h \left[\frac{\theta}{\theta_o} - \frac{1}{2\pi} \sin\left(\frac{2\pi\theta}{\theta_o}\right) \right]$$

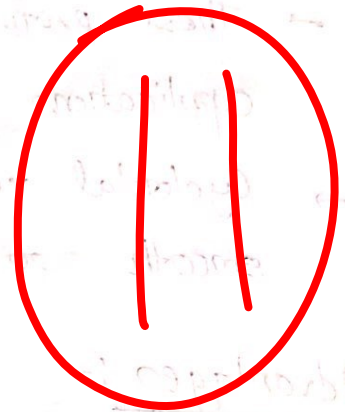
for velocity

$$\begin{aligned} \frac{dx_o}{dt} &= \frac{dx_o}{d\theta} \cdot \frac{d\theta}{dt} \\ &= \omega \frac{dx_o}{d\theta} = \omega \cdot h \left[\frac{1}{\theta_o} - \frac{1}{\theta_o} \cos\left(\frac{2\pi\theta}{\theta_o}\right) \right] \\ &= \frac{\omega h}{\theta_o} \left[1 - \cos\frac{2\pi\theta}{\theta_o} \right] \\ &= \frac{\omega h}{\theta_o} \left[2 \sin^2 \frac{\pi\theta}{\theta_o} \right] \end{aligned}$$

$$V = \frac{2\omega h}{\theta_0} \left[\sin^2 \frac{\pi\theta}{\theta_0} \right]$$

$$V_{\max} \text{ @ } \theta = \frac{\theta_0}{2}$$

$$V_{\max} = \frac{2\omega h}{\theta_0}$$



for Acceleration

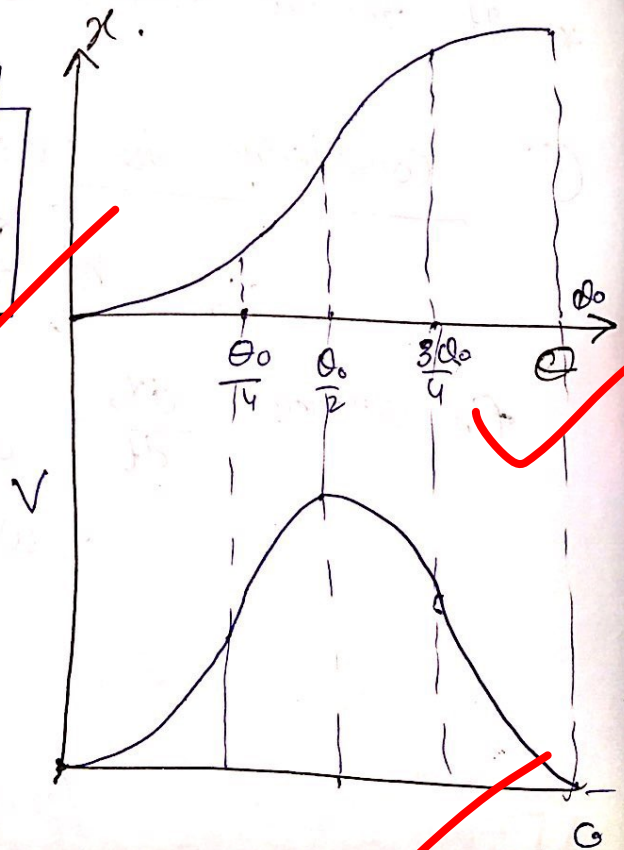
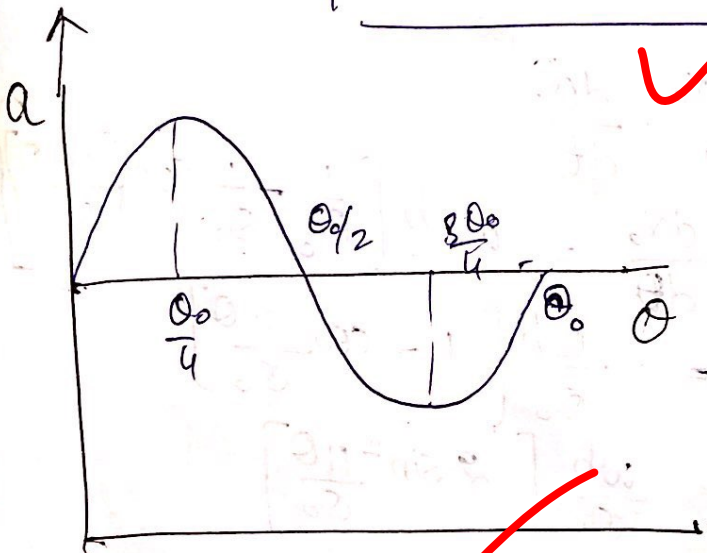
$$a = \frac{dv}{dt} = \frac{dv}{d\theta} \cdot \frac{d\theta}{dt}$$

$$= \omega \cdot \frac{2\omega h}{\theta_0} \left[2 \sin \frac{\pi\theta}{\theta_0} \cdot \frac{\cos \pi\theta}{\theta_0} \right] \frac{\pi\theta}{\theta_0}$$

$$a = \frac{2\pi \omega^2 h}{\theta_0^2} \left[\sin \left(\frac{2\pi\theta}{\theta_0} \right) \right]$$

$$a_{\max} \text{ @ } \theta = \theta_0/4$$

$$a_{\max} = \frac{2\pi \omega^2 h}{\theta_0^2}$$



Q-1(d)

$$m = 6.5 \text{ mm}$$

$$t = 19$$

$$r = \frac{m \cdot t}{2} = 61.75 \text{ mm}$$

$$T = 47$$

$$R = 152.75 \text{ mm}$$

$$\phi = 20^\circ$$

$$\text{addendum} = 6.5$$

$$[A=1]$$

path of Approach (POA)

$$= \sqrt{R_A^2 + R^2 \cos^2 \phi} - R \sin \phi$$

$$r_A = 61.75 + 6.5$$

$$= 68.25 \text{ mm}$$

$$R_A = 159.25 \text{ mm}$$

$$POA = \sqrt{(159.25)^2 - (152.75)^2 \cos^2 20} - 152.75 \sin 20$$

$$= 16.73 \text{ mm}$$

Path of recess = POR = $\sqrt{r_A^2 - r^2 \cos^2 \phi} - r \sin \phi$

$$= \sqrt{68.25^2 - 61.75^2 \cos^2 20} - 61.75 \sin 20$$

$$= 14.811 \text{ mm}$$

Path of contact = POA + POR = 16.73 + 14.811

$$= 31.5411 \text{ mm}$$

Arc of contact = $\frac{POC}{\cos \phi} = \frac{31.541}{\cos 20} = 33.56 \text{ mm}$

More variations than acceptable

33.56

$$\begin{aligned}\text{Contact Ratio} &= \text{No of teeth in contact} \\ &= \frac{AOC}{\text{pitch}} = \frac{34.629}{\pi \times 6.5} \\ &= 1.6958 \quad 1.64\end{aligned}$$

$$\begin{aligned}\text{Angle Turned by larger wheel} &= \frac{AOC}{R} \\ &= \frac{34.629}{152.75} \\ &= 0.2267 \text{ rad.} \\ &= 12.99^\circ\end{aligned}$$

Angular speed of smaller wheel ω_1

$$\omega_1 = \frac{V}{r} = \frac{1.2}{0.06175} = 19.433 \text{ rad/s}$$

$$\frac{\omega_2}{\omega_1} = \frac{T_1}{T_2}$$

$$\omega_2 = 7.856 \text{ rad/s}$$

(i) Sliding velocity when engagement start

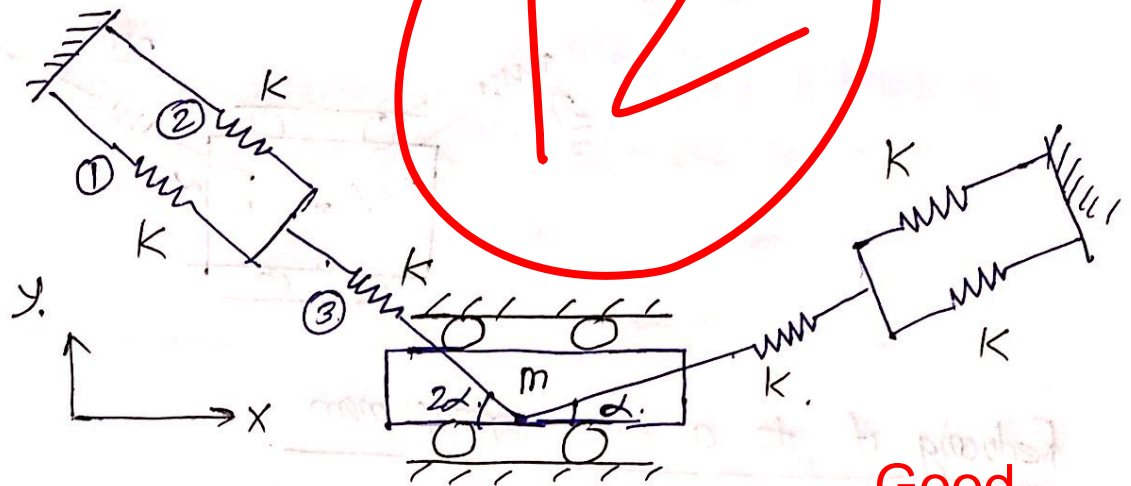
$$\begin{aligned}V_{s1} &= (\omega_1 + \omega_2) (K.P) \\ &= (19.433 + 7.856) 0.01673 \\ &= 0.4565 \text{ m/s}\end{aligned}$$

