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HEAT TRANSFER

MECHANICAL ENGINEERING

Date of Test : 13/11/2024

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (b) | 7. (a) | 13. (c) | 19. (a) | 25. (b) |
| 2. (c) | 8. (b) | 14. (a) | 20. (c) | 26. (b) |
| 3. (d) | 9. (b) | 15. (a) | 21. (d) | 27. (b) |
| 4. (b) | 10. (c) | 16. (a) | 22. (b) | 28. (c) |
| 5. (a) | 11. (d) | 17. (a) | 23. (c) | 29. (c) |
| 6. (a) | 12. (b) | 18. (b) | 24. (b) | 30. (a) |

DETAILED EXPLANATIONS

1. (b)

$$\begin{aligned}\frac{dT}{d\tau} &= u \frac{dT}{dx} + v \frac{dT}{dy} + w \frac{dT}{dz} \\ &= 2y^2 \times 5y^2 + 3x \times 10xy + 0.0\end{aligned}$$

$$\begin{aligned}\frac{dT}{d\tau} &= 10y^4 + 30x^2y \\ &= 10(2)^4 + 30(1)^2 \times 2 = 220 \text{ units}\end{aligned}$$

2. (c)

$$\begin{aligned}C_h(T_{h_i} - T_{h_e}) &= C_c(T_{c_e} - T_{c_i}) \\ \Rightarrow C_h(20) &= C_c(80) \\ \frac{C_{\min}}{C_{\max}} &= \frac{C_c}{C_h} = \frac{20}{80} = 0.25 = \text{Capacity ratio}\end{aligned}$$

3. (d)

$\frac{Gr}{Re^2}$ signifies the type of convection

$\frac{Gr}{Re^2} \ll 1$, forced convection

$\frac{Gr}{Re^2} \gg 1$, free convection

$\frac{Gr}{Re^2} \simeq 1$, mixed convection

4. (b)

The R value is, $\frac{L}{k} = \frac{0.15}{0.04} = 3.75 \text{ (m}^2 \text{ K/W)}$

5. (a)

For oils Prandtl number (Pr) $\gg 1$ and $\delta_t \ll \delta$.

6. (a)

For counterflow operation, the minimum exit temperatures of oil would be when effectiveness equal to 1.

$$\begin{aligned}\epsilon &= \frac{C_h(T_{h_1} - T_{h_2})}{C_{\min}(T_{h_1} - T_{c_1})} = 1 \\ C_h &= C_{\min} \\ \frac{165 - T_{h_2}}{165 - 30} &= 1 \\ T_{h_2} &= 30^\circ\text{C}\end{aligned}$$

7. (a)

The total irradiation can be obtained by

$$\begin{aligned}
 G &= \int_0^{\infty} G_{\lambda} d\lambda \\
 &= \text{Area under the curve} \\
 &= \frac{1}{2} \times 2000 \times 10 + 2000 \times 30 + \frac{1}{2} \times 2000 \times 10 \\
 G &= 80000 \text{ W/m}^2
 \end{aligned}$$

8. (b)

$$\begin{aligned}
 q'' &= h(T_w - T_{\infty}) = -K \left(\frac{dT}{dy} \right)_{y=0} \\
 \frac{-dT}{dy} &= (T_w - T_{\infty}) \left[\frac{a_1}{L} + 2a_2 \frac{y}{L^2} \right] \\
 \left(\frac{dT}{dy} \right)_{y=0} &= -(T_w - T_{\infty}) \frac{a_1}{L} \\
 \Rightarrow h(T_w - T_{\infty}) &= K \frac{a_1}{L} (T_w - T_{\infty}) \\
 \frac{hL}{K} &= a_1 \\
 Nu &= \frac{hL}{K} = a_1
 \end{aligned}$$

9. (b)

