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Web: www.madeeasy.in | E-mail: info@madeeasy.in | Ph: 011-45124612

Power System-1

ELECTRICAL ENGINEERING

Date of Test : 14/10/2024

ANSWER KEY >

1. (a)	7. (c)	13. (b)	19. (c)	25. (c)
2. (c)	8. (c)	14. (b)	20. (b)	26. (b)
3. (d)	9. (b)	15. (c)	21. (c)	27. (b)
4. (d)	10. (c)	16. (c)	22. (b)	28. (a)
5. (b)	11. (d)	17. (d)	23. (a)	29. (a)
6. (a)	12. (a)	18. (a)	24. (d)	30. (a)

DETAILED EXPLANATIONS

1. (a)

Solar cell maximum power,

$$\begin{aligned} P_{\max} &= V_{\max} \times I_{\max} \\ &= -6 \times 10^{-3} \times 0.14 \\ &= 0.84 \text{ mW} \end{aligned}$$

$$\begin{aligned} P_{\text{input}} &= \text{Intensity} \times \text{Area} \\ &= 100 \times 5 \times 10^{-4} \text{ W} \end{aligned}$$

Cell efficiency, $\eta = \frac{0.84 \times 10^{-3}}{100 \times 5 \times 10^{-4}} = 0.0168 \text{ or } 1.68\%$

2. (c)

The self GMD of the seven strand conductor is the 49th root of 49 distances,

$$D_s = ((r')^7 (D_{12}^2 D_{26}^2 D_{14}^2 D_{17}^2)^6 (2r)^6)^{1/49}$$

$$D_s = ((0.7788r)^7 (D_{12}^2 D_{26}^2 D_{14}^2 D_{17}^2)^6 (2r)^5)^{1/49}$$

$$D_{12} = 2r, D_{26} = 2\sqrt{3}r, D_{14} = 4r, D_{17} = 2r$$

$$D_s = ((0.7788r)^7 (2^2r^2 \times 3 \times 2^2r^2 \times 2^2 \times r \times 2r \times 2r)^6)^{1/49}$$

$$\begin{aligned} D_s &= \frac{2r(3 \times 0.7788)^{1/7}}{6^{1/49}} \\ &= 2.1767 \times 2 = 0.435 \approx 0.44 \text{ cm} \end{aligned}$$

3. (d)

For given system:

Total reactive power at,

$$G_1 = \text{Reactive power demand at Bus 1} + \text{Reactive power being transferred to Bus 2}$$

Reactive power demand at bus = 10 pu

Reactive power transferred to bus 2,

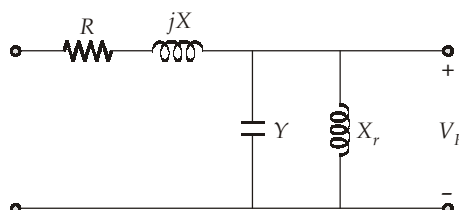
$$Q_s = \frac{|V_s|}{X} (|V_s| - |V_R| \cos \delta)$$

$$Q_s = \frac{1}{0.04} (1 - 1 \times \cos 20^\circ) = 1.508 \text{ pu}$$

\therefore Total reactive power at G_1 $Q_{G1} = 1.508 + 10 = 11.508 \text{ pu}$

4. (d)

Given transmission line model can be drawn,



Equivalent T-matrix will be

$$\begin{bmatrix} A_1 & B_1 \\ C_1 & D_1 \end{bmatrix} = \begin{bmatrix} 1+YZ & Z \\ Y & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1/jX_r & 1 \end{bmatrix}$$

For no ferranti effect,

$$V_s = V_R \rightarrow A_1 = 1$$

$$1 + YZ + \frac{Z}{jX_r} = 1$$

Simplifying, $YZ = j \frac{Z}{X_r}$

or $|X_r| = \frac{Z}{YZ} = \frac{1}{Y} = \frac{1}{4 \times 10^{-4}} = 2500 \Omega$

5. (b)

$$\text{Plug setting} = \frac{\text{Primary fault current of C.T.}}{\text{CT ratio} \times \text{relay current setting}}$$

$$1 = \frac{I_f}{\frac{500}{1} \times 0.3}$$

$$I_f = 0.3 \times 500 = 150 \text{ A}$$

$$\text{Fault current, } I_f = 3 I_{a0}$$

$$I_{a0} = \frac{I_f}{3} = \frac{150}{3} = 50 \text{ A}$$

6. (a)

$$C_{an} = \frac{2\pi\epsilon_0}{\ln\left(\frac{\text{GMD}}{r}\right)} \text{ F/m}$$

$$\text{GMD} = (3 \times 4 \times 5)^{1/3} = 3.914 \text{ m}$$

$$C_{an} = \frac{2\pi \times 8.854}{\ln\left(\frac{3.914}{2 \times 10^{-2}}\right)} \times 10^{-12} \text{ F/m}$$

$$C_{an} = 10.54 \text{ pF/m}$$

7. (c)

Transmission line parameters,

$$V_s = A V_r + B I_r \quad \dots(i)$$

There is no load current but current flowing through the shunt inductor is I_L .