① When engagement ends.

$$\begin{aligned}V_{s2} &= (\omega_1 + \omega_2) P.L \\ &= (19.433 + 7.856) \times 0.014811 \\ &= 0.4041 \text{ m/s}\end{aligned}$$

② at pitch point $Q.P = 0$ $V = 0$

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$m = 5 \text{ kg}$, $K = 2 \text{ kN/m}$.

Calculation of equivalent spring stiffness.

for LHS spring system.

spring 1 & spring 2 are in parallel.

for equiv. of ① 2 ②.

$S_{12} = S_1 + S_2$

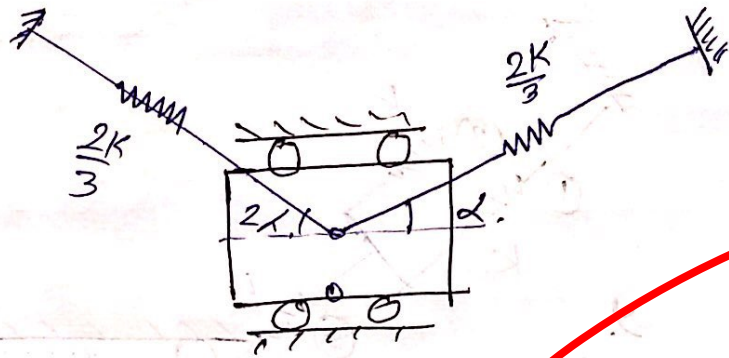
$$K_{12} = S_{12} = K_1 + K_2 = 2K$$

2 3 in series

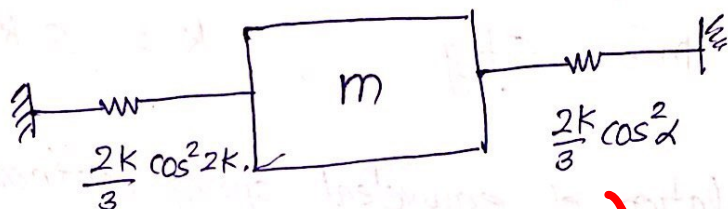
$$\frac{1}{R_{eq}} = \frac{1}{K_{12}} + \frac{1}{K} = \frac{1}{2K} + \frac{1}{K}$$

$$S_{eq} = \frac{2K}{3}$$

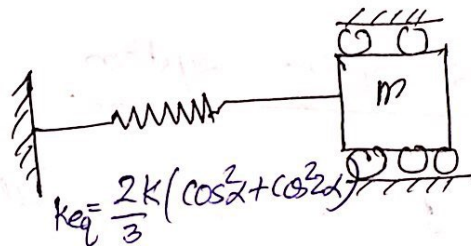
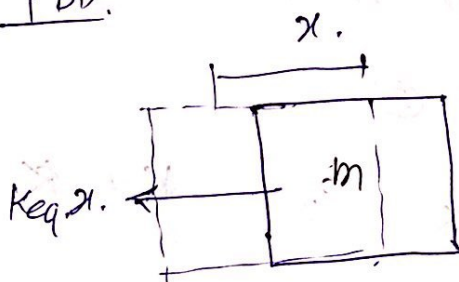
Now equivalent spring system



Reducing it to a single spring mass



FBD.



Applying D'Alemberts law

$$ma + K_{eq} x = 0$$

$$m \ddot{x} + \frac{2K}{3} (\cos^2 \alpha + \cos^2 2\alpha) x = 0$$

Eqⁿ of motion.

$$\omega_n = \sqrt{\frac{2K}{3m} (\cos^2 \alpha + \cos^2 2\alpha)} = \sqrt{\cos^2 \alpha + \cos^2 2\alpha} \times 16.33 \text{ rad/s}$$

$$\omega_n = 16.33 \sqrt{\cos^2 \alpha + \cos^2 2\alpha}$$

Q-2(a)

Total load. = 6000N.

$R_A = 3000N$
 $R_B = 3000N$ } due to
 symm.
 loading

Let load intensity

$$y = ax^2 + bx + c$$

① at $x=0, y=0$

$\Rightarrow c=0$

$$y = ax^2 + bx$$

② at $x=2 \frac{dy}{dx}=0$

$$\frac{dy}{dx} = 2ax + b$$

$$0 = 2a \times 2 + b$$

$$4a + b = 0 \quad \text{--- (1)}$$

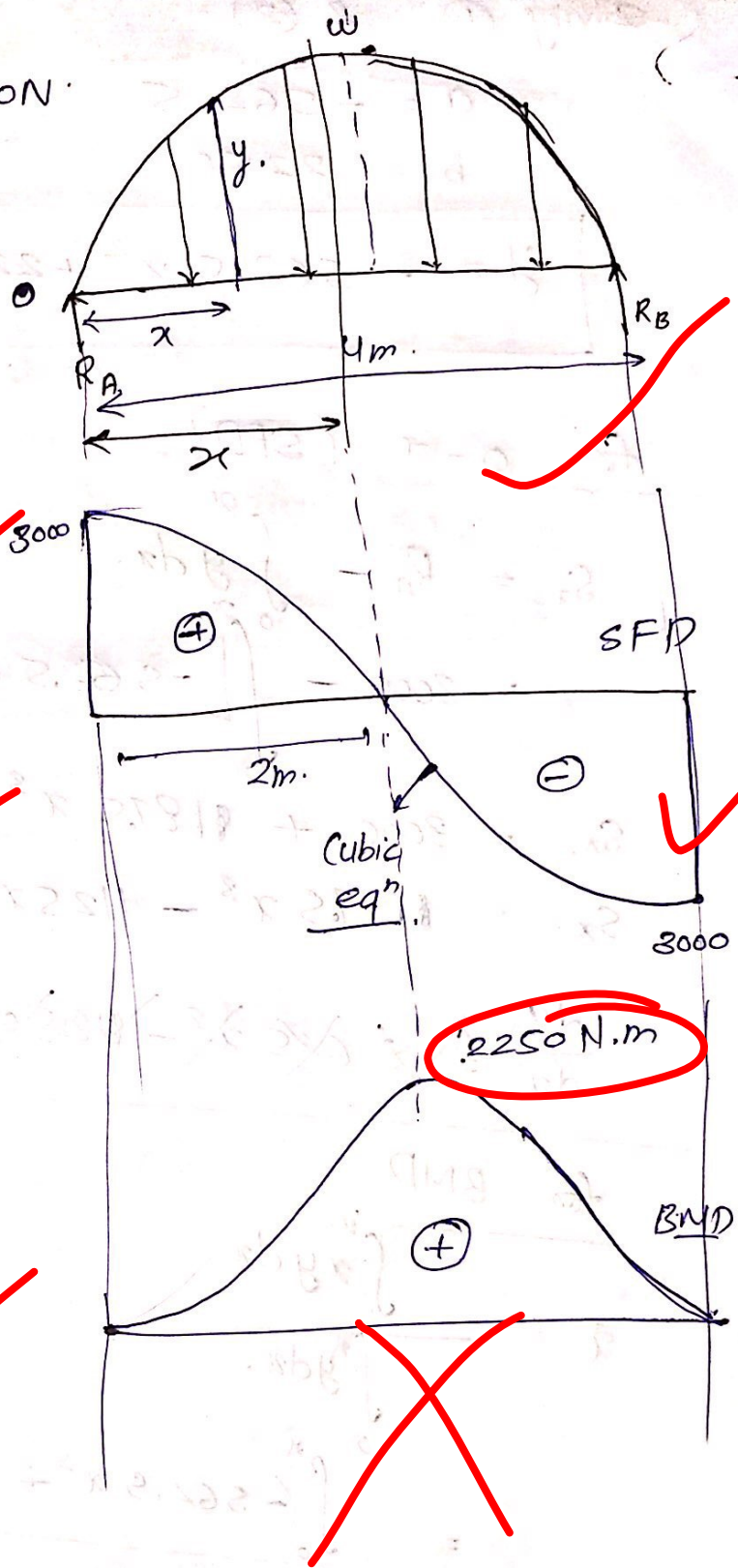
③ at $x=4, y=0$

~~$$0 = 16a + 4b$$~~

$$\text{Total load} = \int_0^4 y \cdot dx$$

$$6000 = \int_0^4 (ax^2 + bx) dx$$

$$6000 = a \frac{64}{3} + 8b \quad \text{--- (2)}$$



Solving ① & ②

$$a = -562.5$$

$$b = 2250$$

$$y = -562.5x^2 + 2250x$$

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for 0-x (SFD)