We know that,

$$\begin{aligned}
 Q &= hA_s(T_5 - T_0) \\
 A_s &= 5 \times 0.4 \times 0.4 = 0.8 \text{ cm}^2 \\
 Q &= \frac{4.8}{24} = 0.2 \text{ W}
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 \text{From eqn. (1), } 0.2 &= 18 \times 0.8 \times 10^{-4} \times (T_s - 30) \\
 T &= 168.88^\circ\text{C} \simeq 169^\circ\text{C}
 \end{aligned}$$

10. (c)

$$NTU = \frac{UA}{C_{\min}} = \frac{1800 \times 15}{3 \times 4.18 \times 10^3} = 2.153$$

For steam condenser,

$$\begin{aligned}
 \epsilon &= 1 - \exp(-NTU) \\
 &= 1 - \exp(-2.153) \\
 \epsilon &= 0.88
 \end{aligned}$$

11. (d)

$$\begin{aligned}
 q &= 10^5 \text{ W/m}^2, & r_1 &= 0.04 \text{ m}, & r_2 &= 0.06 \text{ m}, \\
 k &= 20 \text{ W/mK}
 \end{aligned}$$

for sphere,

$$R_{th} = \left[\frac{r_2 - r_1}{4\pi r_1 r_2 k} \right]$$

$$R_{th} = \frac{0.06 - 0.04}{4\pi \times 0.06 \times 0.04 \times 20} = 0.0332 \text{ K/W}$$

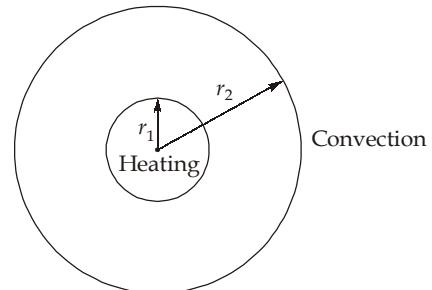
$$\therefore Q = \frac{\Delta T}{R_{th}}$$

$$Q = 4\pi r_1^2 \times q = \frac{T_i - T_0}{0.0332}$$

$$4\pi \times 0.04^2 \times 10^5 \times 0.0332 = T_i - T_0$$

$$T_i = 266.75^\circ\text{C}$$

$$\text{or } T_i = 539.75 \text{ K}$$



12. (b)

Given

$$U_0 = 3000 \text{ W/m}^2\text{K}$$

$$d_i = 2.5 \text{ cm}, d_o = 3 \text{ cm}, k = 50 \text{ W/mK}$$

$$h_0 = 31000 \text{ W/m}^2\text{K}$$

$$\nu = 0.365 \times 10^{-6} \text{ m}^2/\text{s}$$

$$k = 700 \times 10^{-3} \text{ W/mK}$$

$$Pr = 2.2$$

$$\frac{1}{A_0 U_0} = \frac{1}{A_i h_i} + \frac{1}{A_o h_o} + \frac{\ln(r_2/r_1)}{2\pi k L}$$

for unit length,

$$l = 1 \text{ m}$$

$$A_i = \pi d_i = \pi \times 0.025$$

$$A_0 = \pi d_o = \pi \times 0.03$$

$$\frac{1}{\pi \times 0.03 \times 3000} = \frac{1}{\pi \times 0.025 \times h_i} + \frac{1}{\pi \times 0.03 \times 31000} + \frac{\ln(3/2.5)}{2\pi \times 50 \times 1}$$

$$h_i = 4870 \text{ W/m}^2\text{K} \Rightarrow 4.87 \text{ kW/m}^2\text{K}$$

13. (c)

$$T_1 = 1000 \text{ K}, T_2 = 600 \text{ K}$$

$$\left(\frac{q_{12}}{A} \right) = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{2}{\epsilon} - 1 \right)(n+1)}$$

with similar shields

$$\text{Now } \left(\frac{q_{12}}{A} \right)_5 = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{2}{\epsilon} - 1 \right)(5+1)}$$

when 5 more shields are applied

$$\left(\frac{q_{12}}{A} \right)_{10} = \frac{\sigma(T_1^4 - T_2^4)}{\left(\frac{2}{\epsilon} - 1 \right)(10+1)}$$

$$\frac{\left(\frac{q_{12}}{A}\right)_{10}}{\left(\frac{a_{12}}{A}\right)_5} = \frac{1/11}{1/6} = \frac{6}{11}$$

