



MADE EASY

India's Best Institute for IES, GATE & PSUs

ESE 2024 : Mains Test Series

UPSC ENGINEERING SERVICES EXAMINATION

Mechanical Engineering

Test-2 : Heat Transfer + Refrigeration and Air-Conditioning [All Topics]

Thermodynamics-1 + Strength of Materials & Mechanics-1 [Part Syllabus]

Name : RAJESH KASANIYA

Roll No : ME24MBL10044

Test Centres			Student's Signature
Delhi <input type="checkbox"/>	Bhopal <input type="checkbox"/>	Jaipur <input type="checkbox"/>	<u>Rajesh</u>
Pune <input type="checkbox"/>	Kolkata <input type="checkbox"/>	Hyderabad <input type="checkbox"/>	

Instructions for Candidates

1. Do furnish the appropriate details in the answer sheet (viz. Name & Roll No).
2. There are Eight questions divided in TWO sections.
3. Candidate has to attempt FIVE questions in all in English only.
4. Question no. 1 and 5 are compulsory and out of the remaining THREE are to be attempted choosing at least ONE question from each section.
5. Use only black/blue pen.
6. The space limit for every part of the question is specified in this Question Cum Answer Booklet. Candidate should write the answer in the space provided.
7. Any page or portion of the page left blank in the Question Cum Answer Booklet must be clearly struck off.
8. There are few rough work sheets at the end of this booklet. Strike off these pages after completion of the examination.

FOR OFFICE USE

Question No.	Marks Obtained
Section-A	
Q.1	
Q.2	
Q.3	
Q.4	
Section-B	
Q.5	
Q.6	
Q.7	
Q.8	
Total Marks Obtained	

Signature of Evaluator

Cross Checked by

Section : A

Q.1 (a) In a 25 tonnes absorption refrigeration system the heating in generator is carried out by using steam at 3 bar and 90% dry. The refrigeration temperature is -15°C . The condensation of the refrigerant is carried out at 40°C using cooling water. Determine:

- (i) Maximum possible C.O.P. of the system and
 (ii) Quantity of steam required per hour to run the plant if the steam leaves the generator as saturated water at same pressure. Assume relative C.O.P. = 0.35.

From steam tables we have

At 3 bar, $T_{\text{sat}} = 133.5^{\circ}\text{C}$, $h_{fg} = 2163.2 \text{ kJ/kg}$

[12 marks]

Ans

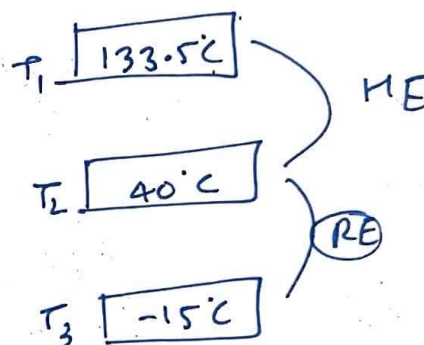
$$R.C. = 25 \times 3.5 = 87.5 \text{ kW}$$

(i) max possible cop

$$(\text{COP})_{\text{max}} = \left(1 - \frac{T_2}{T_1}\right) \left(\frac{T_3}{T_2 - T_3}\right)$$

$$= \frac{93.5}{406.5} \times \frac{256}{65}$$

$$(\text{COP})_{\text{max}} = 0.9058$$



(ii) $(\text{COP})_{\text{act}} = 0.317 = \frac{\dot{Q}_E}{\dot{Q}_G} = \frac{87.5}{\dot{Q}_G}$

$$\Rightarrow \dot{Q}_G = 276.025 \text{ kW}$$

$$\dot{Q}_G = x \dot{m}_s h_{fg}$$

$$\Rightarrow 276.025 = 0.9 \times \dot{m}_s (2163.2)$$

$$\Rightarrow \dot{m}_s = 0.1417 \text{ kg/s}$$

- Q.1 (b) Air at 12°C flows past a flat plate 1.2 m wide and 1.6 m long. The plate is maintained at 88°C temperature and dissipates 3.95 kW of energy. Determine the convective heat transfer coefficient and the velocity at which air flows along the length of the plate. At the mean temperature of 50°C, the thermo-physical properties of air are:
 $\rho = 1.09 \text{ kg/m}^3$; $k = 0.028 \text{ W/m}^\circ\text{C}$; $\text{Pr} = 0.73$; $c_p = 1007.5 \text{ J/kgK}$
and $\mu = 2.029 \times 10^{-5} \text{ kg/m-s}$

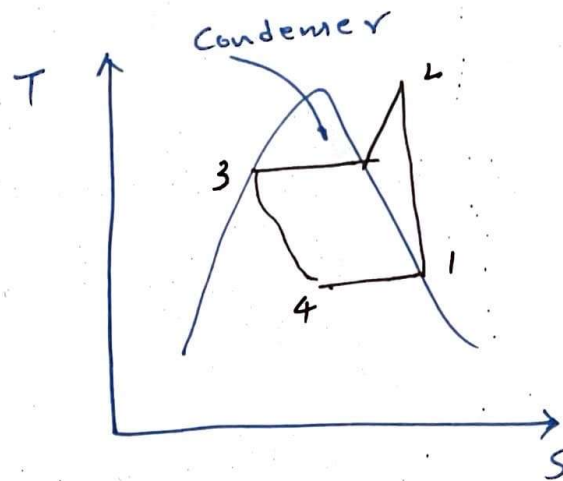
Use the following correlations if required:

$$Nu = \frac{hl}{k} = 0.664(\text{Re})^{0.5}(\text{Pr})^{0.33} \text{ for laminar flow}$$

$$= \frac{hl}{k} = [0.036(\text{Re})^{0.8} - 836](\text{Pr})^{0.33} \text{ for turbulent flow}$$

[12 marks]

