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HYDROLOGY

CIVIL ENGINEERING

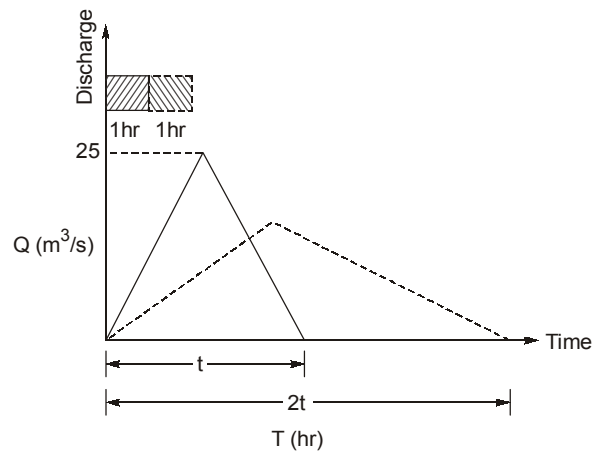
Date of Test : 21/04/2025

ANSWER KEY ➤

- | | | | | |
|--------|---------|---------|---------|---------|
| 1. (b) | 7. (c) | 13. (c) | 19. (b) | 25. (d) |
| 2. (d) | 8. (a) | 14. (a) | 20. (b) | 26. (c) |
| 3. (a) | 9. (d) | 15. (c) | 21. (a) | 27. (d) |
| 4. (a) | 10. (c) | 16. (d) | 22. (d) | 28. (a) |
| 5. (a) | 11. (c) | 17. (b) | 23. (c) | 29. (a) |
| 6. (a) | 12. (a) | 18. (b) | 24. (c) | 30. (c) |

Detailed Explanations

1. (b)



For 2-hr UH, the base time will increase, hence peak will go down.

2. (d)

Certain chemicals such as cetyl alcohol (hexadecanol) and stearyl alcohol (octadecanol) forms monomolecular layers on a water surface. These layers act as evaporation inhibitors by preventing the water molecules to escape past them.

3. (a)

$$\text{Lake evaporation} = C_p \times \text{Pan evaporation}$$

Average value of Pan coefficient C_p

Class A pan	0.70
ISI pan	0.80
Colorado Sunken pan	0.78

So for class A pan, C_p value is the minimum and , so for same lake evaporation, pan evaporation is maximum for class A pan.

4. (a)

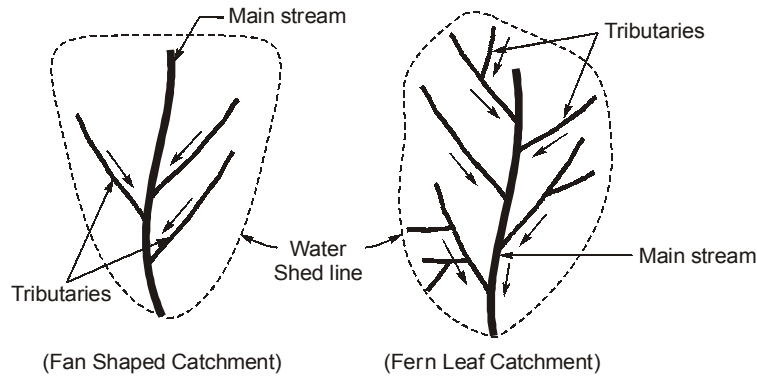
Since variation is more than 10%,

$$\begin{aligned}
 P_x &= \frac{105}{3} \left[\frac{156}{155} + \frac{140}{150} + \frac{104}{120} \right] \\
 &= 98.2 \text{ cm}
 \end{aligned}$$

5. (a)

$$\begin{aligned}
 Q_{\text{equilibrium}} &= 2.78 \frac{A}{T} \\
 &= 2.78 \times 360 \times \frac{1}{4} \simeq 250 \text{ cumecs}
 \end{aligned}$$

6. (a)



7. (c)

The limiting case of a UH of zero duration is known as IUH (Instantaneous Unit Hydrograph). The ordinate of one IUH at any time 't' is the slope of S-curve of intensity 1 cm/hr.

8. (a)

Isopleth is a line on a map connecting points having same numerical values of a certain quantity such as population figure or geographical measurement. Isobars are contour lines that connects different points with same constant pressure. Isochrones are lines on a map connecting points relating to equal time of travel of surface runoff or equal time of concentration.