% reduction,

$$\left[1 - \frac{(q_{12}/A)_{10}}{(q_{12}/A)_5}\right] \times 100 = \left[1 - \frac{6}{11}\right] \times 100 = 45.45\%$$

14. (a)

Given: $d_0 = 30 \text{ cm}$, $L = 170 \text{ cm}$, $h = 8 \text{ W/m}^2\text{K}$, $k = 7 \text{ W/mK}$

$$s = \frac{\pi r_0^2 L}{2\pi r_0 L + 2\pi r_0^2}$$

$$s = \frac{\pi \times 0.15^2 \times 1.7}{2\pi \times 0.15 \times 1.7 + 2\pi \times 0.15^2}$$

$$s = 0.0689 \text{ m}$$

$$Bi = \frac{hs}{k} = \frac{8 \times 0.0689}{7} = 0.0787$$

Lumped analysis is valid,

$$\frac{ht}{\rho sc} = \ln \left[\frac{37 - 20}{26 - 20} \right]$$

$$t = \frac{1.0414 \times 1000 \times 0.0689 \times 4180}{8} = 37492 \text{ second}$$

or $t = 10.41 \text{ hours} = 10 \text{ hours } 25 \text{ minutes before}$
 i.e. died at 12 : 00 – (10 : 25 – 6 : 00) PM = 7 : 35 pm yesterday

15. (a)

Statement 1 is correct but statement 2 is incorrect, it depends on matter which type of phenomenon is taking place.

Volumetric phenomenon = gas, semi transparent solids

Surface phenomenon = solids and liquids

16. (a)

Given:

$$d = 30 \text{ mm}, L = 700 \text{ mm},$$

$$T_\infty = 25^\circ\text{C}, T_0 = 600^\circ\text{C}$$

$$h = 20 \text{ W/m}^2\text{K}, k = 132.3 \text{ W/mK}$$

$$m = \sqrt{\frac{hP}{kA}} = \sqrt{\frac{4h}{kd}} \quad (\text{for cylinder})$$

$$m = \sqrt{\frac{4 \times 20}{132.3 \times 0.03}} = 4.49$$

Steady state rate of heat lost,

$$q = \sqrt{hPkA} \times \theta_0 \times \tanh(mL)$$

$$\sqrt{hPkA} = \sqrt{20 \times (\pi \times 0.03) \times 132.3 \times (\pi \times 0.25 \times 0.03^2)} = 0.4199$$

$$\tanh(mL) = \tanh(4.49 \times 0.7) = 0.9963$$

$$\dot{q} = 0.4199 \times 0.9963 \times (600 - 25)$$

$$\dot{q} = 240.57 \text{ W}$$

$$\text{Heat lost in one minute} = \dot{q} \cdot t = 240.57 \times 60 \times 10^{-3} \text{ kJ} = 14.43 \text{ kJ}$$

17. (a)

$$D = 20 \text{ mm}, \rho = 978 \text{ kg/m}^3, \mu = 4 \times 10^{-4} \text{ kg/m-s}, \text{Pr} = 2.54,$$

$$\text{Re} = \frac{\rho V D}{\mu} = \frac{978 \times 2 \times 0.02}{4 \times 10^{-4}} \Rightarrow \text{Re} = 97800$$