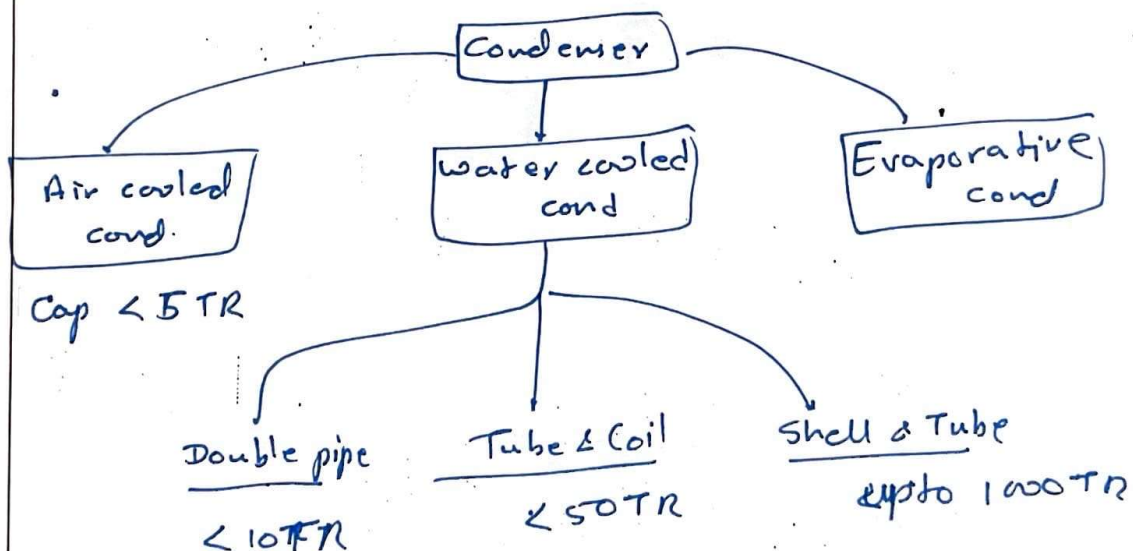
- Q.1 (c) What are the functions of condenser in a refrigerating machine? Name different types of condensers. Describe with neat sketch the evaporative condenser. [12 marks]



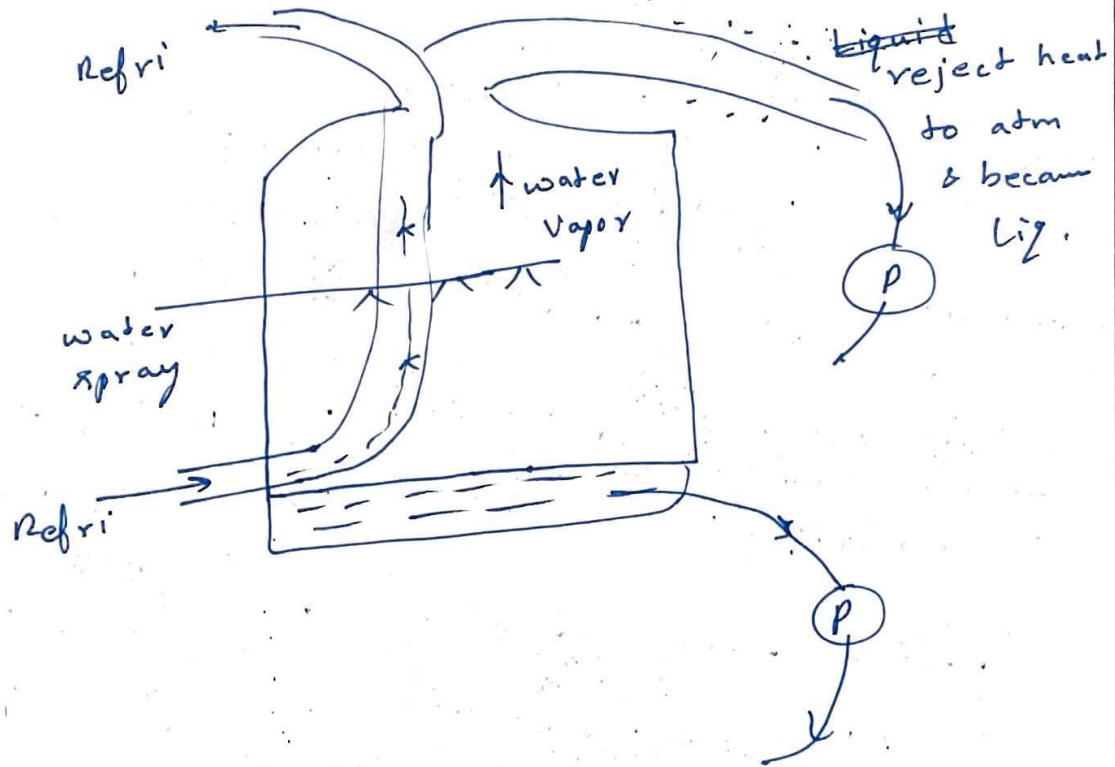
VCRS

Functions

- ① Liquidify the refrigerent by rejecting heat (at const P)



Evaporative cool - Refrigerant cooled by water & then water rejects heat to air & liquidify.



- Q.1 (d) Saturated steam at 120°C flows inside a copper pipe of thermal conductivity 450 W/mK , having an internal diameter of 12 cm and external diameter of 14 cm . The surface resistance on the steam side is $11500 \text{ W/m}^2\text{K}$ and that on the outside surface of pipe is $20 \text{ W/m}^2\text{K}$. Determine the heat loss from the pipe if it is located in space at 30°C . How this heat loss would be affected if the pipe is lagged with 3 cm thick insulation of thermal conductivity 0.20 W/mK ?

[12 marks]

Ans

Find
 $Q_{\text{loss}} = ?$

Assumption

- ① $L = 1 \text{ m}$
- ② neglecting convective heat transfer w/o insulation

Given

Air 30°C

Steam 120°C

$T_{\text{steam}} = 120^\circ\text{C}$

$K_{\text{cu}} = 450 \text{ W/mK}$

$r_i = 6 \text{ cm}$

$r_o = 7 \text{ cm}$

$R_i = 11500 \text{ W/m}^2\text{K}$

$R_o = 20 \text{ W/m}^2\text{K}$

$A_i = \frac{2\pi r_i L}{1} = 0.3769 \text{ m}^2$

$A_o = 0.4398 \text{ m}^2$

120°C

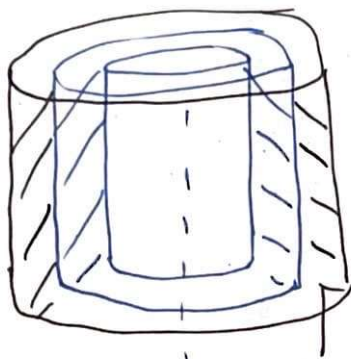
30°C

$q = \frac{\Delta T}{R_{\text{total}}} = \frac{90}{\frac{1}{11500 A_i} + \frac{\ln(7/6)}{2\pi L \times 450} + \frac{1}{20 A_o}}$

$\Rightarrow q = \frac{90}{0.05014} = 1789.658 \text{ W}$

$Q_{\text{loss}} = q = 1789.658 \text{ W}$

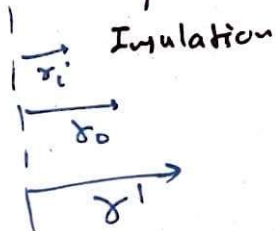
Heat loss from pipe w/o insulation.



