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SOIL MECHANICS

CIVIL ENGINEERING

Date of Test : 22/07/2024

ANSWER KEY >

1. (a)	7. (d)	13. (c)	19. (c)	25. (a)
2. (c)	8. (c)	14. (d)	20. (b)	26. (d)
3. (a)	9. (c)	15. (a)	21. (a)	27. (c)
4. (b)	10. (c)	16. (a)	22. (a)	28. (c)
5. (d)	11. (d)	17. (c)	23. (d)	29. (b)
6. (a)	12. (b)	18. (d)	24. (c)	30. (a)

DETAILED EXPLANATIONS

1. (a)

Equivalent permeability, $k_{eq} = \sqrt{k_x \times k_z} = \sqrt{32 \times 8} = 16$ units

2. (c)

3. (a)

4. (b)

$$\text{Area ratio, } A_r = \frac{D_0^2 - D_i^2}{D_i^2} = \frac{50^2 - 40^2}{40^2} = 0.5625 \text{ or } 56.25\% \simeq 56\%$$

5. (d)

$$\begin{aligned} \frac{\Delta H}{H} &= \frac{\Delta e}{1 + e_o} \\ \Rightarrow \frac{26 - 24}{26} &= \frac{\Delta e}{1 + 1.22} \\ \Rightarrow \Delta e &= 0.171 \\ \Rightarrow e_i - e_f &= \Delta e \\ \Rightarrow e_f &= 1.22 - 0.171 = 1.05 \end{aligned}$$

6. (a)

$$\text{Toughness index, } I_t = \frac{I_p}{I_f} = \frac{4 \times I_f}{I_f} = 4$$

7. (d)

The effect of overburden pressure on SPT value may be approximated by the equation.

$$N = N' \left(\frac{350}{\bar{\sigma} + 70} \right)$$

$\bar{\sigma}$ = Effective overburden pressure at test level

$$= 18 \times 6 = 108 \text{ kN/m}^2 \neq 280 \text{ kN/m}^2 \text{ (OK)}$$

$$\therefore N = 28 \times \left(\frac{350}{108 + 70} \right) = 55$$

8. (c)

$$B = \frac{\Delta U_3}{\Delta \sigma_3} = \frac{0.19 - 0.09}{0.3 - 0.1} = \frac{0.1}{0.2} = 0.5$$

9. (c)

As per Taylor's method,

$$\text{Stability number, } S_n = \frac{C}{F_C \gamma H}$$

$$\Rightarrow S_n = \frac{C}{\gamma H_C} \quad (\because F_C = 1 \text{ for critical height})$$

$$\begin{aligned} \Rightarrow H_C &= \frac{C}{\gamma S_n} \\ &= \frac{30}{24 \times 0.05} = 25 \text{ m} \end{aligned}$$

10. (c)

Tap water contains a considerable amount of air. During permeability test, this air gets struck and remains trapped between sand grains thereby lowering the permeability.

11. (d)

$$\text{Factor of safety } F = \left(1 - \frac{\gamma_w h}{\gamma_{avg} z} \right) \frac{\tan \phi}{\tan \beta}$$

$$\gamma_{avg} = \frac{20 \times 5 + 15 \times 5}{10} = 17.5 \text{ kN/m}^3$$

$$\therefore F = \left(1 - \frac{10 \times 5}{17.5 \times 10} \right) \times \frac{\tan 45^\circ}{\tan 30^\circ} = \frac{5\sqrt{3}}{7} = 1.24$$

12. (b)

$$\begin{aligned} I_D &= \frac{e_{max} - e}{e_{max} - e_{min}} \times 100 = \frac{0.75 - 0.5}{0.75 - 0.25} \times 100 \\ &= 50\% \end{aligned}$$

I_D	Classification
<15	Very loose
15 – 35	Loose
35 – 65	Medium dense
65 – 85	Dense
>85	Very dense

13. (c)

Shrinkage limit,

$$\begin{aligned} W_s &= w_1 - \Delta w \\ &= w_1 - \frac{\Delta V \cdot \rho_w}{M_s} \\ &= \frac{M_1 - M_d}{M_d} - \frac{(V_1 - V_d) \rho_w}{M_d} \\ &= \frac{55.4 - 39.8}{39.8} - \frac{(29.2 - 21.1) \times 1}{39.8} \\ &= 0.39 - 0.20 = 0.19 = 19\% \end{aligned}$$

14. (d)

$$\text{Weight of dry soil} = 450 - 9 = 441 \text{ gm}$$

$$\text{Volume of paraffin} = \frac{9}{0.9} = 10 \text{ cc}$$

$$\text{Volume of soil} = 295 - 10 = 285 \text{ cc}$$

$$\text{Dry density, } \gamma_d = \frac{441}{285} = 1.547 \text{ gm/cc}$$

$$\text{Also, } \gamma_d = \frac{G\gamma_w}{1+e} = \frac{2.65 \times 1}{1+e} = 1.547$$

$$\Rightarrow e = 0.713$$

15. (a)

16. (a)

Adhesion factor, $a = 0.5$.