$$S_x = R_A - \int_0^x y dx$$

$$= 3000 - \int_0^x [-562.5x^2 + 2250x] dx$$

$$S_x = 3000 + 187.5x^3 - 1125x^2$$

$$S_x = 187.5x^3 - 1125x^2 + 3000$$

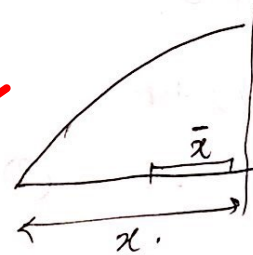
$$\frac{dS_x}{dx} = 562.5x^2 - 2250x = 0$$

for BMD

$$\bar{x} = \frac{\int_0^x xy dx}{\int_0^x y dx}$$

$$= \frac{\int_0^x (-562.5x^3 + 2250x^2) dx}{\int_0^x (-562.5x^2 + 2250x) dx}$$

$$= \frac{-140.625x^4 + 750x^3}{-187.5x^3 + 1125x^2}$$



$$= \frac{-140.625x^2 + 750x}{-187.5x + 1125}$$

$$\bar{x} = \frac{-0.125x^2 + 0.667x}{-0.1666x + 1}$$

$$M_x = R_A \cdot x - \int_0^x (-562.5x^2 + 2250x) d\bar{x}$$

$$= 3000x + \left(187.5x^3 + 1125x^2 \right) \left(\frac{-0.125x^2 + 0.667x}{-0.1666x + 1} \right)$$

$$= 3000x + (-1125x^2) \left(-0.125x^2 + 0.667x \right)$$

$$M_x = 140.625x^4 - 750x^3 + 3000x$$

M · max at $x = 2$

$$\frac{dM_x}{dx} = 0 \text{ at } x = 2$$

$$M_{\max} = 2250 \text{ N.m}$$

$$\frac{d^2M}{dx^2} = 1687.5x^2 - 4500x$$

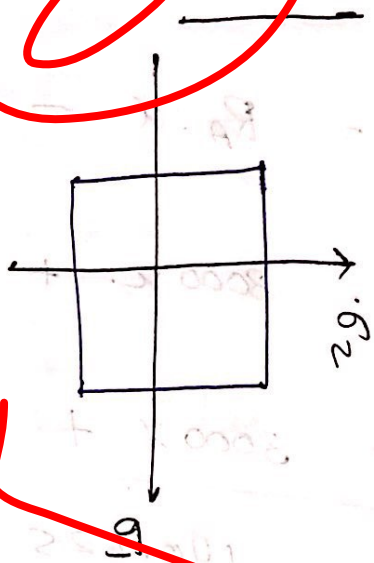
$$\begin{array}{c} + \quad - \quad + \\ \hline \checkmark \quad 0 \quad \wedge \quad 2.667 \quad \checkmark \end{array}$$

$$M_{x=1} = 140.625 - 750 + 3000$$

Q-2 (b) (i)

Ans:

MPS T

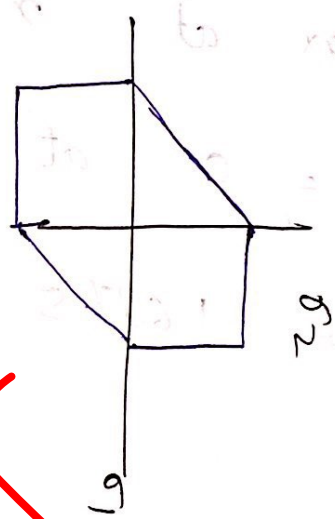


This theory gives good Result for materials which do not yield

$$\sigma_1 \leq \frac{S_{yt}}{N}$$

the Graph will always form a square for various values of σ_1 and σ_2

MSST

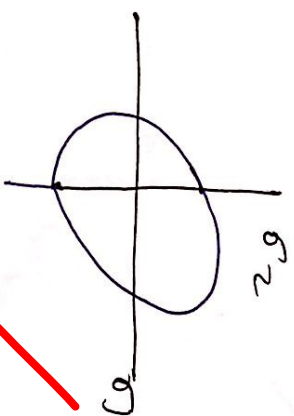


It is a conservative theory used for material which shows yielding

$$\frac{(\sigma_1 - \sigma_2)}{2} \leq \frac{S_{ys}}{N}$$

the Graph is hexagon & design will be more safer when the principle stresses are same in nature.

MDT



It is the economical theory used for ductile material.

$$\sqrt{\sigma_1^2 + \sigma_2^2 + \sigma_1 \sigma_2} \leq \frac{S_{yt}}{N}$$

* It is not applicable for a material which is under the hydrostatic state of stress.

Q-2(b)

$$\sigma_{yt} = 380 \text{ N/mm}^2$$

$$\sigma_x = 100 \text{ N/mm}^2, \sigma_y = 40 \text{ N/mm}^2, \tau_{xy} = 80 \text{ N/mm}^2$$

① for max^m principal stress theory :-

$$\sigma_{1/2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$= 70 \pm \sqrt{(30)^2 + 80^2}$$

$$\sigma_1 = 155.44 \text{ MPa.}$$

$$\sigma_2 = -15.44 \text{ MPa.}$$

$$\sigma_1 \leq \sigma_{yt}$$

$$155.44 \leq \frac{380}{N} \quad N = 2.444$$

as per the MPST the material will not fail.

② Maximum shear stress theory :

$$[\tau_{\max}]_{\text{absolute}} = \text{Max}^m \left[\frac{\sigma_1 - \sigma_2}{2}, \frac{\sigma_1}{2}, \frac{\sigma_2}{2} \right]$$

$$= \frac{155.44 + 15.44}{2}$$

$$= 85.44 \text{ MPa}$$

$$\tau_{PS} = \frac{\sigma_{ys}}{2} = \frac{380}{2} = 190$$

$$N = 2.2237$$

③ Max^m Distortion Energy theory:

$$155.44^2 + 15.44^2 + 155.44 \times 15.44 \leq \left(\frac{380}{N}\right)^2$$

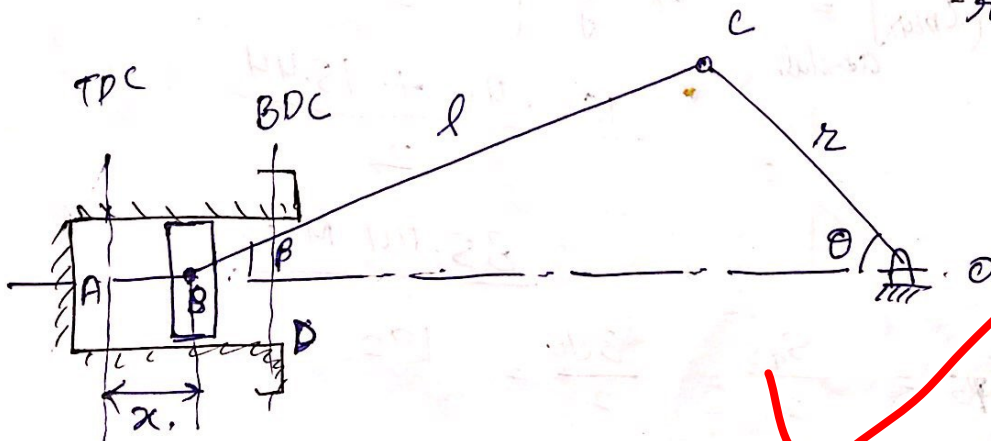
$$N = 2.32/2$$

$$N_{MSST} > N_{DET} > N_{MSST}$$

c.R length $l = 175 \text{ mm} = 0.175 \text{ m}$

$$N = 400 \text{ rpm}$$

$$n = \underline{2}$$



from the figure shown.