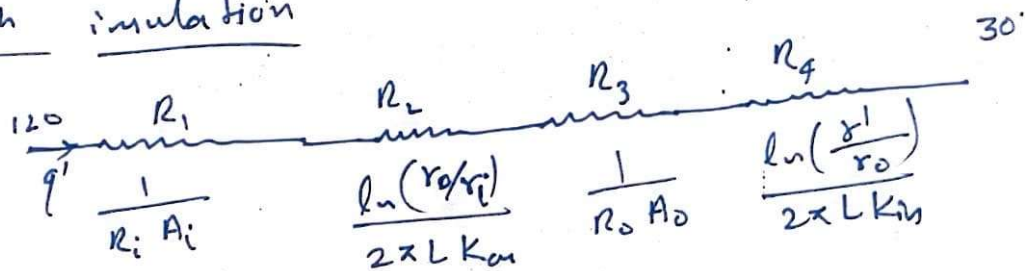
$$t = 3 \text{ cm}$$

$$r_1 = r_o + 3 = 10 \text{ cm}$$

$$K_{\text{ins}} = 0.2 \text{ W/mK}$$



with insulation



$$\Rightarrow q' = \frac{\Delta T}{R_{\text{total}}} = \frac{90}{\frac{1}{11500 \times 0.7763} + \frac{\ln(7/6)}{2\pi L \times 0.2} + \frac{1}{20 \times 0.4338} + \frac{\ln(10/7)}{2\pi L \times 0.2}}$$

$$\Rightarrow q' = \frac{90}{0.3978}$$

$$\Rightarrow \boxed{q' = 226.2427 \text{ W}}$$

Heat loss with insulation

$$\boxed{q - q' = 563.4153 \text{ W}}$$

So by adding insulation if we neglect convection HT then 563.4153 W heat loss will be less.

- Q.1 (e) Saturated air at 5°C is required to be supplied to a room where the temperature must be held at 21°C with a relative humidity of 55%. The air is heated and then water is sprayed to give the required humidity. Determine the mass of spray water required per m^3 of air at room conditions. Assume that the total pressure is constant at 1.0132 bar. (Refer steam table for the properties of water vapour in moist air)

[12 marks]

- Q.2 (a) The following data refer to a steam jet refrigeration system:
- Condition of the motive steam = 10 bar, dry saturated
 - Temperature of water in the flash chamber = 6°
 - Temperature at which the make up water is supplied = 22°
 - The pressure at which condenser is operated = 0.06 bar
 - Nozzle efficiency = 0.85
 - Entrainment efficiency = 0.65
 - Compression efficiency = 0.8
 - The quality of steam and flash vapour at beginning of compression = 0.9
- Determine the following:
- (i) Mass of motive steam required per kg of flash vapour.
 - (ii) Refrigerating effect per kg of flash vapour.
 - (iii) The coefficient of performance of the system.
- [Refer steam table for properties of steam]

[20 marks]

- Q.2 (b)** A hemispherical cavity of radius 0.8 m is covered with a plate having a hole of 0.3 m diameter. The inner surface of the plate is maintained at 560 K by a heater embedded in the surface. Assuming the surfaces to be black and the hemisphere to be well insulated. Calculate:
- (1) the temperature of the surface of the hemisphere
 - (2) the power input to the heater.

[20 marks]

Q.2 (c) Ambient conditions for an aircraft cruising at 1200 km/h are 0.35 bar and -15°C . The cabin temperature is 25°C and turbine exit pressure is 1.06 bar. The pressure ratio of compressor is 5.0. Assuming 100 percent efficiency of ram effect, compressor and turbine and ideal heat exchanger, determine for simple gas refrigeration cycle of 30 tonnes capacity.

- (i) Temperatures and pressures at all points of cycle.
- (ii) Mass flow rate and volume flow rate at compressor inlet and turbine outlet.
- (ii) Work requirement
- (iv) Coefficient of performance of cycle.

Assume : $c_p = 1.005 \text{ kJ/kgK}$, $R_{\text{air}} = 0.286 \text{ kJ/kgK}$, $\gamma = 1.4$

[20 marks]

- Q.3 (a) (i) List the assumptions made while analysing the heat flow from a finned surface.
- (ii) A turbine blade 6 cm long, 4.8 cm^2 cross-sectional area and 12 cm perimeter is made of stainless steel of thermal conductivity 110 kJ/m-hr-deg . The temperature at the root of the blade is 520°C and it is exposed to products of combustion passing through the turbine at 880°C . The film coefficient between the blade and the combustion gases is $1200 \text{ kJ/m}^2\text{-hr-deg}$. Determine the temperature at the middle of blade and the rate of heat flow from it. The blade may be treated as a fin losing heat at the tip.

[6 + 14 marks]

①

Assumptions

- ① Thermal conductivity (k) is const for fin over entire length
- ② h (Heat transfer coeff) is const.
- ③ No resistance at junction of fin and base material
- ④ No radiative heat transfer from fin

Q.3 (b) A Freon-12 VCRS installation has the following data:

Refrigeration capacity = 20 tons

Evaporator temperature = -10°C

Condenser temperature = 30°C

Temperature of refrigerant superheated as gas in evaporator = -5°C

Temperature of refrigerant subcooled as liquid in condenser = 25°C

Compressor particulars:

Number of cylinders = 2

Stroke = 1.5 times the bore

r.p.m. = 1200

Determine the following:

- (i) refrigerating effect per kg
- (ii) theoretical power
- (ii) coefficient of performance
- (iv) bore and stroke and compressor

Saturation temperature $t_s^{\circ}\text{C}$	Absolute pressure p bar	Specific volume v_g m ³ /kg	Enthalpy of liquid h_f kJ/kg	Enthalpy of vapour h_g kJ/kg	Entropy of liquid s_f kJ/kg $^{\circ}\text{K}$	Entropy of vapour s_g kJ/kg $^{\circ}\text{K}$
-10	2.1928	0.07702	190.72	347.96	0.96561	1.5632
+30	7.4457	0.02372	229.11	364.96	1.0999	1.5481

Take: Liquid specific heat, $c_{pl} = 0.963$ kJ/kgK

Vapour specific heat $c_{pv} = 0.615$ kJ/kgK

[20 marks]