Let L_1 and L_2 be the depths of embedment of pile in top both layers, respectively. Then,

$$Q_a = \frac{Q_u}{\text{FOS}}$$

$$\Rightarrow Q_u = Q_a \times \text{FOS} = 380 \times 2 = 760 \text{ kN}$$

$$\text{Also, } Q_u = \alpha(C_{u1})\pi dL_1 + \alpha(C_{u2})\pi dL_2 + (C_{u1})N_c \frac{\pi d^2}{4}$$

$$760 = 0.5 \times 45 \times \pi \times 0.4 \times 5 + 0.5 \times 100 \times \pi \times 0.4 \times L_2 + 100 \times 9 \times \frac{\pi \times 0.4^2}{4}$$

$$760 = 254.5 + 62.8 \times L_2$$

$$L_2 = \frac{760 - 254.8}{62.8} = 8 \text{ m}$$

Therefore, the length of the pile is as given below,

$$L_1 + L_2 = 5 + 8 = 13 \text{ m}$$

17. (c)

$$K_{P1} = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ} = 3$$

$$K_{P2} = \frac{1 + \sin 15^\circ}{1 - \sin 15^\circ} = 1.698$$

$$\text{At } h = 0 \text{ m, } p_1 = K_{P1}q = 3 \times 20 = 60 \text{ kN/m}^2$$

$$\text{At } h = 4 \text{ m, in top layer } p_2 = K_{P1}(q + \gamma_1 h) = 3(20 + 4 \times 16) = 252 \text{ kN/m}^2$$

At $h = 4$ m, in bottom layer,

$$\begin{aligned} p_3 &= K_{P2}(q + \gamma_1 h) + 2C\sqrt{K_{P2}} \\ &= 1.698(20 + 16 \times 4) + 2 \times 15\sqrt{1.698} \\ &= 181.72 \text{ kN/m}^2 \end{aligned}$$

At $h = 8$ m i.e., at point A,

$$\begin{aligned} p_4 &= K_{P2}(q + \gamma_1 \times 4 + \gamma_2 \times 4) + 2C\sqrt{K_{P2}} \\ &= 1.698(20 + 16 \times 4 + 18 \times 4) + 2 \times 15\sqrt{1.698} \\ &= 303.98 \text{ kN/m}^2 \end{aligned}$$

18. (d)

$$\sigma_z = \frac{3Q}{2\pi z^2} \left(\frac{1}{1 + \left(\frac{r}{z}\right)^2} \right)^{5/2}$$

For stress vertically below the load, $r = 0$

$$\therefore \sigma_z = \frac{3Q}{2\pi z^2}$$

$$\therefore \frac{\sigma_{2m}}{\sigma_{5m}} = \frac{\frac{1}{2^2}}{\frac{1}{5^2}} = 6.25$$

19. (c)

For strip footing,

$$\begin{aligned} q_u &= cN_C + qN_q + 0.5 \gamma BN_\gamma \\ &= 50 \times 8 + 20 \times 1 \times 3 + 0.5 \times 20 \times 2 \times 2 \\ &= 500 \text{ kN/m}^2 \end{aligned}$$

$$\therefore q_{nu} = q_u - \gamma D_f = 500 - 20 \times 1 = 480 \text{ kN/m}^2$$

\(\therefore\) Safe bearing capacity,

$$\begin{aligned} q_s &= q_{ns} + \gamma D_f \\ &= \frac{480}{3} + 20 \times 1 = 160 + 20 \\ &= 180 \text{ kN/m}^2 \end{aligned}$$

$$\therefore \text{Total safe load} = 180 \times 2 \times 10 = 3600 \text{ kN}$$

20. (b)

$$\begin{aligned} \text{Ultimate pull} &= \alpha \bar{C} A_s + W_p \\ &= 0.5 \times 120 \times (\pi \times 0.5 \times 12) + \frac{\pi}{4} \times 0.5^2 \times 12 \times 25 \\ &= 1189.88 \text{ kN} \end{aligned}$$