displacement $x = OA - OB$

$$OA = l + r$$

$$OB = r \cos \theta + l \cos \beta$$

$$x = l + r - l \cos \beta - r \cos \theta \quad \text{--- (1)}$$

$$\sin \beta = \frac{\sin \theta}{n}$$

$$\cos \beta = \sqrt{1 - \sin^2 \beta} = \frac{\sqrt{n^2 - \sin^2 \theta}}{n}$$

putting in eqn (1)

$$x = l + r - \frac{l \sqrt{n^2 - \sin^2 \theta}}{n} - r \cos \theta$$

$$x = r \left[(1 - \cos \theta) + \left(n - \sqrt{n^2 - \sin^2 \theta} \right) \right]$$

Velocity $= \frac{dx}{dt} = \frac{dx}{d\theta} \cdot \frac{d\theta}{dt} = \omega \frac{dx}{d\theta}$

$$= \omega r \left[\sin \theta - \frac{2 \sin \theta \cos \theta}{2 \sqrt{n^2 - \sin^2 \theta}} \right]$$

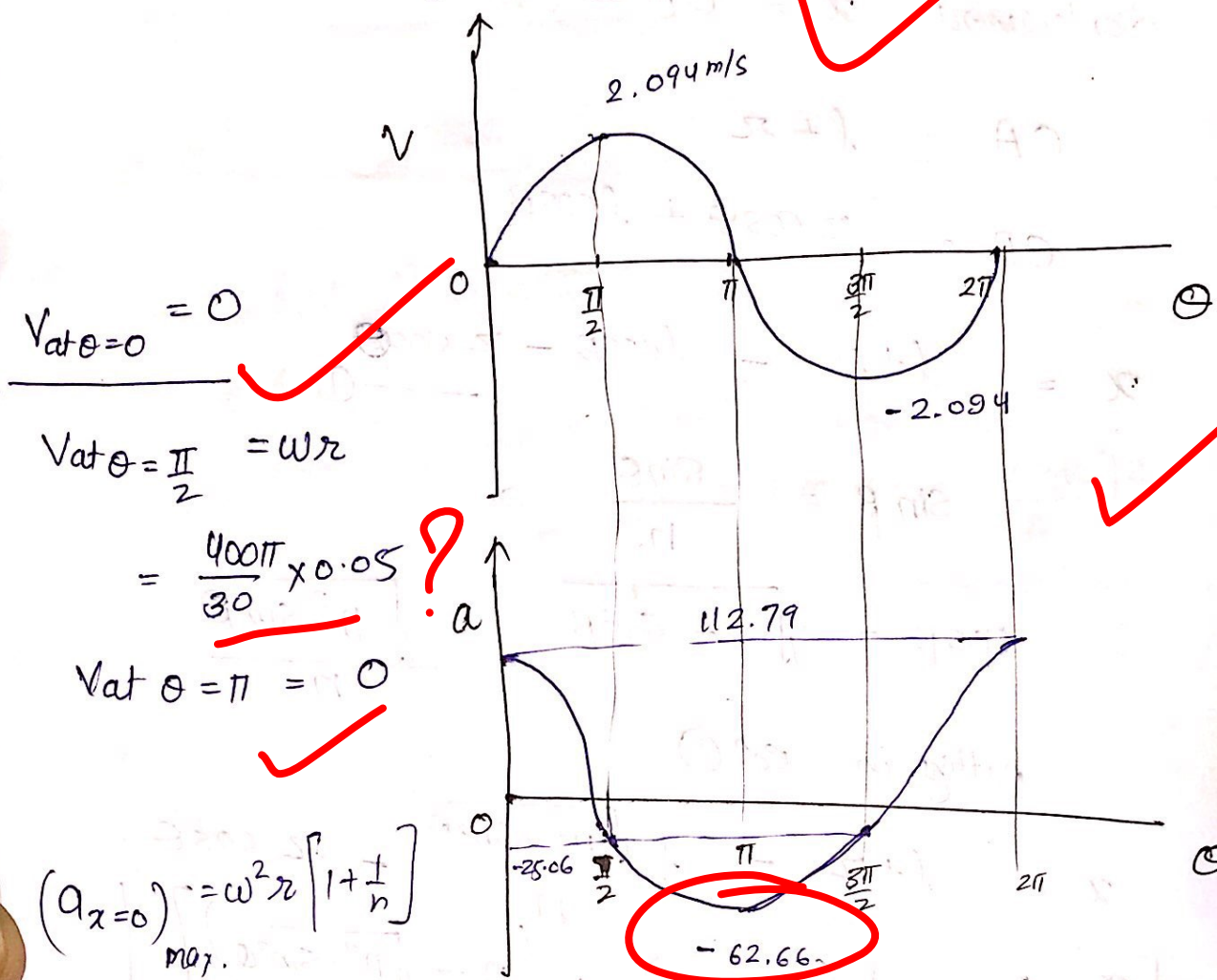
$$V = \omega r \left[\sin \theta + \frac{\sin 2\theta}{2 \sqrt{n^2 - \sin^2 \theta}} \right]$$

assuming $n^2 - \sin^2 \theta \rightarrow n^2$

Acceleration $a = \frac{dv}{dt} = \frac{dv}{d\theta} \cdot \frac{d\theta}{dt} = \omega \frac{dv}{d\theta}$

$$= \omega^2 r \left[\cos \theta + \frac{2 \cos 2\theta}{2n} \right]$$

$$a = \omega^2 r \left[\cos \theta + \frac{\cos 2\theta}{n} \right]$$



$$V_{at \theta=0} = 0$$

$$V_{at \theta=\frac{\pi}{2}} = \omega r$$

$$= \frac{400\pi}{30} \times 0.05$$

$$V_{at \theta=\pi} = 0$$

$$(a_{\theta=0}) = \omega^2 r \left[1 + \frac{1}{n} \right]$$

$$= 112.79 \text{ m/s}^2$$

$$a_{\theta=\frac{\pi}{2}} = -25.06 \text{ m/s}^2$$

$$a_{\theta=\pi} = -62.66 \text{ m/s}^2$$

$$a_{\theta=\frac{3\pi}{2}} = -25.06 \text{ m/s}^2$$

$$a_{\theta=2\pi} = 112.79 \text{ m/s}^2$$

$$n = \frac{175}{50} = 3.5$$

for acceleration to be zero

$$\cos \theta + \frac{\cos 2\theta}{n} = 0$$

$$\cos \theta + \frac{2\cos^2 \theta - 1}{3.5} = 0$$

$$2\cos^2\theta + 3.5\cos\theta - 1 = 0$$

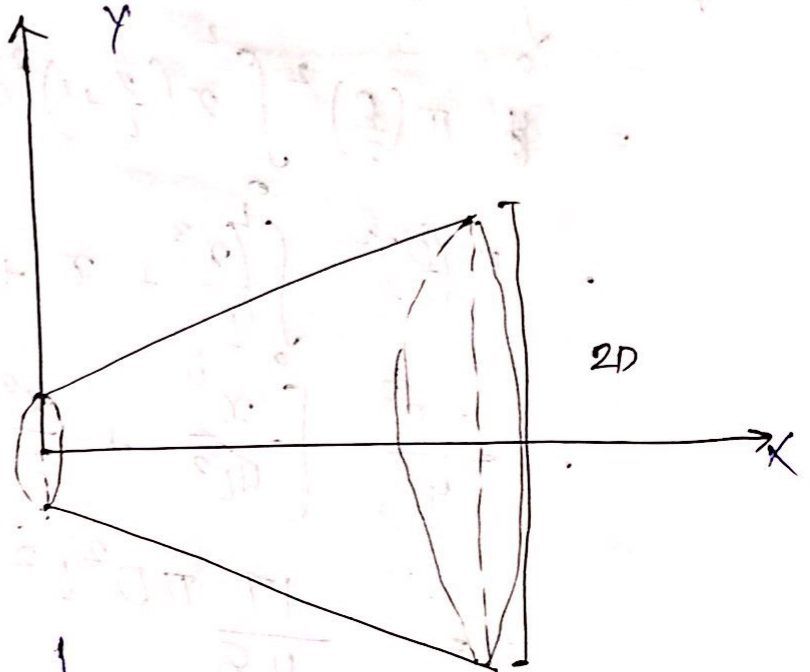
$$\cos\theta = \frac{1}{4}, \quad \cos\theta = -2 \quad \times$$

$$\theta = 75.52^\circ, 284.47^\circ$$

Q-4a)