Now equation (i) becomes,

$$V_s = A V_r + B I_L$$

Dividing the above equation with I_L on both sides.

$$\frac{V_s}{I_L} = A \frac{V_r}{I_L} + B \frac{I_L}{I_L}$$

Since,

$$V_s = V_R$$

$$X_L = A X_L + B$$

$$X_L (1 - A) = B$$

$$X_L = \frac{B}{1 - A} = \frac{160}{1 - 0.9} = 1600 \Omega$$

8. (c)

P_{\max} is more if 'X' of line is low,

$$P_{\max} = \frac{V_1 V_2}{X}$$

∴ L is low ($X = 2\pi fL$)

$$L = 2 \times 10^{-7} \ln\left(\frac{GMD}{GMR}\right)$$

To get more P_{\max} , GMD should be low and GMR should be high.

9. (b)

$$V = i \sqrt{\frac{L}{C}} = 20 \sqrt{\frac{2}{8 \times 10^{-6}}} = \frac{20}{2 \times 10^{-3}} = 10 \text{ kV}$$

10. (c)

Maximum dielectric stress = g_{\max}

$$g_{\max} = \frac{V}{r \ln\left(\frac{R}{r}\right)}$$

Minimum dielectric stress = g_{\min}

$$g_{\min} = \frac{V}{R \ln\left(\frac{R}{r}\right)}$$

∴ the ratio of maximum to minimum dielectric stress

$$= \frac{g_{\max}}{g_{\min}}$$

(or)

$$\frac{g_{\max}}{g_{\min}} = \frac{\frac{V}{r \ln\left(\frac{R}{r}\right)}}{\frac{V}{R \ln\left(\frac{R}{r}\right)}} = \frac{R}{r} = \frac{D}{d}$$

11. (d)

$$GMD = (20 \times 20 \times 40)^{1/3} = 25.2 \text{ feet}$$

$$GMR = (0.7788 \times 0.5 \times 8)^{1/2} = 1.765 \text{ inch}$$

$$= \frac{1.765}{12} \text{ feet} = 0.147 \text{ feet}$$

$$\begin{aligned} \text{Inductance, } L &= 0.2 \ln \frac{\text{GMD}}{\text{GMR}} \text{ mH/km} \\ &= 0.2 \ln \frac{25.2}{0.147} = 1.028 \text{ mH/km} \end{aligned}$$

12. (a)

$$\text{Input to motor} = \frac{\text{Motor output}}{\eta} = \frac{80 \text{ kW}}{0.95} = 84.21 \text{ kW}$$

Initial power factor, $\cos \phi_1 = 0.75$ (lagging)

Power factor after improvement,

$$\cos \phi_2 = 0.95 \text{ (lagging)}$$

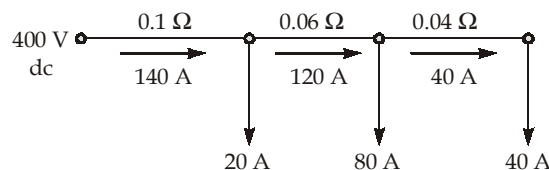
$$\begin{aligned} \text{KVAR rating of capacitor bank} &= P(\tan \phi_1 - \tan \phi_2) \\ &= 84.21 [\tan(\cos^{-1}(0.75)) - \tan(\cos^{-1}(0.95))] \\ &= 46.58 \text{ kVAR} \end{aligned}$$

13. (b)

$$\begin{aligned} \text{GMR} &= \left[\left((0.7788 \times 2) \times 50 \times 50 \times 50\sqrt{2} \right)^4 \right]^{1/16} \\ &= 22.9 \text{ cm} \end{aligned}$$

14. (b)

For given dc system, SLD can redrawn,



$$\begin{aligned} V_{\min} &= V_{\text{dc}} - I_1 R_1 - I_2 R_2 - I_3 R_3 \\ &= 400 - (140 \times 0.1) - (120 \times 0.06) - (0.04 \times 40) \\ &= 400 - 14 - 7.2 - 1.6 = 377.2 \text{ V} \end{aligned}$$