∴ Re > 2300 flow is turbulent

Using Dittus Boltier equation,

$$\text{Nu} = 0.023(\text{Re})^{0.8}(\text{Pr})^{0.4}$$

$$\frac{h_i d}{k} = 0.023(97800)^{0.8}(2.54)^{0.4}$$

$$h_i = 328.04 \times \frac{0.332}{0.02} = 5445.5 \text{ W/m}^2\text{K}$$

$$\frac{1}{U} = \frac{1}{h_i} + \frac{1}{h_0} = \frac{1}{5445.5} + \frac{1}{10000}$$

$$U = 3525.6 \text{ W/m}^2\text{K}$$

18. (b)

$$F_{12} = 0.12$$

$$F_{12} + F_{11} + F_{13} = 1$$

$$F_{13} = 1 - F_{12} = 1 - 0.12 = 0.88$$

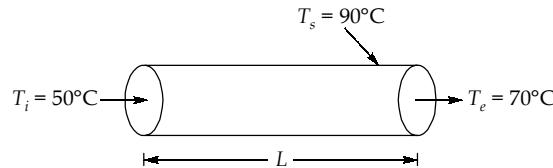
$$A_3 F_{31} = A_1 F_{13}$$

$$F_{31} = \frac{\pi}{4} \times \frac{d^2}{\pi \times d \times h} \times 0.88$$

$$F_{31} = \frac{d}{4 \times h} \times 0.88 = 0.165$$

$$\begin{aligned} q_{3\text{-surrounding}} &= 2 \times F_{31} \times A_3 \times \sigma(T_3^4 - T_0^4) \\ &= 2 \times 0.165 \times \pi \times 0.075 \times 0.1 \times 5.67 \times 10^{-8} \times (700^4 - 310^4) \\ &= 102 \text{ W} \end{aligned}$$

19. (a)



We know that for constant temperature wall :

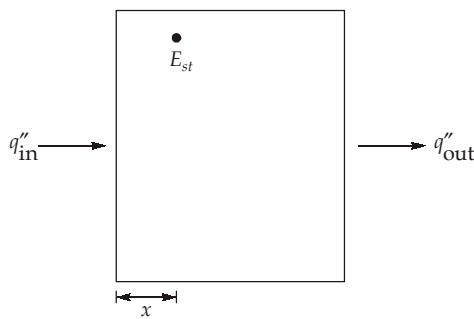
$$\begin{aligned} \frac{T_e - T_s}{T_i - T_s} &= e^{\frac{-hPL}{\dot{m}C_p}} \\ \dot{m} &= \rho \times A \times V = \rho \times \frac{\pi}{4} \times d^2 \times V \\ &= 1000 \times \frac{\pi}{4} \times (0.02)^2 \times 1.2 = 0.377 \text{ kg/s} \\ \frac{70 - 90}{50 - 90} &= e^{\frac{-6.5 \times 10^3 \times \pi \times 0.02 \times L}{0.377 \times 4.2 \times 10^3}} = e^{-0.258L} \\ 0.69314 &= 0.258L \\ L &= 2.686 = 2.7 \text{ m} \end{aligned}$$

20. (c)

$$T_{(x)} = a + bx + cx^2$$

By Fourier law,

$$q''_x = -k \frac{\partial T}{\partial x}$$



$$\begin{aligned} \text{So, } q''_{in} &= -k \frac{\partial T}{\partial x} \Big|_{x=0} \\ &= -k(b + 2cx) \Big|_{x=0} = -1(-200 + 2 \times 30 \times 0) \\ q''_{in} &= 200 \text{ W/m}^2 \\ q''_{out} &= -k(b + 2cx) \Big|_{x=0.3} = -1(-200 + 2 \times 30 \times 0.3) \\ &= 182 \text{ W/m}^2 \end{aligned}$$

Applying on energy balance to control volume about the wall

$$\begin{aligned} E''_{in} - E''_{out} &= E''_{st} \\ E''_{st} &= 200 - 182 = 18 \text{ W/m}^2 \end{aligned}$$

21. (d)

The center temperature of the wire (cylinder) is given by

$$T_o = T_s + \frac{\dot{e}_{\text{gen}} r_0^2}{4k}$$

Given :

$$T_s = 110^\circ\text{C}$$

$$\dot{e}_{\text{gen}} = \frac{2.5 \times 10^3}{\pi \times r^2 \times l} = \frac{2.5 \times 10^3}{\pi \times (3 \times 10^{-3})^2 \times 1}$$