This shape can be
Generated by revolving
a line about X Axis

For the eqⁿ of line. D

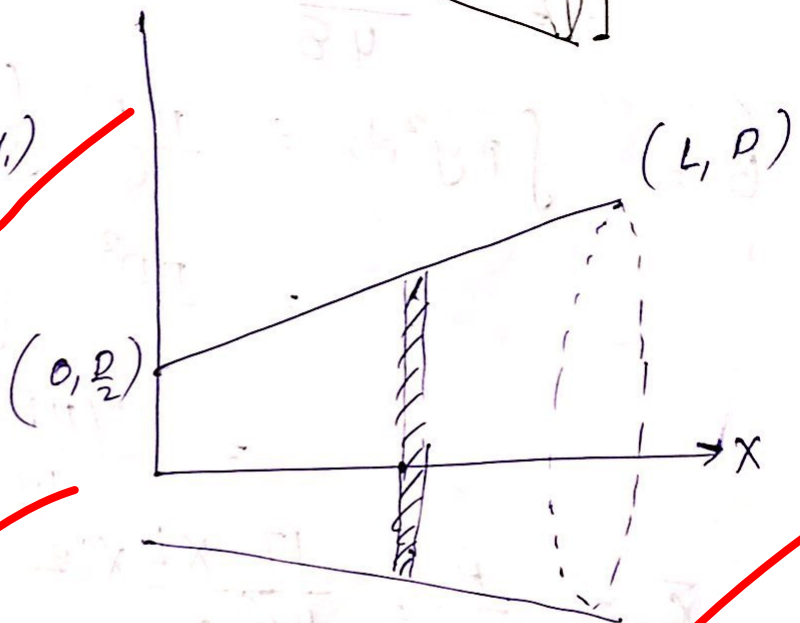


$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - \frac{D}{2} = \frac{D/2}{L} (x)$$

$$y = \frac{D}{2} \left[\frac{x}{L} + 1 \right]$$

↳ eqⁿ of line.



if this line Revolves about X-Axis

$$\bar{x} = \frac{\int \pi y^2 \cdot x \, dx}{\int \pi y^2 \, dx} = A$$

Let

$$\int \pi y^2 \, dx = B.$$

$$A = \int_0^L \pi y^2 x \, dx.$$

$$= \pi \left(\frac{D}{2}\right)^2 \int_0^L x \left(\frac{x}{L} + 1\right)^2 dx.$$

$$= \pi \left(\frac{D}{2}\right)^2 \int_0^L \left(\frac{x^3}{L^2} + x + \frac{2x^2}{L}\right) dx.$$

$$= \frac{\pi D^2}{4} \left[\frac{x^4}{4L^2} + \frac{x^2}{2} + \frac{2x^3}{3L} \right]_0^L$$

$$= \frac{17 \pi D^2 L^2}{48}$$

$$B = \int \pi y^2 dx = \frac{\pi D^2}{4} \int_0^L \left(1 + \frac{x}{L}\right)^2 dx.$$

$$= \frac{\pi D^2}{4} \left[x + \frac{x^3}{3L^2} + \frac{x^2}{L} \right]_0^L$$

$$= \frac{7 \pi D^2 L}{12}$$

$$\bar{x} = \frac{A}{B} = \frac{17 \times L \times 12}{48 \times 7} = \frac{17}{28} L$$

Ans

$$\bar{x} = 0.6071 L$$

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Q-4(b)

$$P = 7.5 \text{ kW}$$

$$@ 360 \text{ rpm}$$

$$D_1 = 250 \text{ mm}$$

$$D_2 = 500 \text{ mm}$$

$$M_1 = 10 \text{ kg}$$

$$M_2 = 30 \text{ kg}$$

$$\sigma_{yt} = 380$$

$$FOS = 3$$

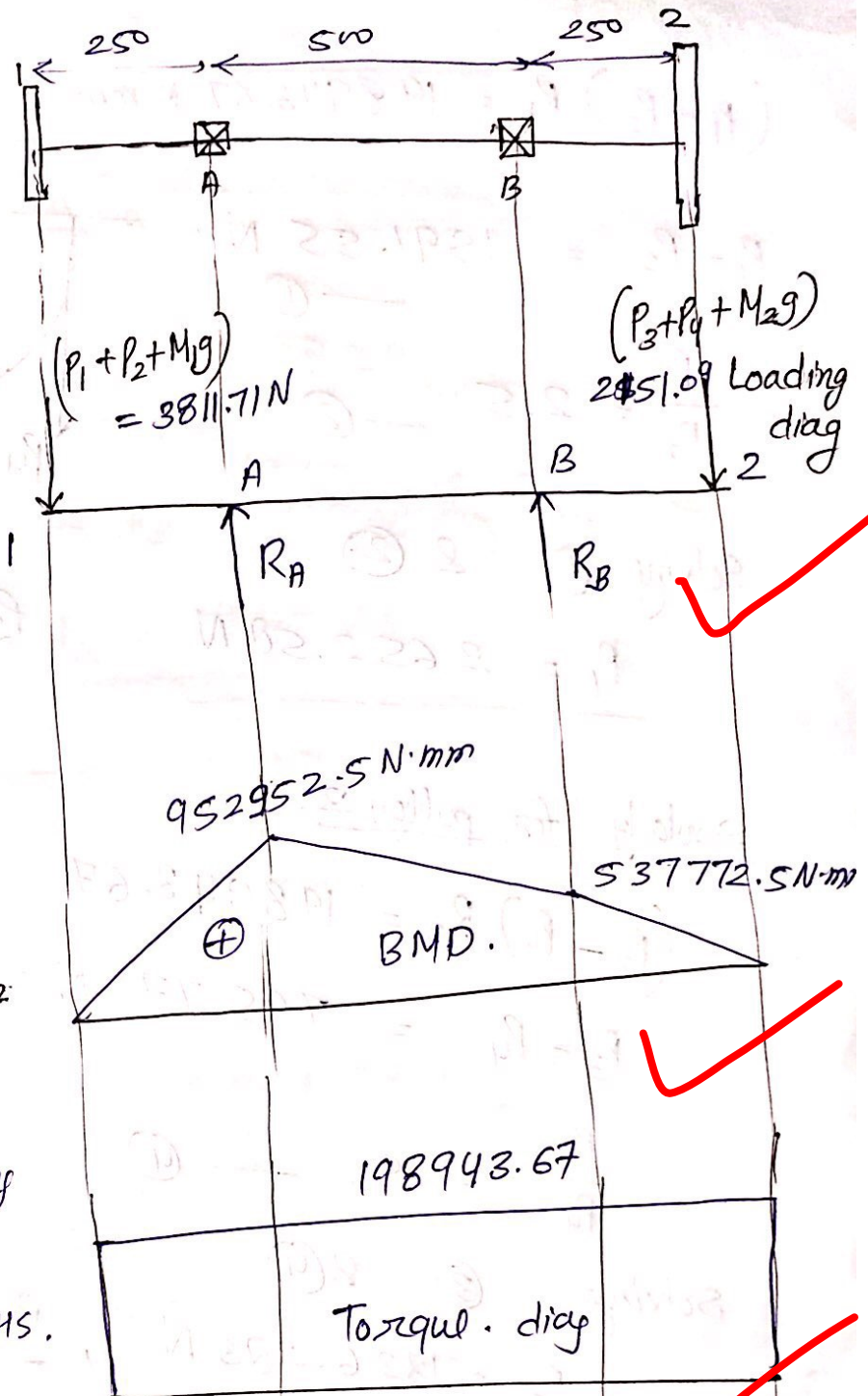
$$\theta = 0.5^\circ$$

$$G = 79300 \text{ N/mm}^2$$

Assuming shaft rotating
in ACW direction
when viewed from LHS.

$$T = \frac{P}{\omega} = \frac{7.5 \times 10^6}{\frac{2\pi \times 360}{60}}$$

$$= 198943.67 \text{ N}\cdot\text{mm}$$



$$(P_1 - P_2) R_1 = 198943.67 \text{ N}\cdot\text{mm}$$

$$P_1 - P_2 = 1591.55 \text{ N} \quad \text{--- ①}$$

$$\frac{P_1}{P_2} = 2.5 \quad \text{--- ②}$$

Solving ① & ②

$$P_1 = 2652.58 \text{ N}$$

$$P_2 = 1061.03 \text{ N}$$

Similarly for pulley 2.

