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# Synchronous Machine

ELECTRICAL ENGINEERING

Date of Test : 26/08/2024

## ANSWER KEY >

- |        |         |         |         |         |
|--------|---------|---------|---------|---------|
| 1. (c) | 7. (b)  | 13. (d) | 19. (b) | 25. (a) |
| 2. (d) | 8. (b)  | 14. (a) | 20. (a) | 26. (c) |
| 3. (c) | 9. (d)  | 15. (b) | 21. (a) | 27. (a) |
| 4. (a) | 10. (a) | 16. (a) | 22. (b) | 28. (a) |
| 5. (b) | 11. (b) | 17. (b) | 23. (a) | 29. (c) |
| 6. (a) | 12. (b) | 18. (b) | 24. (b) | 30. (c) |

**DETAILED EXPLANATIONS**

1. (c)

Frequency,  $f = \frac{PN}{120} = \frac{4 \times 1500}{120} = 50 \text{ Hz}$

Total number of stator conductor = Number of slots  $\times$  conductor per slot  
 $= 80 \times 6 = 480$

Stator conductor per phase,  $Z_p = \frac{480}{3} = 160$

Winding factor,  $k_w = 0.98$

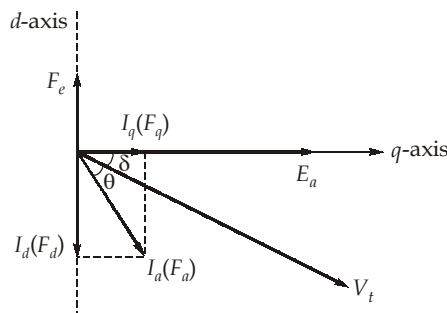
Generated voltage per phase,  $E_p = 2.22 \times k_w \times f \times \phi \times Z_p$   
 $= 2.22 \times 0.98 \times 50 \times 0.04 \times 160$   
 $= 696.19 \text{ V}$

Generated line voltage,  $E_L = \sqrt{3}E_p = 1205.83 \text{ V}$

2. (d)

Both statements are correct for starting of synchronous motor. It is recommended to connect an external resistance 7 to 10 times the field resistance to avoid insulation damage.

3. (c)



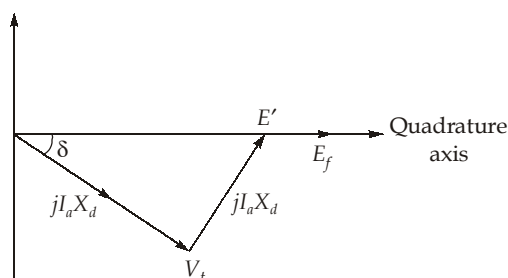
Thus by phasor we can conclude that

- $F_e$  leads  $F_a$  by angle  $(90 + \theta + \delta)$
- $F_q$  leads  $F_a$  by angle  $(\delta + \theta)$
- $F_d$  lags  $F_a$  by angle  $(90 - (\delta + \theta))$
- $F_e$  leads  $V_t$  by angle  $(90 + \delta)$ .

4. (a)

Power angle is the angle between  $E_f$  and  $V_t$

As  $E'$  and  $E_f$  are in phase, angle between  $E'$  and  $V_t$  is also equal to power angle,  $\delta$



$$\begin{aligned}
 I_a &= 1 \angle 0^\circ \text{ p.u.} \\
 \text{Quadrature axis function, } X_q &= 1.2 \text{ p.u.} \\
 E' &= V_t + jI_a X_q \\
 &= 1 + j1 \times 1.2 \\
 &= 1.562 \angle 50.19^\circ \text{ A} \\
 \delta &= 50.194^\circ
 \end{aligned}$$

5. (b)