11. (c)

$$\text{Peak of DRH} = 135 - 10 = 125 \text{ m}^3/\text{s}$$

$$P = 54 \text{ mm}, \quad \phi = 4 \text{ mm/hr}$$

$$\therefore n = P - \phi \times t = 54 - 4 \times 1 = 50 \text{ mm} = 5 \text{ cm}$$

$$\therefore \text{Peak of 1 hr. UH} = \frac{125}{5} = 25 \text{ m}^3/\text{s}$$

12. (a)

$$n = 2 + 3 = 5 \text{ cm}$$

$$\text{For DRH, } (\Sigma O) = (1 + 7 + 26 + 37 + 27 + 13 + 1) - 7 = 105$$

$$n = \frac{0.36 \Sigma O t}{A}$$

$$\Rightarrow A = \frac{0.36 \times 105 \times 1}{5} = 7.56 \text{ km}^2$$

13. (c)

$$P = 5 \times 2 = 10 \text{ cm}$$

$$= 10 \times 10^{-2} \times 100 \times 10^4 = 10^5 \text{ m}^3$$

$$R = 1 \text{ m}^3/\text{s} \times 10 \times 60 \times 60 = 36000 \text{ m}^3$$

$$\therefore \text{Runoff coefficient} = \frac{R}{P} = \frac{36000}{10^5} = 0.36$$

14. (a)

Time (hr)	4-h UH (m ³ /s)	S-curve addition	S-curve	Offset S-curve	Δy	6-h UH = ($\Delta y \times 4/6$)
0	0	—	0	—	0	0
2	9	—	9	—	9	6
4	20	0	20	—	20	13.33
6	35	9	44	0	44	29.33
8	43	20	63	9	54	36
10	22	44	66	20	46	30.67
		63		44		
		66		69		
				66		

15. (c)

$$(i) \quad \text{Mean rainfall, } (\bar{P}) = \frac{\sum P}{n} = \frac{800 + 620 + 400 + 560}{4} = 595 \text{ mm}$$

$$(ii) \quad \text{Standard deviation, } \sigma = \sqrt{\frac{(P - \bar{P})^2}{n - 1}} = 165.23$$

$$(iii) \quad \text{Coefficient of variation, } c_v = \frac{100 \sigma}{\bar{P}} = \frac{100 \times 166.93}{595} = 27.77$$

$$(iv) \quad \text{Optimum number of rain gauges, } (N) = \left(\frac{c_v}{\epsilon} \right)^2 = \left(\frac{28.29}{10} \right)^2 \Rightarrow 7.7113 \approx 8 \text{ Nos}$$

$$(v) \quad \begin{aligned} \text{Additional gauges required to be installed} \\ &= 8 - \text{Existing 4 gauges} \\ &= 8 - 4 = 4 \end{aligned}$$

16. (d)

Time (1)	Total Stream flow in cumecs (2)	Base flow in cumecs (3)	Direct run off = column (2) – 4.8 (4)
0	4.8	4.8	0
2	5.1	4.8	0.3
4	6.5	4.8	1.7
6	7.4	4.8	2.6
8	10.2	4.8	5.4
10	8.8	4.8	4.0
12	7.4	4.8	2.6

Using Simpson's rule, the area enclosed by this discharge hydrograph

$$= \frac{H}{3} \left[\frac{1^{st} + \text{last ordinate}}{2} + 4 \times \text{Even ordinates} + 2 \times \text{odd ordinates} \right]$$

$$= \frac{2 \times 60 \times 60}{3} \left[\frac{0 + 2.6}{2} + 4(0.3 + 2.6 + 4.0) + 2(1.7 + 5.4) \right]$$

$$= 103440 \text{ m}^3$$

$$\therefore \text{Depth of water in the hydrograph} = \frac{103440}{400 \times 10^4} = 2.586 \times 10^{-2} \text{ m or } 2.586 \text{ cm}$$

$$\text{Rainfall} = 4 \text{ cm}$$

$$\text{Runoff} = 2.586 \text{ cm}$$

$$\therefore \text{Infiltration including basin recharge} = 4 - 2.586 = 1.414 \text{ cm}$$

$$t_r = 4 \text{ hr (given)}$$

$$\therefore \phi_{\text{index}} = \frac{1.414}{4} = 0.35 \text{ cm/hr}$$

17. (b)

$$\text{Loss} = \text{Rainfall} - \text{Runoff} = \frac{0.8}{100} \times 6 - \frac{256000}{8.6 \times 10^6} = 0.01823 \text{ m} = 1.823 \text{ cm}$$

$$\text{Rate of loss} = \frac{1.823}{6} = 0.304 \text{ cm/hr}$$

18. (b)

The probability of occurrence of an event ($x \geq x_T$) at least once over a period of n successive years is called the risk, $\bar{R}$.