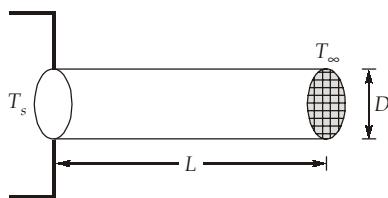
$$\dot{e}_{\text{gen}} = 88.419 \times 10^6 \text{ W/m}^3$$

$$k = 21 \text{ W/m°C}$$

$$\text{So, } T_o = 110 + \frac{88.419 \times 10^6 \times (3 \times 10^{-3})^2}{4 \times 21}$$

$$T_o = 119.473^\circ\text{C}$$

22. (b)



$$\text{Fin effectiveness, } \varepsilon_f = \frac{\text{Heat transfer rate with fin}}{\text{Heat transfer rate without fin}}$$

$$\varepsilon_f = \frac{Q_f}{hA\theta_o}$$

$$Q_f = \sqrt{hPkA} (\tan hml) \theta_o$$

$$m = \sqrt{\frac{hP}{kA}} = \sqrt{\frac{12 \times \pi \times 4 \times 10^{-2} \times 4}{237 \times \pi \times (4 \times 10^{-2})^2}} = 2.25 \text{ m}^{-1}$$

$$Q_f = \sqrt{12 \times \pi \times 4 \times 10^{-2} \times 237 \times \frac{\pi}{4} \times (4 \times 10^{-2})^2 (\tan h(2.25 \times 0.1)) \theta_o}$$

$$Q_f = 0.6701 \times 0.2212 = 0.1482 \theta_o$$

$$\varepsilon_f = \frac{0.1482 \theta_o}{12 \times \frac{\pi}{4} \times (4 \times 10^{-2})^2 \times \theta_o} = 9.83$$

23. (c)

Given,

$$T_s = 30^\circ\text{C}$$

$$T_\infty = 25^\circ\text{C}$$

$$A = 1.5 \text{ m}^2$$

$$h = 7 \text{ W/m}^2 \text{ K}$$

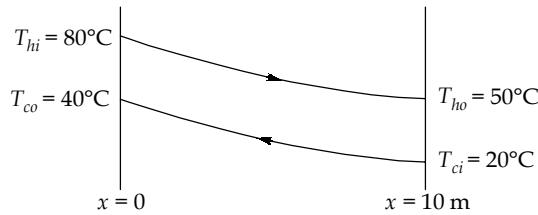
$$\epsilon = 0.9$$

$$\begin{aligned} \dot{Q}_{\text{convection}} &= h \times A (T_s - T_\infty) \\ &= 7 \times 1.5 [30 - 25] = 52.5 \text{ W} \end{aligned}$$

$$\begin{aligned}\dot{Q}_{\text{radiation}} &= \varepsilon \times \sigma \times A (T_s^4 - T_\infty^4) \\ &= 0.9 \times 5.67 \times 10^{-8} \times 1.5 \times [303^4 - 298^4] = 41.54 \text{ W} \\ \dot{Q}_{\text{total}} &= 52.5 + 41.54 = 94.04 \text{ W}\end{aligned}$$

24. (b)

Assume counter,

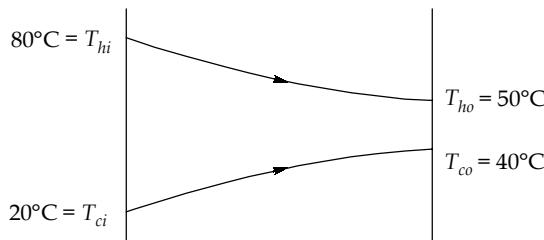


$$\Delta T_1 = 80^\circ\text{C} - 40^\circ\text{C} = 40^\circ\text{C}$$

$$\Delta T_2 = 50^\circ\text{C} - 20^\circ\text{C} = 30^\circ\text{C}$$

$$\text{LMTD} = \frac{\Delta T_1 - \Delta T_2}{\ln\left(\frac{\Delta T_1}{\Delta T_2}\right)} = \frac{40^\circ\text{C} - 30^\circ\text{C}}{\ln\left(\frac{40}{30}\right)} = 34.7^\circ\text{C}$$