Emf equation synchronous motor is given as

$$\vec{E} = \vec{V}_t - \vec{I}_a \vec{Z}_s$$

Given that,  $\vec{V}_t = 1 \angle 0^\circ \text{ p.u.}$ ,  $\vec{I}_a = 1 \angle 90^\circ \text{ p.u.}$ ,  $\vec{Z}_s = 0.5 \angle 90^\circ \text{ p.u.}$ 

$$\begin{aligned}
 \vec{E} &= 1 \angle 0^\circ - (1 \angle 90^\circ) \times (0.5 \angle 90^\circ) \\
 &= 1 - 0.5 \angle 180^\circ
 \end{aligned}$$

$$\vec{E} = 1 + 0.5 \angle 0^\circ = 1.5 \text{ p.u.}$$

6. (a)

Given that,

$$V_t = 1.0 \text{ pu, } I_a = 1.0 \text{ pu, } 0.8 \text{ pf lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.9^\circ$$

$$x_d = 0.8 \text{ pu, } x_q = 0.5 \text{ pu}$$

$$\tan \psi = \frac{V_t \sin \phi + I_a x_q}{V_t \cos \phi + I_a r_a} = \frac{1 \times 0.6 + 1 \times 0.5}{1 \times 0.8 + 0} = \frac{11}{8}$$

$$\psi = \tan^{-1} \left( \frac{11}{8} \right) = 53.97^\circ \simeq 54^\circ$$

Power angle,

$$\delta = \psi - \phi = 54^\circ - 36.9^\circ = 17.1^\circ$$

7. (b)

3rd harmonic voltage in line of Y-connected generator is neutralized. So,

$$V_{L, \text{peak}} = \sqrt{6} V_{ph(\text{rms})} = 231 \sqrt{6} = 565.83 \text{ volts}$$

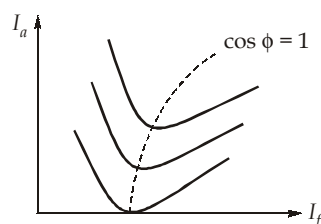
8. (b)

As we know,

$$I_{sc} \propto \frac{E_f}{X_s} \propto \frac{I_f \times f}{f} \quad (\because I_{sc} \propto I_f)$$

$$I_{sc2} = I_{sc1} \times \frac{I_{f2}}{I_{f1}} = 20 \times \frac{1.5}{1} = 30 \text{ A}$$

9. (d)



10. (a)

By large air-gap length, the reluctance of the air-gap increases, so that the leakage flux decreases hence leakage reactance decreases. So, flux distribution will improved (more sinusoidal).  
 Because of large air-gap length, armature reaction decreases. So, the voltage regulation will be less.

11. (b)

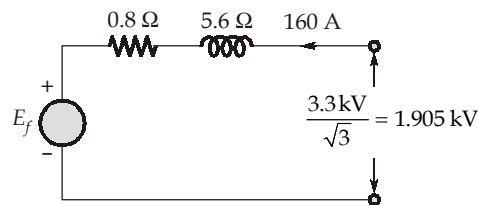
Given,

$$\text{Synchronous impedance, } X_s = 0.8 + j5.6 = 5.656 \angle 81.86^\circ \Omega$$

$$\text{Per phase voltage, } V_p = \frac{\text{Rated line voltage}}{\sqrt{3}} = \frac{3.3 \text{ kV}}{\sqrt{3}} = 1.905 \text{ kV}$$

$$\begin{aligned} \vec{E}_{f \text{ phase}} &= 1.905 - 5.656 \angle 81.86^\circ \times 0.16 \angle -36.9^\circ \\ &= 1.905 - 0.90496 \angle 44.96^\circ \\ &= 1.417 \angle -26.82^\circ \text{ kV or } 2.454 \text{ kV (line)} \end{aligned}$$