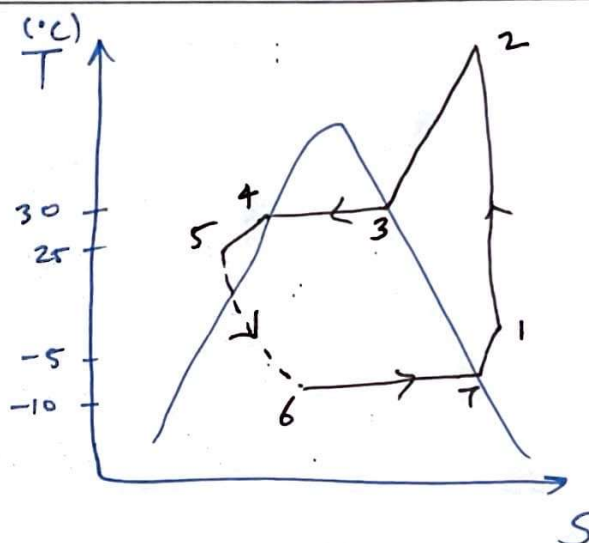
Ans

$$RC = 20 \times 3.5 = 70 \text{ kW}$$

$$K = 2$$

$$L = 1.5 \text{ D}$$

$$N = 1200 \text{ rpm}$$



(i)

$$RE = \frac{RC}{\dot{m}}$$

$$\eta_{vol} = \frac{\dot{m} v_1}{\frac{\pi D^3 L N K}{4 \times 60}} = 1$$

Assumptions

$$\textcircled{1} \eta_{vol} = 1$$

$$\frac{v_1}{v_7} = \frac{T_1}{T_7} \quad (\because \text{const } P) \quad \textcircled{2} \text{ Bore } D = 0.1 \text{ m}$$

$$\Rightarrow v_1 = 0.07040 \text{ m}^3/\text{kg}$$

$$\Rightarrow \dot{m} (0.07040) = \frac{\pi}{4} 1.5 D^3 \times \frac{1200}{60} \times 2$$

$$\Rightarrow \dot{m} =$$

- Q.3 (c) An existing heat exchanger of 24 m^2 surface area is to be used to condense low pressure steam. The cooling medium will be feed water available at 42°C , its flow rate being 0.94 kg/s . The overall heat transfer coefficient is estimated at $130 \text{ W/m}^2\text{K}$.

Calculate the quantity of steam condensed and the exit temperature of the feed water. At the condensing pressure steam has saturation temperature of 100°C and latent heat of vapourisation is 2257 kJ/kgK . Assume that the steam is initially just saturated and that the condensate leaves the exchanger without sub-cooling. How would the performance of the exchanger be affected if the overall heat transfer coefficient can be doubled by a modification of feed water flow through the exchanger? Take C_p of water 4.187 kJ/kgK .

[20 marks]

- Q.4 (a) 900 kg/hr of cream cheese at 16°C is pumped through 1.6 m length of 9 cm inner diameter tube which is maintained at 98°C. Determine the temperature of cheese leaving the heated section and the rates of heat transfer from the tube to the cheese. The relevant thermo-physical properties of cheese are : $\rho = 1150 \text{ kg/m}^3$; $\mu = 22.5 \text{ kg/m-s}$; $c_p = 2750 \text{ J/kgK}$; $k = 0.42 \text{ W/mK}$. Use the following correlation for laminar flow inside a tube

$$Nu = \frac{h d}{k} = 3.65 + \frac{0.067 \frac{d}{l} Re Pr}{1 + 0.04 \left(\frac{d}{l} Re Pr \right)^{0.67}}$$

[20 marks]

- Q.4 (b) Air flowing at the rate of $120 \text{ m}^3/\text{min}$ at 40°C DBT and 50% RH is mixed with another stream flowing at the rate of $60 \text{ m}^3/\text{min}$ at 26°C DBT and 50% RH. The mixture flows over a cooling coil, whose ADP temperature is 10°C and by-pass factor is 0.2. Determine DBT and RH of air leaving the coil. If this air is supplied to an air-conditioned room where DBT of 26°C and RH of 50% are maintained estimate room sensible heat factor and cooling load capacity of the coil in tonnes of refrigeration.

[Refer Psychrometric chart attached]

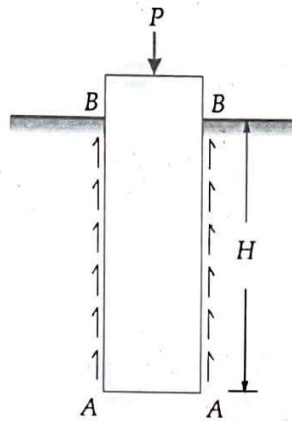
[20 marks]

- Q.4 (c) (i) During heat treatment, cylindrical pieces of 26 mm diameter, 32 mm height and at 30°C are placed in a furnace at 760°C with convection coefficient $84 \text{ W/m}^2\text{-K}$. Calculate the time required to heat the pieces to 620°C . What will be the shortfall in temperature if the pieces are taken out from the furnace after 270 seconds? Assume the following property values : $\rho = 7850 \text{ kg/m}^3$; $C_p = 480 \text{ J/kgK}$; $K = 42 \text{ W/m-K}$.
- (ii) Draw a typical boiling curve for pool boiling of water at saturation temperature and atmospheric pressure. Mark each boiling regime and explain briefly its various regimes.

[10 + 10 marks]

Section : B

- Q.5 (a) A pile of uniform section is embedded in soil by a depth H . The pile supports a structural load P at its top which is transferred to the soil entirely by friction as shown in figure below. The variation of friction (f) along the depth of the pile is given by $f = ky^2$, where y is the elevation above the bottom of the pile. Determine the shortening of the pile.

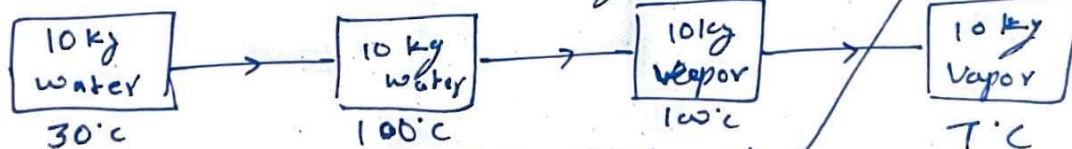
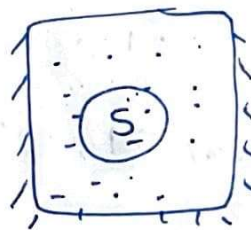


[12 marks]

- Q.5 (b) A lump of steel of mass 15 kg at 800°C is dropped in 10 kg of water at 30°C contained in an insulated container which is open to the atmosphere. If the specific heat of steel and water are 0.5 kJ/kgK and 4.27 kJ/kgK respectively and latent heat of vaporization of water at 100°C is 2257 kJ/kg, then calculate the change in entropy of steel, water and the universe.