$$(P_3 - P_4) R_2 = 198943.67$$

$$P_3 - P_4 = 795.77 \text{ N} \quad \text{--- ③}$$

$$\frac{P_3}{P_4} = 2.5 \quad \text{--- ④}$$

Solving ③ & ④

$$P_3 = 1326.283 \text{ N}$$

$$P_4 = 530.51 \text{ N}$$

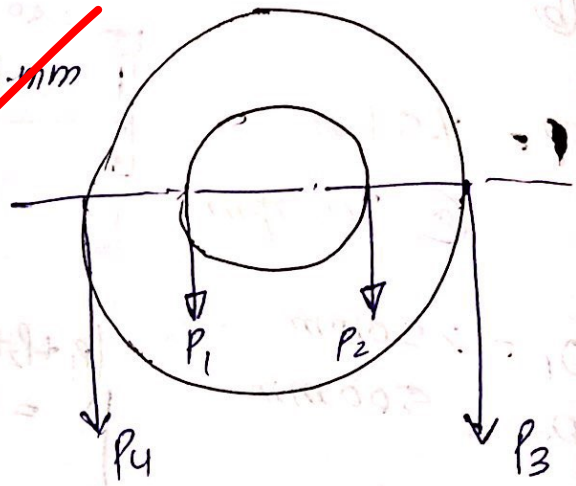
Total force at 1.

$$F_1 = P_1 + P_2 + M_1 g = 2652.58 + 1061.03 + 10 \times 9.81$$

$$= 3811.71 \text{ N}$$

$$F_2 = P_3 + P_4 + M_2 g = 1326.283 + 530.51 + 30 \times 9.81$$

$$= 2151.09 \text{ N}$$



$$R_A + R_B = F_1 + F_2$$

$$R_A + R_B = 3811.71 + 2151.09$$

$$R_A + R_B = 5962.8 \text{ N}$$

$$\sum M_A = 0$$

$$F_1 \times 2500 + R_B \times 500 = F_2 \times 750$$

$$3811.71 \times 2500 + R_B \times 500 = 2151.09 \times 750$$

$$R_B = 1320.78 \text{ N}$$

$$R_A = 4642.02 \text{ N}$$

~~Bending Moment~~ Using Rigidity Criterion

$$\theta_{\max} = \frac{TL}{GJ}$$

$$\frac{0.5 \times \pi}{180} = \frac{198943.67 \times 1000}{79300 \times \frac{\pi}{32} d^4}$$

$$d = 41.366 \text{ mm}$$

Selecting shaft diameter \rightarrow next higher number in the series of S.

$$d = 45 \text{ mm}$$

Bending Moment at critical crosssection (at A)

$$M = 952952.5 \text{ N}\cdot\text{mm}$$

$$T = 198943.67 \text{ N}\cdot\text{mm}$$

Using MDET.

$$M_e = \sqrt{M^2 + \frac{3}{4} T^2}$$
$$= \sqrt{952952.5^2 + \frac{3}{4} \times 198943.67^2}$$
$$= 968401.98 \text{ N}\cdot\text{mm}$$

$$\sigma_{\text{induced}} = \frac{32 M_e}{\pi d^3} = \frac{32 \times 968401.98}{\pi \times 45^3}$$
$$= 108.247 \text{ N/mm}^2$$

$$\sigma_{\text{per}} = \frac{380}{3} = 126.66 \text{ N/mm}^2$$

$$\sigma_{\text{induced}} < \sigma_{\text{per}}$$

Hence design is safe.

$$d = 45 \text{ mm}$$

Q-4 ©

$$M = 250 \text{ kg}$$

piston mass $m_p = 3.75 \text{ kg}$

stroke $L = 150 \text{ mm}$

crank. Rad. $\alpha = L/2 = 75 \text{ mm}$

Transmitted load $(F_T)_{\max} = 500 \text{ N}$

$N = 750 \text{ rpm}$

$$\omega = \frac{750 \times 2\pi}{60} = 78.54 \text{ rad/s}$$

unbalance force due to recip mass

$$(F_0)_{\max} = m \alpha \omega^2$$

$$= 3.75 \times 0.075 \times (78.54)^2$$
$$= \underline{1734.9 \text{ N}}$$

as per question.

$$\frac{F_T}{F_0} = \frac{1}{\sqrt{(1 - \gamma^2)^2}}, \quad \gamma = \frac{\omega}{\omega_n}$$

$$\Sigma = 0$$

$$\frac{500}{1734.9} = \frac{1}{\sqrt{(1 - \gamma^2)^2}}$$

$$\gamma^2 - 1 = \frac{1734.9}{500}$$

$$\gamma^2 = 3.47 + 1$$
$$\boxed{\gamma = 2.114}$$

$$2.114 = \frac{\omega}{\omega_n} = \frac{78.54}{\omega_n}$$

$$\boxed{\omega_n = 37.1523 \text{ rad/s}}$$

$$37.1523 = \sqrt{\frac{s}{250}}$$

$$\text{stiffness } s = 345.073 \text{ kN/m}$$

① at $N = 800 \text{ rpm}$

$$\omega = 83.775 \text{ rad/s.}$$

$$F_o = m r \omega^2 = 3.75 \times 0.075 \times 83.775^2 = 1973.88$$

Amplitude $A = \frac{F_o/s}{\left(\frac{\omega}{\omega_n}\right)^2 - 1} = \frac{1973.88}{\left(\frac{83.775}{37.1523}\right)^2 - 1}$

$$\boxed{A = 1.4 \text{ mm}}$$

② below 750 rpm.

$$\frac{500}{3.75 \times 0.075 \omega^2} = \frac{1}{1 - \left(\frac{\omega}{37.1523}\right)^2}$$

by solving. $\omega = 27.875 \text{ rad/s.}$

$$\boxed{N = 266.18 \text{ rpm}}$$

Q-5@

Function of Flux Coating

① Deoxidisers

flux coating may work on deoxidisers & prevent the oxidation.

Eg: Graphite, Silicon, ferro silicon. etc.

② Arc stabilizers

Arc stabilisers are added in the flux coating which help to stabilise arc and high speeds and at different ~~at~~ orientation of welding

Eg: Ferran oxide, silicon oxide, potassium silicate etc.

③ slag forming Agents

these are added to the flux coating & they form slag & prevent molten metal to come in contact with atmospheric gases.

Eg: ferran oxide, Titanium oxide, CaF_2 etc.

④ Alloying element

Some time alloying element is added in the coating they enhance the quality of weld, small amount of alloy impurity can strengthen the welded joint.

Eg: Ni, Cr, Co.

⑤ Gas forming Compounds

Gas forming compounds are added that convert into gas & protect weld pool.

Eg: Cellulose, CaCO_3 .

0-5⑥

① Titanium Alloys

- Titanium alloys having very good strength and having approximately half weight compared to iron so they can be used widely
- their carbides are used in cutting tool material TiC having 3100 VHN hardness.

Limitation

- Machinability of Titanium & its alloys are very poor

→ Costly.

Application

- Used in Aircrafts
- cutting tool material.

② Refractory Materials

- Refractory materials are those, which can withstand at elevated temperature.
- They do not lose their Mechanical properties at the elevated Temp.

Eg: Al_2O_3 , Graphite.

Limitation

Every material has certain Temp beyond which they can't withstand

Application

- Used in furnace lining
- Crucibles (Annealing)
- Metal casting dies.

8

Super Alloys :

these are Generally Ni based Alloy in which more than 10% Alloying is done to enhance the properties at different working conditions

Eg: Monel, Nimonic, Invar.

Limitation :

- * They are costly compared to other Alloys
- * more alloy content can cause more distortion within Material.