We can draw per phase diagram,



Mechanical power developed,

$$\begin{aligned} P_{\text{mech (dev)}} &= 3E_f I_p \cos(\phi + \delta) \\ &= 3 \times 1.417 \times 160 \cos(-36.9^\circ + 26.82^\circ) \\ &= 669.66 \text{ kW} \end{aligned}$$

$$\text{Shaft power output} = 669.66 - 30 = 639.66 \text{ kW}$$

$$\text{Power input} = \sqrt{3} \times 3.3 \times 160 \times 0.8 = 731.5 \text{ kW}$$

$$\eta = \frac{\text{Shaft power output}}{\text{Total input}} = \frac{639.66}{731.5} \times 100 = 87.44\%$$

**Alternate Solution :**

$$\begin{aligned} \text{Power input} &= \sqrt{3} \times 3.3 \times 160 \times 0.8 \\ &= 731618.26 = 731.618 \text{ kW} \end{aligned}$$

$$\begin{aligned} \text{Copper loss} &= 3I_a^2 R = 3 \times (160)^2 \times R \\ &= 61.44 \text{ kW} \end{aligned}$$

$$\text{Power output} = 640.178 \text{ kW}$$

$$\eta = \frac{640.178}{731.618} \times 100 = 87.44\%$$

12. (b)

We know, terminal voltage,  $V_t = 1 \text{ p.u.}$

$$I_a = 1 \text{ p.u. } 0.8 \text{ p.f. lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.86^\circ$$

Also,

$$X_d = 0.8 \text{ p.u.}$$

$$X_q = 0.6 \text{ p.u.}$$

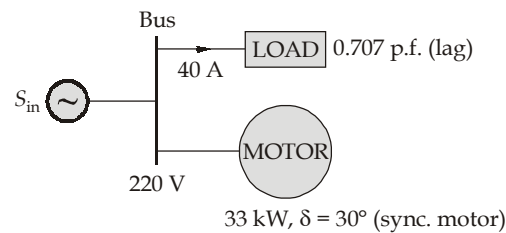
$$\tan \psi = \frac{V_t \sin \phi + I_a X_q}{V_t \cos \phi + I_a X_d} = \frac{1 \times 0.6 + 0.6 \times 1}{1 \times 0.8 + 0} = 1.5$$

$$\psi = \tan^{-1}(1.5) = 56.309^\circ$$

$$\begin{aligned} \text{Power angle, } \delta_1 &= \psi - \phi = 56.309^\circ - 36.86^\circ \\ &= 19.449^\circ \end{aligned}$$

$$\begin{aligned} E_f &= V_t \cos \delta + I_d X_d + I_a r_a = V_t \cos \delta + (I_a \sin \psi) X_d \\ &= 1 \times \cos 19.449 + (1 \times \sin 56.309) \times 0.8 \\ &= 0.9429 + 0.66563 \\ &= 1.60853 \text{ p.u.} \end{aligned}$$

13. (d)



$$\begin{aligned} \vec{S}_{\text{Load}} &= \sqrt{3} \times 220 \times 40 \times \angle \cos^{-1}(0.707) \\ &= 15.242 \angle 45^\circ \text{ kVA} \\ &= (10.78 + j10.78) \text{ kVA} \end{aligned}$$

$$\vec{S}_{\text{motor}} = P_{\text{motor}} + jQ_{\text{motor}}$$

$$P_{\text{motor}} = 33 \text{ kW}$$

Using

$$P_{\text{motor}} = \frac{E_f \times 220}{1.27} \sin 30^\circ = 33 \times 10^3$$

$$E_f = (\sqrt{3} \times 220) = 381 \text{ V (L-L)}$$

$$Q_{\text{motor}} = \frac{220}{1.27} (-381 \cos 30^\circ + 220) = -19.047 \text{ kVAR (leading)}$$

$$\vec{S}_{\text{motor}} = (33 - j19.047) \text{ kVA}$$

$$\begin{aligned} \vec{S}_{\text{in}} &= \vec{S}_{\text{motor}} + \vec{S}_{\text{Load}} \\ &= (33 + 10.48) + j(10.78 - 19.047) \\ &= 43.78 - j8.267 \\ &= 45.55 \angle -10.70^\circ \text{ kVA} \end{aligned}$$

$$\text{Power factor} = \cos(-10.70) = 0.9826 \text{ leading}$$

14. (a)