21. (a)

Let k , $10k$ and $20k$ be the permeabilities of first, second and third soil layers respectively.Let t , $t/2$ and $2t$ be the thicknesses of the first, second and third soil layers respectively.

$$\begin{aligned} \therefore k_h &= \frac{k_1 z_1 + k_2 z_2 + k_3 z_3}{z_1 + z_2 + z_3} \\ &= \frac{kt + 10k \cdot \left(\frac{t}{2}\right) + 20k \cdot 2t}{t + \frac{t}{2} + 2t} \\ &= \frac{kt(1 + 5 + 40)}{t(1 + 0.5 + 2)} = \frac{46k}{3.5} = 13.143k \end{aligned}$$

Also,

$$k_v = \frac{z_1 + z_2 + z_3}{\left(\frac{z_1}{k_1}\right) + \left(\frac{z_2}{k_2}\right) + \left(\frac{z_3}{k_3}\right)}$$

$$= \frac{t + \frac{t}{2} + 2t}{\left(\frac{t}{k}\right) + \left(\frac{t/2}{10k}\right) + \left(\frac{2t}{20k}\right)}$$

$$= \frac{t(1 + 0.5 + 2)}{\frac{t}{k}\left(1 + \frac{1}{20} + \frac{1}{10}\right)} = 3.043k$$

$$\therefore \frac{k_h}{k_v} = \frac{13.143k}{3.043k} = 4.32$$

22. (a)

Load carrying capacity of each pile = $C_u N_C A_b + \alpha \bar{C}_u A_s$

For stiff clay, $C_u = \frac{Q_{undisturbed}}{2} = \frac{250}{2} = 125 \text{ kPa}$

For medium stiff clay, $\bar{C}_u = \frac{200}{2} = 100 \text{ kPa}$

Load carrying capacity of each pile

$$= 9 \times 125 \times \frac{\pi}{4} \times (0.3)^2 + 0.6 \times 100 \times \pi \times (0.3) \times 20$$

$$= 79.52 + 1130.97$$

$$= 1210.49 \text{ kN}$$

$$\simeq 1210.5 \text{ kN}$$

$$\therefore \text{Load carrying capacity of 9 piles} = 9 \times (\text{load carrying capacity of one pile})$$

$$= 10894.5 \text{ kN}$$

Ultimate load carrying capacity of pile group = $3 \times 3800 = 11400 \text{ kN}$

$$\text{Efficiency of pile group} = \frac{11400}{10894.5} \times 100 = 104.64\%$$

23. (d)

Given, seepage head, $h = 1.68 \text{ m}$

Factor of safety, $F = 1.5$

Specific gravity, $G = 2.67$

Porosity, $n = 40\%$

Void ratio, $e = \frac{n}{1-n} = \frac{0.40}{1-0.40} = 0.67$

Critical hydraulic gradient,

$$i_c = \frac{G-1}{1+e} = \frac{2.67-1}{1+0.67} = 1$$

Actual exit hydraulic gradient,

$$i = \frac{i_c}{F} = \frac{1}{1.5} = 0.67$$

But $i = \frac{h}{L}$

$$\Rightarrow L = \frac{h}{i} = \frac{1.68}{0.67} = 2.51 \text{ m}$$

$$\begin{aligned} \therefore \text{Depth of coarse sand required} &= L - 1.5 \\ &= 2.51 - 1.5 = 1.01 \text{ m} \end{aligned}$$

24. (c)

Since it is a case of double drainage and thus, $d = \frac{4}{2} = 2 \text{ m} = 200 \text{ cm}$

For,

$$\begin{aligned} U &= 70\% \text{ of total settlement} \\ T_v &= -0.9332 \log_{10} (1 - U) - 0.0851 \\ &= -0.9332 \log_{10} (1 - 0.7) - 0.0851 \\ &= 0.403 \end{aligned}$$

$$C_v = \frac{T_v d^2}{t}$$

$$\Rightarrow t = \frac{0.403 \times (200)^2}{0.03}$$

$$\Rightarrow t = 537.33 \times 10^3 \text{ min}$$

$$\Rightarrow t = 373 \text{ days}$$

25. (a)