Application

bike muffler, Turbine blades

Noble Metals

Metal which posses Ideal behaviour are called Noble metals

5 (c)

$$h = d$$

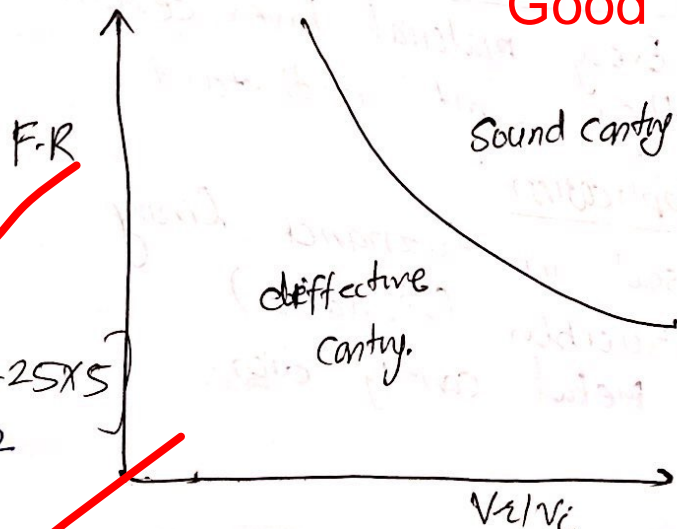
$$25 \times 25 \times 5 \text{ cm}^3$$

$$a = 0.1, b = 0.03, c = 1$$

$$F.R = \frac{(A/V)_{\text{casting}}}{(A/V)_n}$$

For Casting

$$A = 2[25 \times 25 + 25 \times 5 + 25 \times 5] \\ = 1750 \text{ cm}^2$$



$$V = 25 \times 25 \times 5 = 3125 \text{ cm}^3$$

$$(A/V)_c = \frac{1750}{3125} = \frac{14}{25}$$

$$A = \pi d \cdot h + \frac{\pi}{4} d^2$$

$$= \pi d^2 + \frac{\pi}{4} d^2$$

$$= \frac{5\pi}{4} d^2$$

$$V = \frac{\pi}{4} d^2 \cdot h = \frac{\pi}{4} d^3$$

$$\frac{A}{V} = \frac{\frac{5\pi}{4} d^2}{\frac{\pi}{4} d^3} = \frac{5}{d}$$

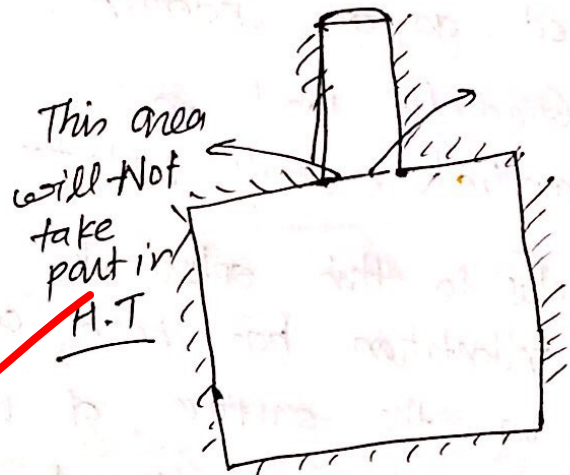
$$X = F.R = \frac{\frac{14}{25}}{\frac{5}{d}} = \frac{14d}{125}$$

$$\frac{V_n}{V_c} = \frac{\frac{\pi}{4} d^3}{3125} = \frac{\pi d^3}{12500}$$

$$X = \frac{a}{y-b} + c$$

$$\frac{14d}{125} = \frac{0.1}{\frac{\pi d^3}{12500} - 0.03} + 1$$

$$d = 11.478 \text{ cm} = h$$



Q-5 (e)

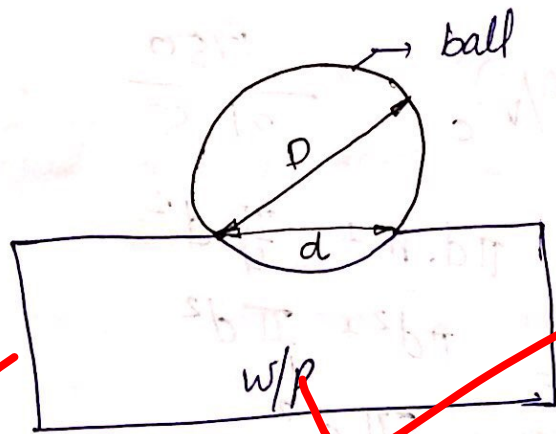
Brinell Hardness Test :

→ It consists of a ball used as an indenter.

→ Gradually load is applied on ball indenter.

→ due to this spherical indentation has been occurred on the surface of W.P.

→ by measuring the diameter of indentation BHN No is calculated.



P → force applied on indenter (kgf)

D → diam. of ball (2mm, 5mm, 10mm)

d → indented diameter.

t → time of application of load. (20-30 sec)

$$BHN = \frac{P}{\frac{\pi D}{2} \left[D - \sqrt{D^2 - d^2} \right]}$$

$$D = 10mm, \quad d = 1.62mm.$$

$$P = 500 \text{ kgf}$$

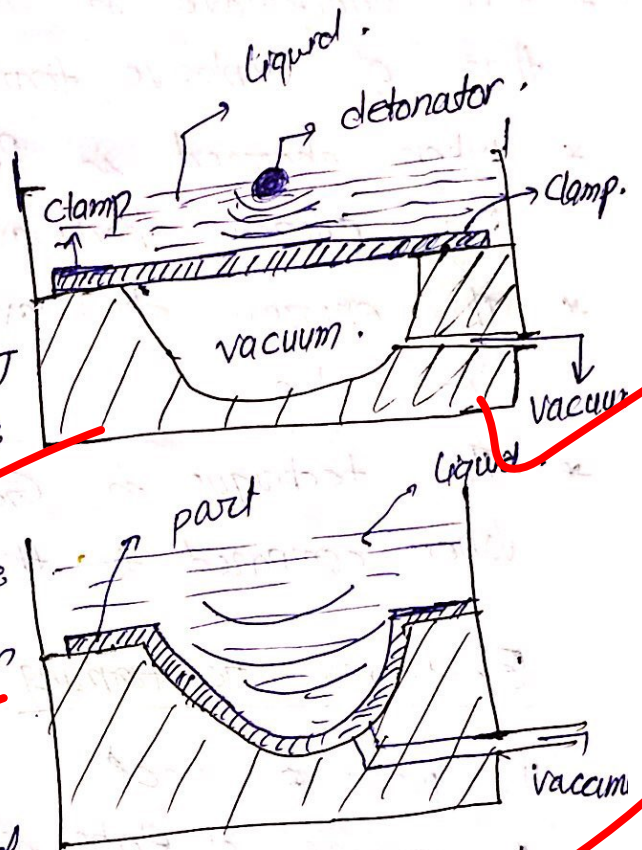
$$BHN = \frac{500}{\frac{\pi \times 10}{2} \left[10 - \sqrt{10^2 - 1.62^2} \right]}$$

$$BHN = 240.97 \text{ HB}$$

6(a)

① Explosive forming.

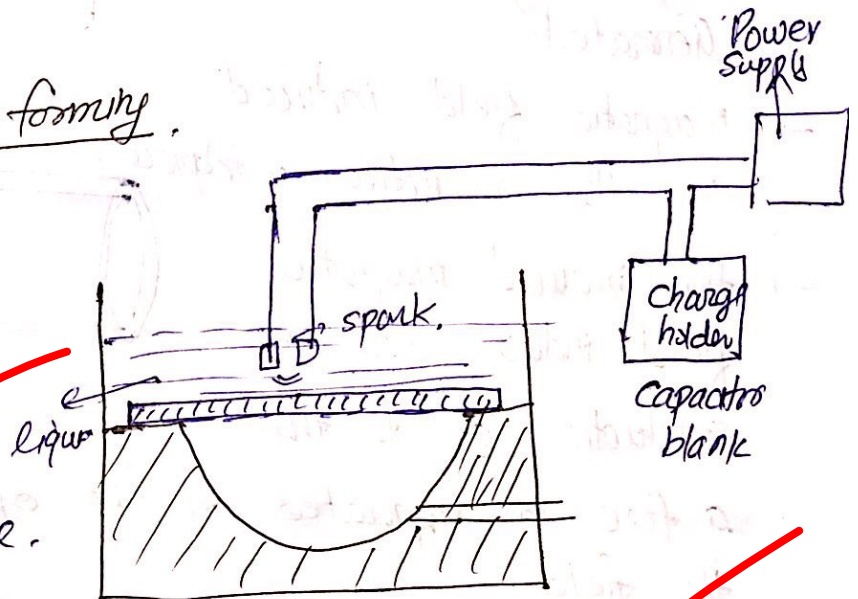
- * Shockwave is Generated in a water medium by explosive
- * with the use of ~~EA~~ TNT or dynamite this explosive wave is Generated.
- * this high energy shock wave force the work piece to form into die.



- * vacuum pump for provided to ease of forming can be done.
- * This Technique is used for thick sections.
- * these parts are Generally used in Aircrafts.

② Electrohydraulic forming.

- * In Electrohydraulic forming the charge is Generated b/w the electrodes
- * due to this charge.



Please see solution for better figures

high energy shock wave is produced.

* this shockwave is Generally consist ten power than that of Explosive forming

* When charged is Released from the charge blank High energy shockwave is Generated.