At maximum power conditions,

$$\delta = \theta_s$$

$$\delta = \cos^{-1} \left[ \frac{0.4}{8} \right] = \cos^{-1}[0.05] = 87.134^\circ$$

$$E_f \angle \delta = V_t \angle 0 + I_a Z_s$$

$$E_f \text{ (per phase)} = \frac{12000}{\sqrt{3}} = 6928.20 \text{ V}$$

$$V_t \text{ (per phase)} = \frac{11000}{\sqrt{3}} = 6350.852 \text{ V}$$

$$E_f \cos \delta + j E_f \sin \delta = V_t + I_a \angle -\phi \cdot Z_s \angle \theta_s$$

$$= V_t + I_a Z_s \angle \theta_s - \phi$$

$$E_f \cos \delta + j E_f \sin \delta = V_t + I_a Z_s \cos(\theta_s - \phi) + j I_a Z_s \sin(\theta_s - \phi)$$

Comparing real and imaginary part,

$$E_f \cos \delta = V_t + I_a Z_s \cos(\theta_s - \phi)$$

$$E_f \sin \delta = I_a Z_s \sin(\theta_s - \phi)$$

$$6928.20 \times \cos 87.134 = 6350.85 + 8 I_a \cos(\theta_s - \phi)$$

$$346.411 = 6350.85 + 8 I_a \cos(\theta_s - \phi)$$

$$8 I_a \cos(\theta_s - \phi) = -6004.438$$

$$I_a \cos(\theta_s - \phi) = -750.554 \quad \dots(i)$$

Also  $8 I_a \sin(\theta_s - \phi) = 6928.20 \times \sin 87.134$

$$8 I_a \sin(\theta_s - \phi) = 6919.534$$

$$I_a \sin(\theta_s - \phi) = 864.941 \quad \dots(ii)$$

By squaring and adding equation (i) and (ii),

$$I_a = 1145.187 \text{ A}$$

Using equation (i),

$$I_a \cos(\theta_s - \phi) = -750.554$$

$$\cos(\theta_s - \phi) = -0.65539$$

$$\theta_s - \phi = 130.949$$

$$87.134 - \phi = 130.949$$

$$\phi = -43.815^\circ$$

$$\cos \phi = 0.7215$$

**15. (b)**

For open circuit test,

Given,  $V_{OC} = 400 \text{ V (rms) line voltage}$

Phase voltage,  $V_{OC, ph} = \frac{400}{\sqrt{3}} = 230.94 \text{ V}$

Field current,  $I_f = 2.5 \text{ A}$

For short circuit test,  $I_{SC} = 12 \text{ A (rms, phase)}$

$$I_f = 1.08 \text{ A}$$

$$\therefore \text{Base impedance, } Z_{base} = \frac{V_{OC}}{I_{SC}} = \frac{230.94}{12} = 19.245 \Omega$$

Also, for synchronous impedance at rated voltage saturation is also considered

$$\therefore \text{SCR} = \frac{I_f \text{ for } V_{OC}}{I_f \text{ for } I_{SC}} = \frac{1}{Z_{S(\text{sat}) \text{ p.u.}}} = \frac{2.5}{1.8} = 1.3888$$

$$Z_{S(\text{sat}) \text{ p.u.}} = \frac{1}{1.3888} = 0.72 \text{ p.u.}$$

$\therefore$  Actual value of  $Z_s$  at rated voltage

$$= Z_{S(\text{sat}) \text{ p.u.}} \times Z_{base}$$

$$= 0.72 \times 19.245$$

$$= 13.85 \Omega$$

16. (a)