Assume parallel,

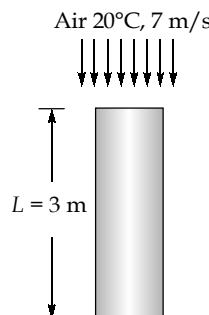


$$\Delta T_1 = 80^\circ\text{C} - 20^\circ\text{C} = 60^\circ\text{C}$$

$$\Delta T_2 = 50^\circ\text{C} - 40^\circ\text{C} = 10^\circ\text{C}$$

$$(\text{LMTD})_{\text{parallel HE}} = \frac{\Delta T_1 - \Delta T_2}{\ln\left(\frac{\Delta T_1}{\Delta T_2}\right)} = \frac{60^\circ\text{C} - 10^\circ\text{C}}{\ln\left(\frac{60}{10}\right)} = 27.9^\circ\text{C}$$

25. (b)



The flow is along 3 m side of the plate, and thus the characteristic length is $L = 3 \text{ m}$. Both sides are exposed to air flow,

$$\begin{aligned}A &= 2 \times w \times L \\ &= 2 \times 2 \times 3 = 12 \text{ m}^2\end{aligned}$$

For flat plates, drag force is equivalent to friction force.

$$F_f = C_f A_s \frac{\rho V^2}{2}$$

$$C_f = \frac{F_f}{\frac{1}{2} \rho A_s V^2} = \frac{0.86}{1.204 \times 12 \times \frac{1}{2} \times (7)^2} = 0.00243$$

From Reynolds Analogy,

$$St \times (\text{Pr})^{2/3} = \frac{C_f}{2} = \frac{0.00243}{2}$$

$$St = \frac{h}{\rho V c_p}$$

$$h = 0.00149 \times 1.204 \times 7 \times 1007 \\ = 12.64 \text{ W/m}^2\text{K}$$

26. (b)

Since fluid properties will be same at same temperature so Prandtl number will be same

$$Nu \propto (\text{Re})^m$$

$$\frac{Nu_2}{Nu_1} = \frac{(VL_C)_2^m}{(VL_C)_1^m} = \left(\frac{V_2 L_{C_2}}{V_1 L_{C_1}} \right)^m$$

$$= \left(\frac{25}{50} \times \frac{12}{6} \right)^m = 1$$

$$Nu_2 = Nu_1$$

$$\frac{h_1 L_{C_1}}{K} = \frac{h_2 L_{C_2}}{K}$$

$$\Rightarrow h_2 = \frac{h_1 L_{C_1}}{L_{C_2}} = \frac{120 \times 6}{12} = 60 \text{ W/m}^2\text{C}$$

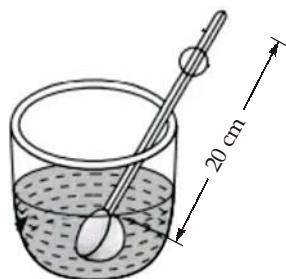
Heat flux from the second airfoil

$$= h_2 (T - T_\infty)$$

$$= 60 \times (80 - 15)$$

$$= 3900 \text{ W/m}^2$$

27. (b)