Hence, risk is given by

$$\begin{aligned}\bar{R} &= 1 - (\text{Probability of occurrence of the event } x \geq x_T \text{ in } n \text{ years}) \\ &= 1 - \left(1 - \frac{1}{T}\right)^n = 1 - \left(1 - \frac{1}{50}\right)^{25} = 0.397 \approx 0.40\end{aligned}$$

where,

T = Return period = 50 years

n = Expected life = 25 years

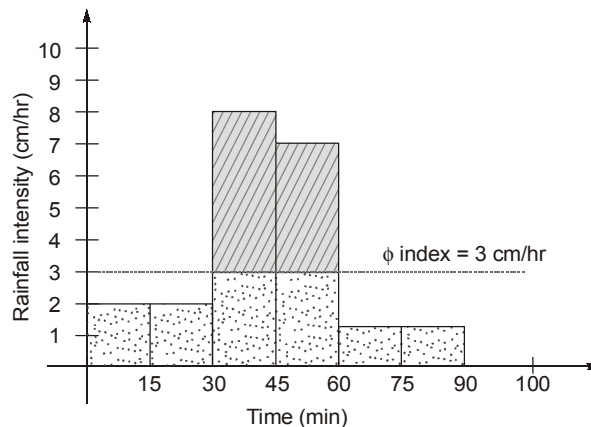
19. (b)

Thiessen Polygon Method: In this method, the rainfall recorded at each station is given a weightage on the basis of an area closest to the station.

$$P_{\text{avg}} = \frac{P_1 A_1 + P_2 A_2 + \dots + P_n A_n}{A_1 + A_2 + \dots + A_n}$$

where, $P_1, P_2, \dots, P_n$ are the rainfall data of areas $A_1, A_2 \dots A_n$.

20. (b)



Hatched portion shows the total runoff and dotted portion shows the total infiltration.

$$\therefore \text{Total runoff} = (8 - 3) \times \frac{15}{60} + (7 - 3) \times \frac{15}{60} = [(8 - 3) + (7 - 3)] \times \frac{15}{60} = 2.25 \text{ cm}$$

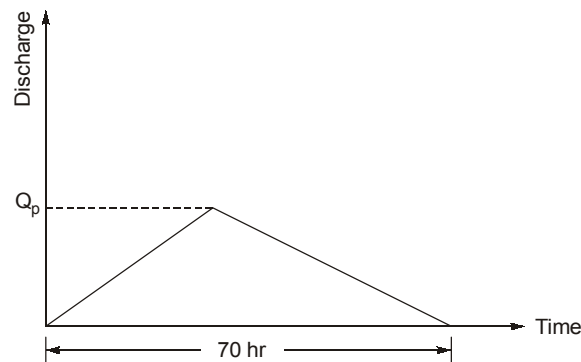
$$\begin{aligned}\text{Total precipitation} &= 2 \times \frac{15}{60} + 2 \times \frac{15}{60} + 8 \times \frac{15}{60} + 7 \times \frac{15}{60} + 1.25 \times \frac{15}{60} + 1.25 \times \frac{15}{60} \\ &= (2 + 2 + 8 + 7 + 1.25 + 1.25) \times \frac{15}{60} = 5.375 \text{ cm}\end{aligned}$$

$$\begin{aligned}W\text{-index} &= \frac{\text{Total precipitation} - \text{Runoff}}{\text{Duration of rainfall in hr}} = \frac{5.375 - 2.25}{90 / 60} \\ &= 2.083 \text{ cm/hr} \approx 2.08 \text{ cm/hr}\end{aligned}$$

24. (c)

Let the peak of the UH be Q_p .

The UH can be shown as



Area of DRH gives the volume of rainfall,

$$\frac{1}{2} \times 70 \times 60 \times 60 \times Q_p = \frac{1}{100} \times 756 \times 10^6$$

$$\Rightarrow Q_p = 60 \text{ m}^3/\text{s}$$

$$\therefore \text{Peak of DRH} = n \times \text{peak of UH} = 5 \times 60 = 300 \text{ m}^3/\text{s}$$

25. (d)

$$\text{Total rainfall} = 0.5 + 1.8 + 2.9 = 5.2 \text{ cm}$$

$$\text{Infiltration} = 5.2 - 2 = 3.2 \text{ cm}$$

$$\text{Excess rainfall duration, } t_e = 2 \times 3 = 6 \text{ hrs.}$$

$$\phi\text{-index} = \frac{3.2}{6} = 0.533 \text{ cm/hr}$$

This value being more than 0.5 cm/hr,

The excess rainfall duration will reduce by 2 hrs.