Since winding is double layer,

So, No. of coils = No. of slots

$$\text{No. of coils} = 36$$

Since each coil is passes 8 turns,

So total number of turns =  $36 \times 8 = 288$  turns

$$\text{Turns per phase} = \frac{\text{Total no. of turns}}{\text{No. of phases}} = \frac{288}{2} = 144 \text{ Turns/phase}$$

$$m = \frac{\text{Slot}}{\text{Pole} \times \text{Phase}} = \frac{36}{6 \times 2} = 3$$

$$\beta = \frac{180^\circ \times \text{Poles}}{\text{Slots}} = \frac{180^\circ \times 6}{36} = 30^\circ$$

$$\text{Distribution factor, } K_d = \frac{\sin\left(\frac{m\beta}{2}\right)}{m \sin\left(\frac{\beta}{2}\right)} = \frac{\sin(45^\circ)}{3 \sin(15^\circ)} = 0.91$$

$$\begin{aligned} \text{Emf per phase} &= 4.44 \phi_m f N_{ph} K_d = 4.44 \times 0.015 \times 50 \times 144 \times 0.91 \\ &= 436.36 \text{ volts/phase} \end{aligned}$$

$$E_{L(\text{rms})} = \sqrt{2} E_{\text{ph}(\text{rms})} = \sqrt{2} \times 436.36 = 617.11 \text{ volts}$$

17. (b)

$$\vec{I}_a = 1 \angle 36.86 \text{ p.u.}$$

$$\vec{V}_t = 1 \text{ p.u.}$$

$$\vec{Z}_s = j0.6 \text{ p.u.}$$

$$\begin{aligned} \vec{E}_f &= \vec{V}_t - \vec{I}_a \vec{Z}_s = 1 \angle 0 - 0.6 \angle 126.86^\circ \\ &= 1.44 \angle -19.44^\circ \text{ p.u.} \end{aligned}$$

$$\begin{aligned} \therefore E_f &= 1.44 \text{ p.u.}, \\ \delta &= -19.44^\circ \end{aligned}$$

As we know,

$$\text{Ful-load torque} = (\text{Maximum torque}) \cdot \sin \delta$$

$$\frac{\text{Maximum torque}}{\text{Full load torque}} = \frac{1}{\sin \delta} = \frac{1}{\sin 19.44} = 3.00$$

**Hint:** The ratio of two torque of a single machine can't be negative, don't put  $\delta$  to  $-\delta$ .

18. (b)

$$375 = \frac{120xf}{16} \Rightarrow f = 50 \text{ Hz}$$

$$\text{Slots per pole} = \frac{144}{16} = 9$$

Slots per pole per phase,  $m = \frac{144}{16 \times 3} = 3$

$$\beta = \frac{180^\circ}{\text{slots per pole}} = 20^\circ$$

$$k_d = \frac{\sin \frac{m\beta}{2}}{m \sin \frac{\beta}{2}} \Rightarrow k_d = \frac{0.5}{3 \times 0.174} = 0.96$$

$Z = \text{number of conductors in series per phase} = \frac{144 \times 10}{3} = 480$

$$\begin{aligned} E_{\text{line}} &= \sqrt{3} \times 4.44 f N_{ph} \phi_m k_d \\ &= \sqrt{3} \times 4.44 \times 0.96 \times 0.03 \times \frac{480}{2} \times 50 \\ &= 2657.76 \text{ V} \end{aligned}$$

19. (b)

$$P_{sy} = \frac{EV}{X_s} \cos \delta$$

where  $P_{sy}$  = symmetrical power coefficient

$$P_{sy} \propto \text{stability} \propto \text{excitation}$$

At 'Q' the excitation is more than at 'P'.

So it is more stable at Q.