[12 marks]

$$\begin{aligned}
 m_s &= 15 \text{ kg} & m_w &= 10 \text{ kg} \\
 T_{s1} &= 800^\circ\text{C} & T_{w1} &= 30^\circ\text{C} \\
 c_s &= 0.5 \text{ kJ/kgK} & c_w &= 4.27 \text{ kJ/kgK} \\
 & & LH &= 2257 \text{ kJ/kg}
 \end{aligned}$$



$$\begin{aligned}
 \Phi_1 &= 10 \times 4.27 \times 70 + 10 \times 2257 + \dots \\
 &= 2989 + 22570 > \Phi_2
 \end{aligned}$$



$$\begin{aligned}
 \Phi_2 &= 15 \times 0.5 \times 700 \\
 &= 5250 \text{ kJ}
 \end{aligned}$$

$\therefore Q_1 > Q_2$
 \hookrightarrow So only a fraction of water will be evaporated.

Heat rejected by steam = Heat gained by H_2O

$$\Rightarrow 5250 = 2989 + m' \times 2257$$

$$\Rightarrow \boxed{m' = 1.017 \text{ kg}} \rightarrow \text{water converted into vapor.}$$

$$\begin{aligned} (\Delta S)_{\text{steel}} &= m_s c_s \ln \frac{T_f}{T_{s1}} \\ &= 15 \times 0.5 \ln \left(\frac{373}{1073} \right) \end{aligned}$$

$$\boxed{(\Delta S)_{\text{steel}} = -7.9247 \text{ kJ/K}} \quad \text{Ans}$$

$$\begin{aligned} (\Delta S)_{\text{water}} &= m_w c_w \ln \left(\frac{T_f}{T_{w1}} \right) + \frac{m' L}{373} \\ &= 10 \times 4.27 \ln \left(\frac{373}{303} \right) + \frac{2261}{373} \end{aligned}$$

$$\Rightarrow \boxed{(\Delta S)_{\text{water}} = 14.9366 \text{ kJ/K}} \quad \text{Ans}$$

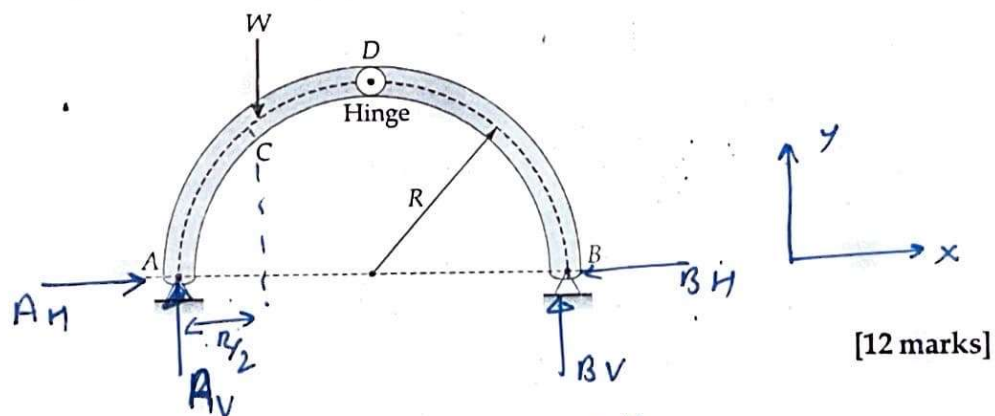
Assumptions

① There is no heat transfer to the atmosphere

$$\Delta S_{\text{univ}} = (\Delta S)_s + (\Delta S)_w + (\Delta S)_{su} \rightarrow 0$$

$$\Rightarrow \boxed{(\Delta S)_{\text{univ}} = 7.0119 \text{ kJ/K}} \quad \text{Ans}$$

- Q.5 (c) A 3-hinged arch loaded at C, at a distance $\frac{R}{2}$ from A. Find the resultant forces at A and B as shown in figure below.



[12 marks]

Force equil of arch in y dirⁿ

$$\sum F_y = 0$$

$$\Rightarrow \boxed{A_V + B_V = W} \quad \text{--- ①}$$

in x-dirⁿ

$$\sum F_x = 0$$

$$\Rightarrow \boxed{A_H = B_H} \quad \text{--- ②}$$

Now by

$$\Sigma M_A = 0$$

$$\Rightarrow -W \frac{R}{2} + B_v \times 2R = 0$$

$$\Rightarrow \boxed{B_v = \frac{W}{4}}$$

from eqn (1)

$$\boxed{A_v = \frac{3W}{4}}$$

Now taking moment in right side of hinge D

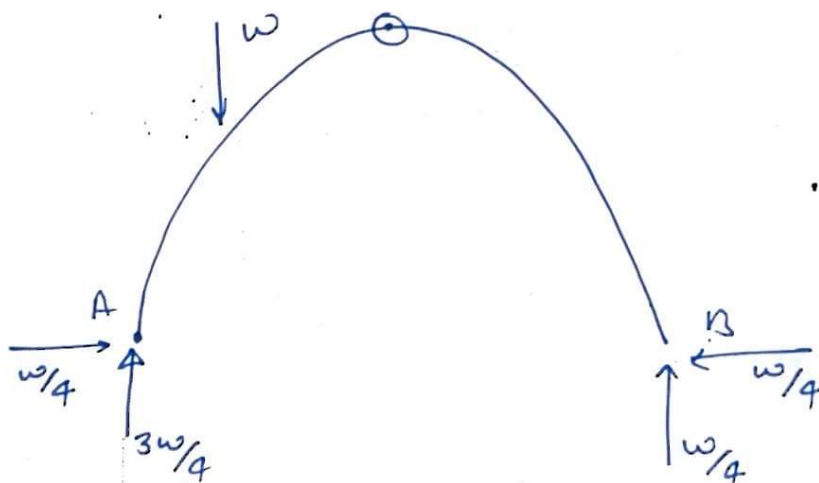
$$\Sigma M_{Dn} = 0$$

$$\Rightarrow +B_v R - B_H R = 0$$

$$\Rightarrow \boxed{B_H = B_v = \frac{W}{4}}$$

from eqn (2)

$$\boxed{A_H = \frac{W}{4}}$$



So Resultant at A

$$F_A = \sqrt{\left(\frac{w}{4}\right)^2 + \left(\frac{3w}{4}\right)^2} = 0.7905 w$$

$$\Rightarrow \boxed{F_A = 0.7905 w} \underline{\underline{\text{Ans}}}$$

Resultant at B

$$F_B = \sqrt{\left(\frac{w}{4}\right)^2 + \left(\frac{w}{4}\right)^2}$$

$$\Rightarrow \boxed{F_B = 0.3535 w} \underline{\underline{\text{Ans}}}$$

Q.5 (d) State and prove Clausius inequality.