15. (c)

$$\text{Given, } |V_S| = |V_R| = 220 \text{ kV}$$

$$\alpha = 5^\circ,$$

$$\beta = 75^\circ$$

Since the power is received at unity power factor,

$$Q_R = 0$$

$$0 = \frac{220 \times 220}{200} \sin(75^\circ - \delta) - \frac{0.85}{200} \times (220)^2 \sin(75^\circ - 5^\circ)$$

$$= 242 \sin(75^\circ - \delta) - 193.29$$

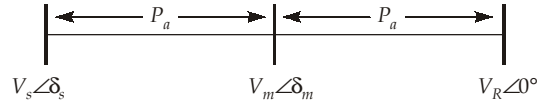
$$193.29 = 242 \sin(75^\circ - \delta)$$

$$75^\circ - \delta = 53^\circ$$

$$\text{Power angle, } \delta = 22$$

16. (c)

Considering the midpoint location with compensator,



The reactance of line upto midpoint is $X/2$,

$$P_e = \frac{V_s V_m}{X/2} \sin(\delta_s - \delta_m) = \frac{V_m V_R}{X/2} \sin(\delta_m - 0)$$

or $\delta_s - \delta_m = \delta_m$ or $\delta_m = \frac{\delta_s}{2} = \frac{30^\circ}{2} = 15^\circ$

$$\begin{aligned} P_e &= \frac{V_s V_m}{X/2} \sin(\delta_s - \delta_m) \\ &= \frac{1 \times 0.90}{0.4/2} \sin 15^\circ = 1.16 \text{ pu} \end{aligned}$$

17. (d)

$$V_s = 120 \text{ kV}, \quad V_r = 110 \text{ kV},$$

$$A = 0.96$$

$$\alpha = 1^\circ, \quad \beta = 80^\circ$$

Maximum power transmitted is given by

$$\begin{aligned} P_{\max} &= \frac{V_s \cdot V_r}{B} - \frac{AV_r^2}{B} \cos(\beta - \alpha) \\ &= \frac{110 \times 120}{100} - \frac{0.96 \times 110^2}{100} \cos(80^\circ - 1^\circ) \\ P_{\max} &= 109.83 \text{ MW} \end{aligned}$$

18. (a)

Core radius, $r_1 = \frac{1.5}{2} = 0.75 \text{ cm}$

Sheath radius, $r_2 = \frac{5}{2} = 2.5 \text{ cm}$

$$\ln\left(\frac{r_2}{r_1}\right) = \log_e^{2.5/0.75} = 1.2$$

$$\rho = \frac{R_{\text{INS}} \times 2\pi l}{\ln\left(\frac{r_2}{r_1}\right)} = \frac{1820 \times 10^6 \times 2\pi \times 3500}{1.2} = 33.35 \times 10^{12} \Omega\text{-m}$$

19. (c)

Capacitance between any two core,

$$C_2 = 3.7 \mu\text{F}$$

Capacitance of each core to neutral,

$$C_N = 2C_2 = 2 \times 3.7 = 7.4 \mu\text{F}$$

$$I_C = 2\pi f V_P C_N$$

$$= 2\pi \times 50 \times \frac{11000}{\sqrt{3}} \times 7.4 \times 10^{-6} = 14.76 \text{ A}$$

20. (b)

$$\text{Insulation resistance, } R = \frac{\rho}{2\pi l} \ln\left(\frac{R}{r}\right) \Omega$$

$$\frac{R_2}{R_1} = \frac{l_1}{l_2}$$

$$R_2 = 1 \text{ M}\Omega \left(\frac{100}{10}\right) = 10 \text{ M}\Omega$$

21. (c)

Power transfer capacity $\propto V^2$

$$\frac{P_1}{P_2} = \frac{V_1^2}{V_2^2}$$

$$P_2 = P_1 \frac{V_2^2}{V_1^2} = P \left(\frac{100}{400}\right)^2 = \frac{P}{16}$$

22. (b)

$$\text{Primary line current} = I_{LP} = \frac{10 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 43.74 \text{ A}$$

CT connected to primary of transformer is delta connected.

So, the current in the secondary of the CT is $\frac{5}{\sqrt{3}} \text{ A}$ \therefore The CT ratio of primary of the transformer is, $43.74 / (5/1.732)$

The secondary line current of the transformer is,

$$I_{LS} = \frac{10 \times 10^6}{\sqrt{3} \times 66 \times 10^3} = 87.47 \text{ A}$$

 \therefore The CT ratio on the secondary is, $\frac{87.47}{5}$.