20. (a)

$$Z_{s(\text{adjusted})} = \frac{V_{\text{rated}} / \sqrt{3}}{I_{sc}} \Bigg|_{\text{At } I_f \text{ corresponding to } V_{oc} = V_{\text{rated}}}$$

Rated armature current,

$$\sqrt{3} V_{\text{rated}} I_a(\text{rated}) = 10 \text{ MVA}$$

$$I_a(\text{rated}) = \frac{10 \times 10^3}{\sqrt{3} \times 13.8} = 418.4 \text{ A}$$

$$I_f(\text{rated}) = 842 \text{ A}$$

$$I_{sc} = \frac{418.4}{226} \times 842 = 1558.8 \text{ A}$$

$$Z_{s(\text{adjusted})} = \frac{13.8 \times 10^3 / \sqrt{3}}{1558.8} = 5.11 \Omega$$

$$\begin{aligned} X_{s(\text{adjusted})} &= \sqrt{Z_{s(\text{adjusted})}^2 - R_a^2} \\ &= \sqrt{5.11^2 - 0.75^2} = 5.054 \Omega \end{aligned}$$

$$X_{s(\text{pu})} = 5.054 \times \frac{10}{(13.8)^2} = 0.2654$$



21. (a)

$$Z_a = (0.5 + j2) \Omega$$

$$= 2.06 \angle 75.96^\circ \Omega; V_t = 415 \text{ V}, E_f = 500 \text{ V}$$

$$\text{Maximum developed power} = \frac{E_f V_t}{Z_s} - \frac{E_f^2}{Z_s^2} \times R_a$$

$$P_{\text{dev}} = \frac{500 \times 415}{2.06} - \left( \frac{500}{2.06} \right)^2 \times 0.5$$

$$= 71.272 \text{ kW}$$

This is per phase power.

$$\therefore \text{Shaft power output} = [3 \times 71.272 - 1] \text{ kW}$$

$$= 212.81 \text{ kW}$$

22. (b)

Given, 44 MVA, Y-connected, 3- $\phi$  salient pole synchronous generator.

It deliver a rated load at 0.8 p.f. lag,

$$V = 10.5 \text{ kV}, X_d = 1.83 \Omega$$

$$X_q = 1.21 \Omega, \text{ Y-connected}$$

$$\tan \Psi = \frac{V \sin \phi + I_a X_q}{V \cos \phi + I_a R_a}$$

$$V_{\text{ph}} = \frac{V_a}{\sqrt{3}} = 6062.17 \text{ V}$$

$$I_a = \frac{P}{\sqrt{3} V_L} = \frac{44 \times 10^6}{\sqrt{3} \times 10.5 \times 10^3} = 2419.3 \angle -36.86^\circ \text{ A}$$

$$\tan \psi = \frac{(6062.17 \times 0.6) + (2419.3 \times 1.21)}{(6062.17 \times 0.8) + (2419.3 \times 0)}$$

$$\psi = 53.546^\circ$$

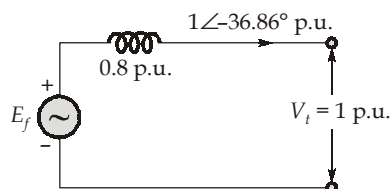
$$\psi = \delta + \phi$$

$$\delta = 53.546^\circ - 36.86^\circ$$

$$= 16.686^\circ \approx 16.69^\circ$$

23. (a)

Consider the circuit diagram drawn below:



From circuit diagram we can write,

$$\vec{E}_f = 1 + j 0.8 (1 \angle -36.86^\circ)$$

$$\vec{E}_f = 1.61 \angle 23.4^\circ \text{ p.u.}$$

Here, power angle,  $\delta = 23.4^\circ$

$$\text{Real power; } P_e = \frac{V_t E_f}{X_s} \sin \delta$$

$$\text{Synchronizing power, } \frac{dP_e}{d\delta} = \frac{V_t E_f}{X_s} \cos \delta = \frac{1 \times 1.61}{0.8} \cos(23.4^\circ)$$