$$\therefore t_e = 4 \text{ hrs.}$$

$$\text{Infiltration} = (1.8 + 2.9) - 2 = 2.7 \text{ cm}$$

$$\phi\text{-index} = \frac{2.7}{4} = 0.675 \text{ cm/hr}$$

26. (c)

Horton's infiltration equation,

$$f_t = f_f + (f_i - f_f)e^{-k_h t}$$

where,

f_f = Final infiltration capacity

f_i = Initial infiltration capacity

k_h = Decay constant

f_t = Infiltration capacity at any time 't'

$$\text{So, } F = \int_0^t f_t dt = \int_0^t \{f_f + (f_i - f_f)e^{-k_h t}\} dt$$

$$\Rightarrow 18 = \int_0^9 \{1 + (10 - 1)e^{-k_h t}\} dt$$

$$\Rightarrow 18 = \int_0^9 (1 + 9e^{-k_h t}) dt$$

$$\Rightarrow 18 = \left(t + \frac{9e^{-k_h t}}{-k_h} \right)_0^9$$

$$\Rightarrow 18 = \left(9 + \frac{9e^{-k_h \times 9}}{-k_h} \right) - \left(0 + \frac{9}{-k_h} \right)$$

Now $e^{-9k_h} \simeq 0$

$$18 = 9 + \frac{9}{k_h}$$

$$\therefore k_h \simeq 1 \text{ h}^{-1}$$

Alternate Method:

Horton's infiltration equation

$$f_p = f_c + (f_0 - f_c)e^{-k_h t}$$

where,

f_c = Final steady state infiltration capacity

f_0 = Initial infiltration capacity

f_p = Infiltration capacity at any time 't'

k_h = Horton's Decay coefficient

For large value of 't'

The total depth of infiltration is given as

$$F_p = f_c t + \frac{f_0 - f_c}{k_h}$$

Given,

$$f_0 = 10 \text{ cm/h}$$

$$f_c = 1 \text{ cm/hr}$$

$$t = 9 \text{ hr}$$

$$f_p = 18 \text{ cm}$$

$$\therefore 18 = 1 \times 9 + \frac{10 - 1}{k_h}$$

$$k_h = \frac{9}{9} = 1 \text{ hr}^{-1}$$

27. (d)

Time base of both the unit hydrographs is same. Let it be t .

$$\therefore \frac{1}{2} \times 30 \times t \times \frac{1}{235} = \frac{1}{2} \times 90 \times t \times \frac{1}{A_2}$$

$$\Rightarrow A_2 = 235 \times 3$$

$$\Rightarrow A_2 = 705 \text{ km}^2$$

28. (a)

The calculations are tabulated below:

Time (hr)	FH (m ³ /s)	Base Flow (m ³ /s)	DRH (m ³ /s)
Col. (1)	Col. (2)	Col. (3)	Col. (4)
0	5	5	0
12	15	5	10
24	40	5	35
36	80	5	75
48	60	5	55
60	50	5	45
72	25	5	20
84	15	5	10
96	5	5	0
			$\Sigma O = 250$

$$\text{Base flow} = 5 \text{ m}^3/\text{sec}$$

$$\text{Now, direct runoff depth, } DRD = \frac{0.36 \times \Sigma O \times t}{A}$$

where

$$\Sigma O = 250 \text{ m}^3/\text{s}; t = 12 \text{ hr}; A = 450 \text{ km}^2$$

$$\therefore DRD = \frac{0.36 \times 250 \times 12}{450} = 2.4 \text{ cm}$$

29. (a)

The SCS-CN method is based on the water balance equation of the rainfall in a known interval of time Δt .

30. (c)

Time(hr)	0	12	24	36	48
Inflow(m ³ /s)	100	750	780	470	270

$$Q_{\text{initial}} = 100 \text{ m}^3/\text{s}$$

$$k = 18 \text{ hours}$$

$$x = 0.3$$

$$2kx < \Delta t < k$$

$$2 \times 18 \times 0.3 < \Delta t < 18$$

$$\Delta t = 12 \text{ hrs}$$

Using Muskingum equation

$$C_0 = \frac{-kx + 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{-18 \times 0.3 + 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.0323$$

$$C_1 = \frac{kx + 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{18 \times 0.3 + 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.613$$

$$C_2 = \frac{k(1-x) - 0.5 \Delta t}{k(1-x) + 0.5 \Delta t} = \frac{18(1-0.3) - 0.5 \times 12}{18(1-0.3) + 0.5 \times 12} = 0.355$$

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