Given : $h = 16$, $k = 15$, $P = 2 \times (0.25 + 1.25) = 3 \text{ cm}$

$$A = 0.25 \times 1.25 \text{ cm}^2$$

$$m = \sqrt{\frac{hP}{kA}} = \sqrt{\frac{16}{15} \times \frac{3 \times 100}{0.25 \times 1.25}} = 32$$

$$mL = 32 \times 0.20 = 6.4$$

$mL > 5$ (So can assume infinitely long fin)

$$\frac{T_L - T_\infty}{T_0 - T_\infty} = e^{-mL}$$

$$\frac{T_L - 25}{70} = e^{-6.4}$$

$$\Rightarrow T_L = 25 + 70 e^{-6.4}$$

Temperature difference across the exposed surface

$$\begin{aligned} T_0 - T_L &= 95 - (25 + 70 e^{-6.4}) \\ &= 70(1 - e^{-6.4}) \end{aligned}$$

28. (c)

$$Q = -kA \left(\frac{dT}{dx} \right)_{x=0}$$

$$\frac{dT}{dx} = 10x - 4$$

$$\left(\frac{dT}{dx} \right)_{x=0} = -4$$

$$Q = -0.15 \times 3 \times (-4) = 1.8 \text{ W}$$

29. (c)

$$\dot{m}_h = \frac{1000}{3600} = 0.277 \text{ kg/s}$$

Hot fluid, $T_{hi} = 70^\circ\text{C}$

$T_{ho} = 40^\circ\text{C}$

$c_{ph} = 2 \text{ kJ/kgK}$

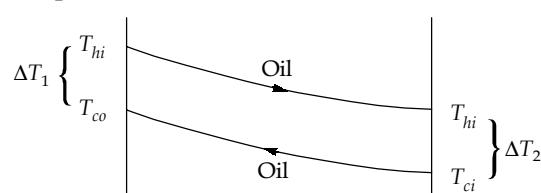
Cold fluid, $T_{ci} = 25^\circ\text{C}$

$T_{co} = 40^\circ\text{C}$

$c_{pc} = 4.2 \text{ kJ/kgK}$

$U = 0.2 \text{ kW/m}^2\text{K}$

Counter flow temperature profile



$$\Delta T_1 = 70^\circ\text{C} - 40^\circ\text{C} = 30^\circ\text{C}$$

$$\Delta T_2 = 40^\circ\text{C} - 25^\circ\text{C} = 15^\circ\text{C}$$

$$\text{LMTD} = \frac{\Delta T_1 - \Delta T_2}{\ln\left(\frac{\Delta T_1}{\Delta T_2}\right)} = \frac{30^\circ\text{C} - 15^\circ\text{C}}{\ln\left(\frac{30^\circ\text{C}}{15^\circ\text{C}}\right)}$$

$$\text{LMTD} = 21.64^\circ\text{C}$$

$$\text{Heat transfer} = \dot{m}_h c_{ph} (T_{hi} - T_{ho}) = U \cdot A \cdot (\text{LMTD})$$

$$10^3 \times 0.277 \times 2 \times (70 - 40) = 0.2 \times 1000 \times A \times 21.64$$

$$A = 3.84 \text{ m}^2$$

30. (a)

Heat conducted = Heat convected

$$\frac{T_1 - T_2}{\ln\left(\frac{r_2}{r_1}\right)} = h \times 2\pi r_2 \times L \times (T_2 - T_\infty)$$

$$\frac{r_1 - r_2}{2\pi K L}$$

$$r_1 = 1 \text{ m}, r_2 = 1.1 \text{ m}$$

$$\Rightarrow \frac{(200 - T_2) \times 2\pi \times 0.05 \times L}{\ln(1.1/1)} = h \times \pi \times 2.2 \times L \times (T_2 - 20)$$

$$\Rightarrow \frac{(200 - T_2)}{\ln(1.1/1)} \times 0.1 = h \times 2.2 \times (T_2 - 20)$$

$$\Rightarrow 200 - T_2 = 2.097 \times 10 \times (T_2 - 20)$$

$$\Rightarrow 200 - T_2 = 20.97 \times (T_2 - 20)$$

$$\Rightarrow 200 - T_2 = 20.97 T_2 - 419.4$$

$$\Rightarrow T_2 = 28.19^\circ\text{C}$$