$$\frac{dP_e}{d\delta} = 1.847 \text{ p.u./electrical radian}$$

$$\begin{aligned} \text{or, } \frac{dP_e}{d\delta} &= 1.847 \times 10^3 \times \frac{\pi}{180} \text{ kW/electrical degree} \\ &= 32.236 \text{ kW/electrical degree} \end{aligned}$$

$$\text{or, } 1 \text{ electrical degree} = \frac{P}{2} \text{ mechanical degree}$$

$$\text{then; } \frac{dP_e}{d\delta} = 32.236 \times 4 \text{ kW/mechanical degree}$$

$$\frac{dP_e}{d\delta} = 128.944 \text{ kW/mechanical degree}$$

24. (b)

$$\text{Power (P)} = \frac{V E_f}{X_s} \sin \delta$$

$$0.75 = \frac{1 \times 1.25}{0.7} \sin \delta$$

$$\delta = 24.83^\circ$$

Current is given by,

$$\vec{I} = \frac{\vec{E}_f - \vec{V}}{jX} = \frac{1.25 \angle 24.83^\circ - 1 \angle 0^\circ}{j0.7}$$

$$I = 0.77 \angle -14.36^\circ$$

$$\text{Phase angle, } \phi = 14.36^\circ$$

$$\text{Power factor} = \cos \phi = 0.9688 \text{ (lagging)}$$

25. (a)

$$\text{Excitation emf, } (\vec{E}_f) = \vec{V} + \vec{I}_a Z_s$$

$$\text{Armature current, } I_a = \frac{20 \times 10^3}{\sqrt{3} \times 400} = 28.87 \text{ A}$$

$$\vec{E}_f = \frac{400}{\sqrt{3}} + (28.87 \angle 36.87^\circ) \times (0.5 + j3)$$

$$\vec{E}_f = 205.85 \angle 22.25^\circ \text{ V}$$

$$\text{Voltage regulation} = \frac{|E_f| - |V|}{|V|} \times 100$$

$$= \frac{205.85 - \left(\frac{400}{\sqrt{3}}\right)}{\left(\frac{400}{\sqrt{3}}\right)} \times 100 = -10.86\%$$

26. (c)

Power angle can be calculated as,

$$\vec{E}'_f = \vec{V}_t + j\vec{I}_a X_q$$

As rated load is being supplied at unity power factor,

$$\therefore \vec{I}_a = 1 \angle 0^\circ \text{ p.u.}$$

$$\begin{aligned} \vec{E}'_f &= 1.0 \angle 0^\circ + j1.0 \angle 0^\circ (0.8) \\ &= 1.28 \angle 38.65^\circ \text{ p.u.} \end{aligned}$$

$$\therefore \text{Power angle, } \delta = 38.65^\circ$$

27. (a)

$$\text{Full load current} = \frac{25 \times 10^3}{\sqrt{3} \times 400 \times 0.8} = 45.11 \text{ A}$$

$$\begin{aligned} \text{Excitation emf } \vec{E}_f &= \vec{V} - j\vec{I}_a X \\ &= \frac{400}{\sqrt{3}} - (45.11 \angle 36.87^\circ)(j7) \\ &= 490.5 \angle -31^\circ \text{ V} \end{aligned}$$

Rotor angle slip by 0.25 mechanical degree,

$$\theta_e = \frac{P}{2} \theta_m$$

$$\Delta\delta = \frac{4}{2} \times 0.25 = 0.5^\circ$$

$$\begin{aligned} \text{Synchronizing emf} &= 2E_f \sin \frac{\Delta\delta}{2} \\ &= 2 \times 490.5 \sin \left( \frac{0.5}{2} \right) = 4.28 \text{ V} \end{aligned}$$

$$\text{Synchronizing current} = \frac{4.28}{7} = 0.611 \text{ A}$$

28. (a)