[12 marks]

Clausius Inequality :-

$$\boxed{\oint \frac{\delta Q}{T} \leq 0}$$

According to clausius in a ~~thermo~~ cyclic process ratio of differential heat transfer to temp at which this is taking place, over entire cycle will be less than or equal to zero

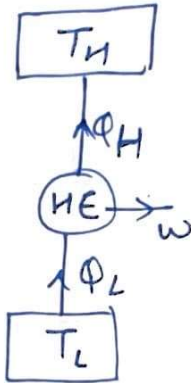
$$\rightarrow \oint \frac{\delta Q}{T} = 0 \rightarrow \text{for reversible}$$

$$\oint \frac{\delta Q}{T} < 0 \rightarrow \text{for irreversible.}$$

Proof (a) for reversible reversible

Assume a carnot ^ HE working b/w two thermal reservoirs T_H & T_L

we know that,



$$\eta = 1 - \frac{T_L}{T_H} = \frac{w}{Q_L} \quad \text{--- (1)}$$

from 1st law

$$w = Q_H - Q_L$$

from eqnⁿ (1)

$$1 - \frac{T_L}{T_H} = \frac{Q_H - Q_L}{Q_L}$$

$$\Rightarrow \frac{T_H}{T_L} = \frac{-Q_H}{Q_L} \Rightarrow -\frac{Q_H}{T_H} = \frac{Q_L}{T_L} \quad \text{--- (2)}$$

$$\Rightarrow \frac{Q_H}{T_H} + \frac{Q_L}{T_L} = 0$$

$$\Rightarrow \oint \frac{\delta Q}{T} = 0 \quad \text{--- for reversible HE (HP)}$$

(b) for irreversible Assume Q_L same as last case

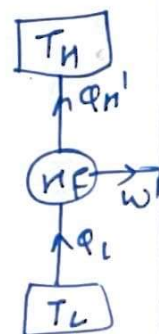
If engine is irreversible then it will do less work
 $\hookrightarrow Q_H'$ will be higher then last case ($Q_H' > Q_H$)

$$Q_H' - Q_H = Q_{diff} \quad \text{--- (3) (Assume)}$$

from 1st law

$$Q_H' = Q_L + w'$$

$$Q_{diff} > 0$$



from eqnⁿ (2) & (3)

$$-\frac{(\Phi_H' - \Phi_{DH})}{T_H} = \frac{\Phi_L}{T_L}$$

$$\Rightarrow \frac{\Phi_H'}{T_H} + \frac{\Phi_L}{T_L} = \frac{\Phi_{DH}}{T_L} > 0 \quad (\because \Phi_{DH} > 0)$$

$$\Rightarrow \boxed{\oint \frac{\delta Q}{T} > 0} \rightarrow \text{for irreversible HE HP}$$

So,

$$\Rightarrow \boxed{\oint \frac{\delta Q}{T} \geq 0}$$

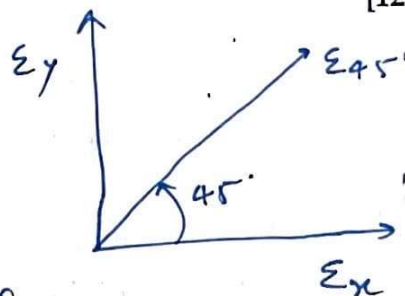
Clausius inequality

- Q.5 (e) A rectangular strain rosette strain gauge records the following values for linear strain at a point in two dimensional stress system : $e_x = 520 \times 10^{-6}$, $e_y = -140 \times 10^{-6}$, and $e_{45^\circ} = 270 \times 10^{-6}$, the later being at 45° to the x and y axes. Calculate the principal strain and stresses. Take $E = 205 \text{ GPa}$ and $\mu = 0.32$.

[12 marks]

Find

$$\begin{cases} \sigma_{1,2} = ? \\ \epsilon_{1,2} = ? \end{cases}$$



We know that

$$\epsilon_{x'} = \left(\frac{\epsilon_x + \epsilon_y}{2} \right) + \left(\frac{\epsilon_x - \epsilon_y}{2} \right) \cos 2\theta + \frac{\phi_{xy}}{2} \sin 2\theta$$

by putting values

$$270 \times 10^{-6} = \left(\frac{520 \times 10^{-6} - 140 \times 10^{-6}}{2} \right) + \left(\frac{520 \times 10^{-6} + 140 \times 10^{-6}}{2} \right) \cos 90^\circ + \frac{\phi_{xy}}{2} \sin 90^\circ$$

$$\Rightarrow 270 \times 10^{-6} = 190 \times 10^{-6} + \frac{\phi_{xy}}{2}$$

$$\Rightarrow \boxed{\Phi_{xy} = 160 \times 10^{-6}}$$

Now,

$$\varepsilon_{1,2} = \frac{\varepsilon_x + \varepsilon_y}{2} \pm \sqrt{\left(\frac{\varepsilon_x - \varepsilon_y}{2}\right)^2 + \left(\frac{\Phi_{xy}}{2}\right)^2}$$

$$\Rightarrow \varepsilon_{1,2} = \left[\frac{520 - 140}{2} \pm \sqrt{\left(\frac{520 + 140}{2}\right)^2 + \left(\frac{160}{2}\right)^2} \right] \times 10^{-6}$$

$$\Rightarrow \varepsilon_{1,2} = (190 \pm 339.5585) \times 10^{-6}$$

$$\Rightarrow \boxed{\varepsilon_1 = 529.5585 \times 10^{-6}}$$

$$\& \boxed{\varepsilon_2 = -149.5585 \times 10^{-6}} \quad \underline{\underline{Ans}}$$

Now

$$\varepsilon_1 = \frac{\sigma_1}{E} - \mu \frac{\sigma_2}{E} \quad \& \quad \varepsilon_2 = \frac{\sigma_2}{E} - \mu \frac{\sigma_1}{E} \quad \text{--- (2)}$$

$$\Rightarrow \mu \varepsilon_1 = \frac{\mu \sigma_1}{E} - \mu^2 \frac{\sigma_2}{E} \quad \text{--- (1)}$$

eqn (1) + (2)

$$\Rightarrow \mu \varepsilon_1 + \varepsilon_2 = \frac{\sigma_2}{E} - \mu^2 \frac{\sigma_2}{E}$$

$$\Rightarrow \sigma_2 = \frac{E}{1 - \mu^2} (\varepsilon_2 + \mu \varepsilon_1)$$

$$\Rightarrow \sigma_2 = \frac{205 \times 10^9}{1 - (0.32)^2} (-149.558 + 0.32 \times 529.5585) \times 10^{-6}$$

$$\Rightarrow \sigma_2 = 4544.9477 \times 10^3 \text{ Pa}$$

$$\Rightarrow \boxed{\sigma_2 = 4.545 \text{ MPa}} \quad \underline{\underline{\text{Ans}}}$$