* This energy shockwave force workpiece to form into die

* This technique is Generally used for small parts when compared to that of explosive forming.

Electromagnetic forming :-

- this process is used the principle of electro. Tube Magnetic force

→ Current is passed through coil. due to this Magnetic field is Generated

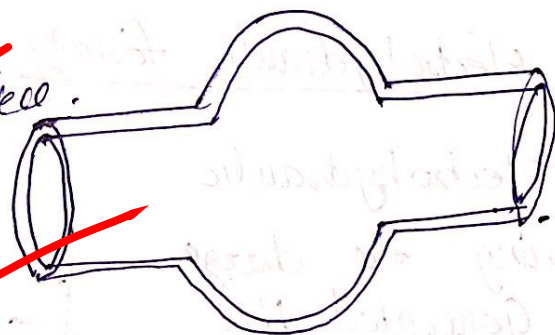
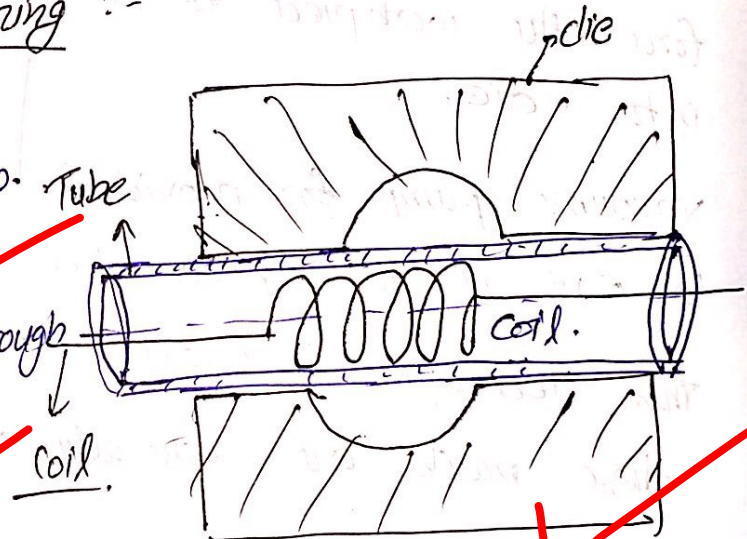
→ Magnetic field induced in the conductive workpiece.

→ this induced magnetic field induce current on conductor. due to this

a force is Generated in the opposite direction of the field

* this force lead to formation of the w/p

* Material (w/p) should be conductive for Electromagnetic forming.



Q-6B

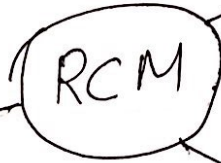
Reliability centred Maintenance

→ Reliability Centred Maintenance is used to determine the requirement of maintenance of any physical system.

→ this maintenance is based on preventive maintenance.

Predictive Maintenance
(25-40%)

Preventive Maintenance.
(40-55%)



Reactive @

Break down Maintenance
10%

① Preventive Maintenance

- Preventive maintenance consist of Routine maintenance or scheduled maintenance.
- Maintenance is done after fixed period of time
- It may sometime leads to occur unneeded Maintenance

→ for a physical system in Reliability centred Maintenance about 40-55% of the components consist of this type of Maintenance.

② Predictive maintenance

- the life of certain physical equipment is predicted and maintenance is done based on that.
- It is having less cost, since failure is predicted means no extra unneeded maintenance are required.
- this is done for critical component
- It is done 25-40% of physical system in RCM.

Reactive or Breakdown Maintenance

- Reactive ~~or~~ breakdown maintenance is done for Non critical parts in physical systems.
- If a this type of maintenance ~~does~~ the component is used until it gets failure.
- After the failure it is replaced by the new one.
- In RCM only ($<10\%$) parts is maintained by this maintenance.

Primary principal missing?

RCM Application

Preventive	Predictive	Reactive
<ul style="list-style-type: none">- done for equipment subjected to Gradual wear.→ done for the system whose failure is pattern is known→ No catastrophic failure.	<ul style="list-style-type: none">→ Equipment with Random failure→ Critical equipment→ there are not subjected to wear→ Some time they can can have catastrophic failure.	<ul style="list-style-type: none">→ done for very small No of product→ Non critical product.→ Equipment are unlikely to fail→ small parts

Advantages

Please refer solution

- It is one of most efficient maintenance Techniques
- It reduces the unnecessary maintenance
- Increase the reliability of physical system
- Minimizing complete checkup time.

6⑥

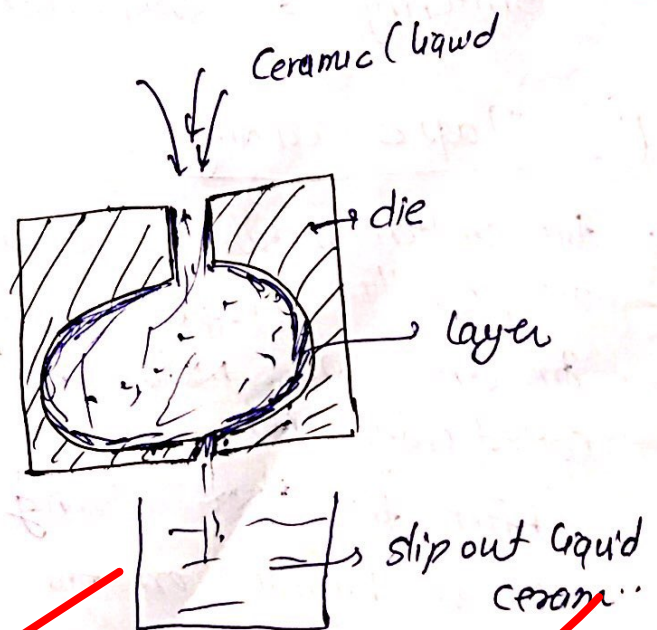
13

① Sintering :

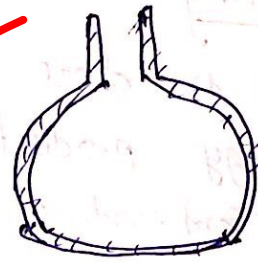
- Sintering is done after the compaction of the powder metallurgy product.
- the Temperature of the compacted powder metallurgy product is increased upto $\frac{3}{4}$ times ~~of~~ its melting Temperature.
- due to this particles fuse together & diffusion is taken place.
- Recrystallization occurs and grain growth is also take place.
- After the sintering approximately 90-95% of density is achieved
- strength increase, hardness increases, brittleness decrease
- porosity ~~xxxx~~ decrease & Toughness increase of the product.

② Slip casting :

- This Technique is used for making complex shape of pottery.
- Liquid ceramic added to the die & it flow ~~layer~~ & slip over the die & a layer is produced.



extra fluid is gone above from below opening
 & this layer is now taken
 out & used on a end
 product.



End product

③ Hot isostatic Pressing

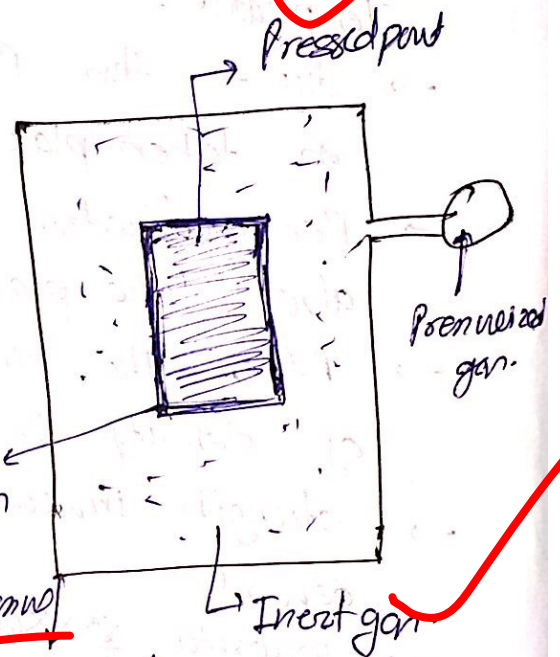
~~the ceramic part powder~~
 sintered part

→ the metal is kept under
 steel can

→ high Temp & pressure in
 applied

→ Inert gas (Eg. Argon) apply pressure
 on can

→ Sintering & compaction is done ^{heated} ^{Chamber} simultaneously.



④ Tape casting

- the molten metal is carried
 away by the Tape carrier

→ In drier zone, ~~metal~~ ceramic
 cooled using Air

* After the ~~the~~ drying
 it is bundled on the
 Roller so it can be used.