For double layer winding,

$$\text{No. of slots} = \text{No. of coils}$$

$$\text{Total number of turns} = 60 \times 10 = 600$$

$$\text{Turns per phase} = \frac{600}{3} = 200$$

$$\text{Pitch factor } (K_c) = \cos 18^\circ = 0.951$$

$$\text{Distribution factor } (K_d) = \frac{\sin \frac{m\beta}{2}}{m \sin \frac{\beta}{2}}$$

$$m = \frac{60}{4} \times \frac{1}{3} = 5$$

$$\beta = \frac{180}{60/4} = 12^\circ$$

$$K_d = \frac{\sin \frac{5 \times 12}{2}}{5 \sin \frac{12}{2}} = 0.9567$$

Induced emf,  $E_{ph} = \sqrt{2} \pi K_w \phi f T_{ph}$

$$E_{ph} = \sqrt{2} \pi \times 0.9567 \times 0.951 \times 0.015 \times 50 \times 200$$

$$E_{ph} = 606.33 \text{ V}$$

$$E_{L-L} = 1.05 \text{ kV}$$

29. (c)

Given,

$$V_t = 1.0 \text{ p.u.}$$

$$I_a = 1.0 \text{ p.u. at } 0.8 \text{ p.f. lagging}$$

$$\phi = \cos^{-1} 0.8 = 36.86^\circ$$

$$X_d = 0.8 \text{ p.u.}$$

$$X_q = 0.5 \text{ p.u.}$$

As we can use the relation,

$$\tan \psi = \frac{V_t \sin \phi + I_a X_q}{V_t \cos \phi + I_a r_a} \quad [\because \text{Here } r_a = 0]$$

$$\tan \psi = \frac{1 \times 0.6 + 1 \times 0.5}{1 \times 0.8 + 0}$$

or

$$\tan \psi = 1.375$$

$$\psi = 53.97^\circ$$

$\therefore$  Power angle;  $\delta = \psi - \phi$  [for generator]

$$= 53.97^\circ - 36.86^\circ$$

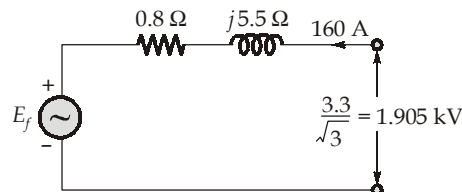
$$= 17.11^\circ$$

We can write,

$$\begin{aligned} \text{No load voltage; } E_f &= V_t \cos \delta + I_d X_d \\ &= V_t \cos \delta + (I_a \sin \psi) X_d \\ &= 1 \times \cos 17.11^\circ + (1 \times \sin 53.97^\circ) \times 0.8 \\ &= 1.602 \text{ p.u.} \approx 1.60 \text{ p.u.} \end{aligned}$$

30. (c)

Consider the following circuit;



$$\text{Full load current} = 160 \angle -36.86^\circ \text{ A}$$

$$\begin{aligned} \text{Synchronous impedance; } Z_s &= (0.8 + j 5.5) \Omega \\ &= 5.56 \angle 81.724^\circ \Omega \end{aligned}$$

From circuit diagram we can write;

$$\vec{E}_f = 1.905 \times 10^3 \angle 0^\circ - 5.56 \angle 81.724^\circ \times 160 \angle -36.86^\circ$$

$$E_f = 1.42 \angle -26.22^\circ \text{ kV}$$

Now

$$P_{\text{mech (dev)}} = 3 \times 1.42 \times 160 \cos (-36.86^\circ + 26.22^\circ) \\ = 669.88 \text{ kW}$$

$$\text{shaft output} = 669.88 - 30 = 639.88 \text{ kW}$$

$$\text{Power input} = \sqrt{3} \times 3.3 \times 160 \times 0.8 \\ = 731.62 \text{ kW}$$

$$\eta_{\text{full load}} = \frac{\text{Output}}{\text{Input}} \times 100 = \frac{639.88}{731.62} \times 100 = 87.46\%$$