& similarly

$$\sigma_1 = \frac{E}{1 - \mu^2} (\epsilon_1 + \mu \epsilon_2)$$

$$\Rightarrow \sigma_1 = \frac{205 \times 10^9}{1 - (0.32)^2} (529.5585 + 0.32(-149.5585)) \times 10^{-6}$$

$$\Rightarrow \sigma_1 = 110013.8750 \times 10^3 \text{ Pa}$$

$$\Rightarrow \boxed{\sigma_1 = 110.014 \text{ MPa}} \quad \underline{\underline{\text{Ans}}}$$

So,

$$\left[\begin{array}{l} \epsilon_1 = 529.5585 \times 10^{-6} \\ \epsilon_2 = -149.5585 \times 10^{-6} \\ \sigma_1 = 110.014 \text{ MPa} \\ \sigma_2 = 4.545 \text{ MPa} \end{array} \right] \quad \underline{\underline{\text{Ans}}}$$

- Q.6 (a) A compound cylinder, formed by shrinking one tube on to another, is subjected to an internal pressure of 60 MPa. Before the fluid is admitted, the internal and external diameters of the compound cylinder are 120 mm and 220 mm, and the diameter at the junction is 180 mm. If after shrinkage, the radial pressure at the common surface is 10 MPa, calculate the final stresses set-up by the section.

[20 marks]

Ans

Given

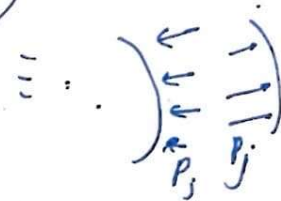
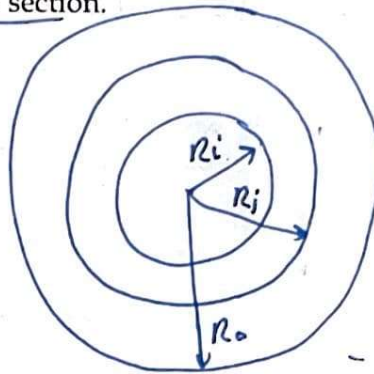
$$P_i = 60 \text{ MPa}$$

$$R_i = 60 \text{ mm}$$

$$R_o = 110 \text{ mm}$$

$$R_j = 90 \text{ mm}$$

$$P_j = 10 \text{ MPa}$$



Case 1] w/o effect of fluid P_i

for inner cyl

Radial Pressure intensity

$$P_r = \frac{B}{r^2} - A$$

$$\text{at } r = R_j; P_r = 0 \Rightarrow$$

$$r = R_j; P_r = P_j = 10$$

from eqnⁿ ① & ②

$$\Rightarrow \begin{cases} B = -64800 \\ A = -18 \end{cases}$$

So, hoop stress

$$\sigma_h = \frac{B}{r^2} + A$$

$$\sigma_{hj} = \frac{-64800}{90^2} - 18 \Rightarrow \sigma_{hj} = -26 \text{ MPa}$$

$$\sigma_{hi} = \frac{-64800}{60^2} - 18 \Rightarrow \sigma_{hi} = -36 \text{ MPa}$$

for outer cyl

$$P_r = \frac{B}{r^2} - A$$

$$\text{at } r = R_i ; P_r = 10 \Rightarrow 10 = \frac{B}{90^2} - A \quad \text{--- (3)}$$

$$r = R_o ; P_r = 0 \Rightarrow 0 = \frac{B}{110^2} - A \quad \text{--- (4)}$$

from (3) & (4)

$$\Rightarrow \boxed{B = 245025}$$

$$\Delta \quad \boxed{A = 20.25}$$

So, hoop stress

$$\sigma_h = \frac{B}{r^2} + A$$

$$\sigma_{hi} = \frac{245025}{90^2} + 20.25 \Rightarrow \boxed{\sigma_{hi} = 50.5 \text{ MPa}}$$

$$\sigma_{ho} = \frac{245025}{110^2} + 20.25 \Rightarrow \boxed{\sigma_{ho} = 40.5 \text{ MPa}}$$

Case 2 for internal pressure P_i

$$P_r = \frac{B}{r^2} - A$$

$$\text{at } r = R_i ; P_r = P_i$$

$$r = R_o ; P_r = 0$$

$$6 = \frac{B}{60^2} - A \quad \text{--- (5)}$$

$$0 = \frac{B}{110^2} - A \quad \text{--- (6)}$$

from eqn (5) & (6)