The increased stress, $\bar{\sigma}_0 + \Delta\bar{\sigma}$ is equal to $70 + 80 = 150 \text{ kN/m}^2$. This is greater than $\bar{\sigma}_c = 120 \text{ kN/m}^2$. Thus soil is normally consolidated.

$$\begin{aligned} \therefore s_c &= C_r \frac{H_0}{1 + e_0} \log \frac{\bar{\sigma}_c}{\bar{\sigma}} + C_c \frac{H_0}{1 + e_0} \log_{10} \frac{\bar{\sigma}_0 + \Delta\bar{\sigma}}{\bar{\sigma}_c} \\ s_c &= 0.03 \frac{5 \times 10^3}{1 + 0.90} \log \frac{120}{70} + 0.27 \frac{5 \times 10^3}{1 + 0.90} \log_{10} \frac{150}{120} \\ &= 18.48 + 68.86 = 87.34 \text{ mm} \end{aligned}$$

26. (d)

$$\begin{aligned} \sigma_z &= \frac{2q'}{\pi z} \left[\frac{1}{1 + \left(\frac{x}{z}\right)^2} \right]^2 \\ &= \frac{2 \times 120}{\pi \times 3.5} \left[\frac{1}{1 + \left(\frac{2}{3.5}\right)^2} \right]^2 \\ &= 12.40 \text{ kN/m}^2 \end{aligned}$$

27. (c)

Given: $B_f = 1.5 \text{ m}, B_p = 0.3 \text{ m}, S_p = 18 \text{ mm}, S_f = ?$

$$\begin{aligned} \therefore \quad \frac{S_f}{S_p} &= \left[\frac{B_f (B_p + 0.3)}{B_p (B_f + 0.3)} \right]^2 \\ \Rightarrow \quad \frac{S_f}{18} &= \left[\frac{1.5 \times (0.3 + 0.3)}{0.3 \times (1.5 + 0.3)} \right]^2 \\ \Rightarrow \quad S_f &= 50 \text{ mm} \end{aligned}$$

28. (c)

Given, square footing, $B = 1.8 \text{ m}$

$$\gamma = 16 \text{ kN/m}^3, C = 0, \phi = 30^\circ$$

$$D_f = 0.8 \text{ m}$$

$$N_C = 30.14, N_q = 18.4 \text{ and } N_\gamma = 15.1$$

We know for square footing,

$$\begin{aligned} q_u &= 1.3CN_C + qN_q + 0.4\gamma BN_\gamma \\ &= 0 + 16 \times 0.8 \times 18.4 + 0.4 \times 16 \times 1.8 \times 15.1 \quad [\because C = 0] \\ &= 409.472 \text{ kN/m}^2 \end{aligned}$$

So, the ultimate load that can be carried by the footing

$$\begin{aligned} &= q_u \times \text{area} \\ &= 409.472 \times 1.8 \times 1.8 \\ &= 1326.69 \text{ kN} \end{aligned}$$

29. (b)

For a raft on clayey soil, for $\frac{D_f}{B} = \frac{5}{10} = 0.5 < 2.5$

$$\begin{aligned} q_{nu} &= 5 \left(1 + 0.2 \frac{D_f}{B} \right) \left(1 + 0.2 \frac{B}{L} \right) C_u \\ &= 5 \times \left(1 + 0.2 \times \frac{5}{10} \right) \left(1 + 0.2 \times \frac{10}{10} \right) \times 40 \\ &= 264 \text{ kN/m}^2 \end{aligned}$$

$$\therefore \quad q_{ns} = \frac{q_{nu}}{F} = \frac{264}{2.5} = 105.6 \text{ kN/m}^2$$

30. (a)

The criteria for determining the design load is that it should be taken as minimum of the following:

(i) Half the load at which settlement is 10% of the pile diameter.

$$10\% \text{ of pile diameter} = 30 \text{ mm}$$

$$\text{Load at 30 mm settlement} = 140 + \frac{160 - 140}{34 - 27} (30 - 27)$$

$$= 148.57 \text{ kN}$$

$$\text{Half of this load} = 74.29 \text{ kN}$$

(ii) Two third of the load at which pile settlement is 12 mm.

$$\begin{aligned}\text{Load corresponding to 12 mm settlement} &= 60 + \frac{80 - 60}{13 - 10}(12 - 10) \\ &= 73.33 \text{ kN}\end{aligned}$$

$$\therefore \frac{2}{3} \times 73.33 = 48.89 \text{ kN}$$

$$\therefore \text{Design load on pile} = 48.89 \text{ kN}$$