23. (a)

In π model, the shunt admittance at each end of the line is $\frac{Y}{2}$

$$\begin{aligned} \frac{Y}{2} &= j\omega \frac{C}{2} = j(2\pi \times 50) \times \frac{0.03}{\pi} \times \frac{1}{2} \times 10^{-6} \times 100 \\ &= 150 \times 10^{-6} \angle 90^\circ \text{ } \Omega \end{aligned}$$

24. (d)

Zero regulation of a transmission line occurs at a leading power factor,

$$\text{when } \phi = \tan^{-1}\left(\frac{X}{R}\right)$$

$$\text{Given, } X = R$$

$$\phi = 45^\circ$$

$$\text{Hence } \cos \phi = 0.707 \text{ leading.}$$

25. (c)

$$P_R = \frac{V_S V_R}{Z} \cos(\theta - \delta) - \frac{V^2}{Z} \cos \theta$$

For maximum power transfer,

$$\theta = \delta$$

and also it is given that, $V_R = V_S = V$

$$P_{R \max} = \frac{V^2}{Z} - \frac{V^2}{Z} \cos \theta$$

$$Z = \sqrt{R^2 + X^2}$$

$$\cos \theta = \frac{R}{Z}$$

$$P_{R \max} = \frac{V^2}{\sqrt{R^2 + X^2}} - \frac{V^2 R}{(R^2 + X^2)}$$

$$Z = R + jX$$

So, keeping $\frac{dP_{R \max}}{dX} = 0$

We get, $X = \sqrt{3}R$

$$X = \sqrt{3} \times \sqrt{3}$$

$$X = 3 \Omega$$

26. (b)

The relay current setting = 25%

∴ The relay operates at a current of
 $= 0.25 \times 5 = 1.25 \text{ A}$

The VA burden on the relay is,

$$VA = 5$$

$$5 = V \times 1.25$$

∴ $V = 4 \text{ V.}$

27. (b)

$$\text{String efficiency} = \frac{\text{Voltage across the string}}{n \times \text{Voltage across the lower most unit}}$$

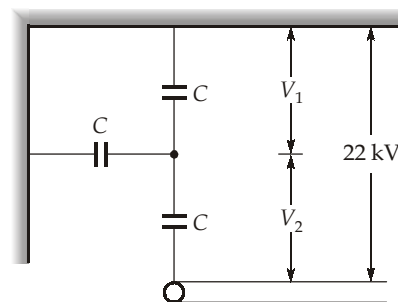
$$\eta = \frac{V_1 + V_2}{n \times V_2} \times 100$$

$$V_2 = V_1 + KV_1$$

$$V_2 = 2 V_1$$

$$\eta = \frac{V_1 + 2V_1}{2 \times 2V_1} \times 100$$

$$= \frac{3V_1}{4V_1} \times 100 = 0.75 \times 100 = 75\%$$



28. (a)

$$\text{Load factor} = \frac{\text{Average load}}{\text{Maximum demand}}$$

$$\text{Plant capacity factor} = \frac{\text{Average load}}{\text{Plant capacity}}$$

$$\frac{\text{Load factor}}{\text{Plant capacity factor}} = \frac{0.6}{0.5} = \frac{\text{Plant capacity}}{\text{Maximum demand}}$$

$$\text{Plant capacity} = \frac{0.6}{0.5} \times 30 = 36 \text{ MW}$$

$$\begin{aligned} \text{Reserve capacity} &= \text{Plant capacity} - \text{Maximum demand} \\ &= 36 - 30 = 6 \text{ MW} \end{aligned}$$

29. (a)

$$\text{The secondary current, } I_s = \frac{I_p}{n}$$

$$\text{Where, } n = \frac{500}{5}$$

$$I_s = 7500 \times \frac{5}{500} = 75 \text{ A}$$

$$\text{Relay current setting} = 125\% \text{ of } 5\text{A} = 1.25 \times 5 = 6.25 \text{ A}$$

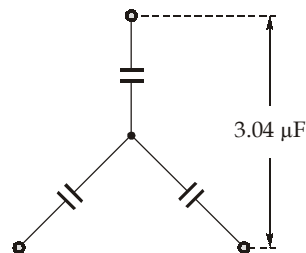
$$\text{Plug setting multiplier (PSM)} = \frac{75}{6.25} = 12$$

Using data in characteristic table is

Operating time corresponding to PSM = 12 is 2.8 sec (at TMS = 1)

$$\text{Operating time of relay} = 2.8 \text{ sec} \times 0.4 = 1.12 \text{ sec.}$$

30. (a)



Since the capacitance measured is $3.04 \mu\text{F}$ between the conductors, the capacitance per phase will be

$$2 \times 3.04 = 6.08 \mu\text{F}$$

$$\begin{aligned} \text{3-phase kVAR required} &= V^2 \omega C \\ &= 20^2 \times 314 \times 6.08 \times 10^{-3} \\ &= 763.6 \text{ kVAR} \end{aligned}$$