$$\boxed{B = 51247.6588}$$

$$\boxed{A = 4.2353}$$

$$\boxed{B = 307402.3529}$$

$$\boxed{A = 25.4117}$$

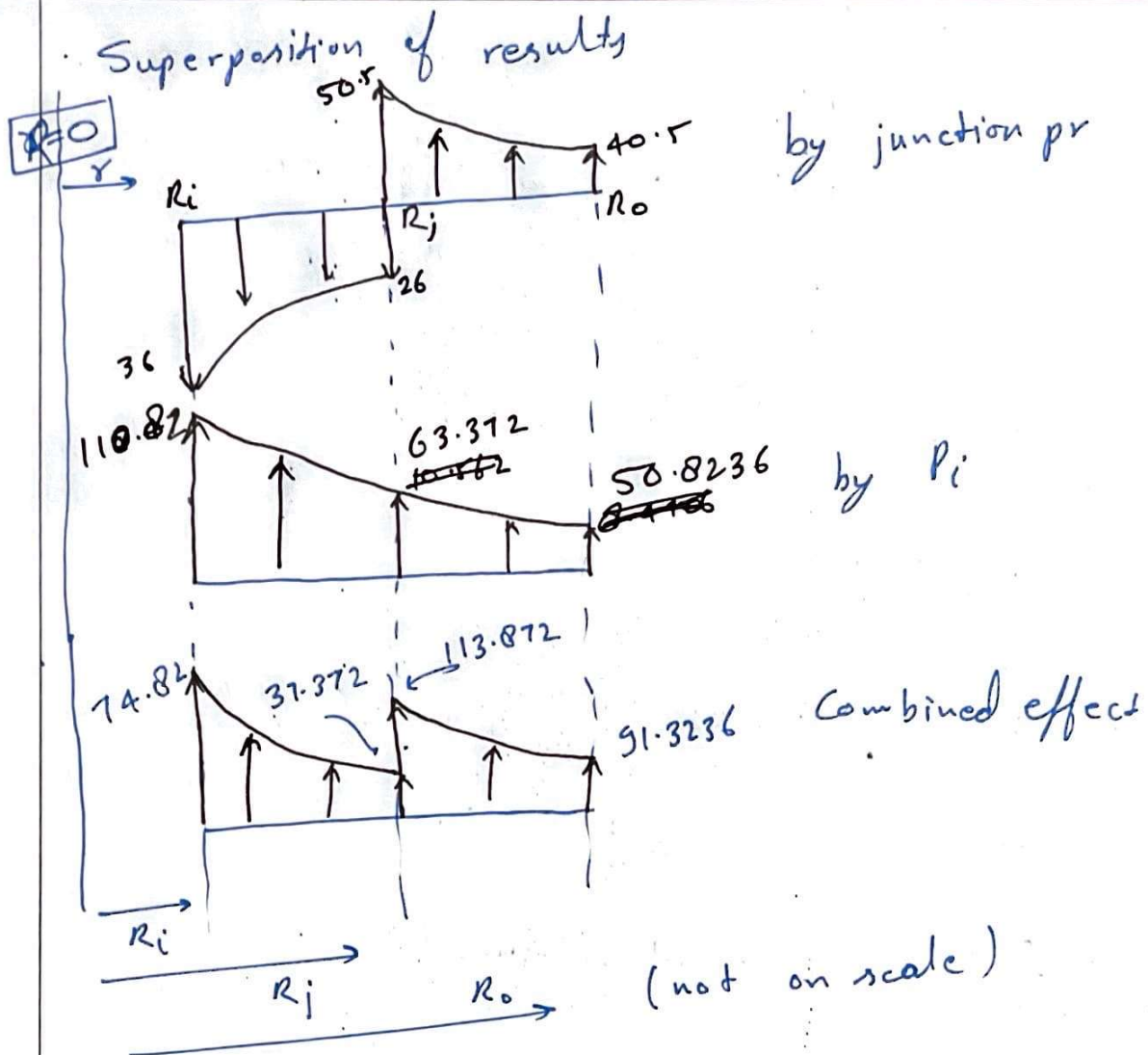
So, hoop stress

$$\sigma_h = \frac{B}{r^2} + A$$

$$\sigma_{hi} = \frac{51247.6588}{60^2} + 4.2353 \Rightarrow \boxed{\sigma_{hi} = 110.823 \text{ MPa}}$$

$$\sigma_{hj} = \frac{B}{90^2} + A \Rightarrow \boxed{\sigma_{hj} = 63.572 \text{ MPa}}$$

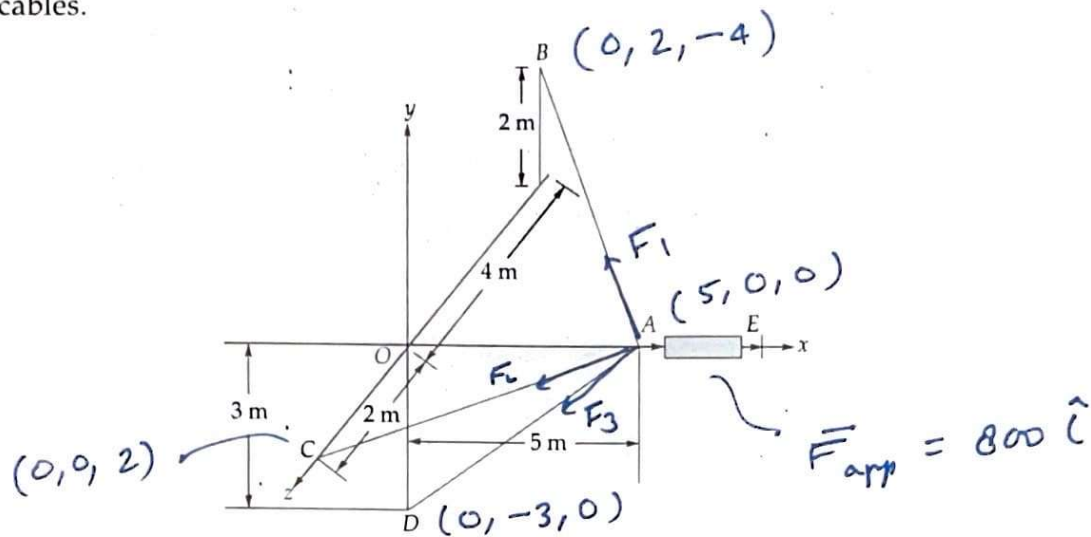
$$\sigma_{ho} = \frac{B}{110^2} + A \Rightarrow \boxed{\sigma_{ho} = 50.8235 \text{ MPa}}$$



So, final stresses

$$\left. \begin{aligned} \sigma_{hi} &= 74.823 \text{ MPa} \\ (\sigma_{hj})_i &= 37.372 \text{ MPa} \\ (\sigma_{hj})_o &= 113.872 \text{ MPa} \\ \sigma_{ho} &= 91.3236 \text{ MPa} \end{aligned} \right\} \underline{\underline{A_m}}$$

- Q.6 (b) A system of 3 cables AB, AC and AD shown in figure below is subjected to a force of 800 kN along the x-direction by turn buckle AE. Calculate the forces developed in the cables.



• unit vector in AB dirⁿ

[20 marks]

$$\hat{A}B = \frac{(0\hat{i} + 2\hat{j} - 4\hat{k}) - (5\hat{i} + 0\hat{j} + 0\hat{k})}{|\vec{AB}|}$$

$$\Rightarrow \hat{A}B = \frac{-5\hat{i} + 2\hat{j} - 4\hat{k}}{\sqrt{5^2 + 2^2 + 4^2} \rightarrow 6.1082}$$

$$\Rightarrow \hat{A}B = \frac{-5\hat{i} + 2\hat{j} - 4\hat{k}}{\sqrt{5^2 + 2^2 + 4^2} \rightarrow 6.1082}$$

$$\Rightarrow \hat{A}B = -0.7454\hat{i} + 0.2981\hat{j} - 0.5962\hat{k}$$

$$\hat{A}C = \frac{(0, 0, 2) - (5, 0, 0)}{|\vec{AC}|} = \frac{(-5, 0, 2)}{\sqrt{25 + 4}}$$

$$\hat{A}C = -0.9285\hat{i} + 0\hat{j} + 0.3714\hat{k}$$

$$\hat{A}D = \frac{(0, -3, 0) - (5, 0, 0)}{|\vec{AD}|} = \frac{(-5, -3, 0)}{\sqrt{25 + 9}}$$

$$\Rightarrow \hat{A}D = -0.8575\hat{i} - 0.5145\hat{j} + 0\hat{k}$$

$$\text{So, } \vec{F}_1 = \hat{F}_1 (\hat{A} \hat{B})$$

$$\Rightarrow \vec{F}_1 = [-0.7454\hat{i} + 0.2981\hat{j} - 0.5962\hat{k}] F_1 \quad \text{--- (1)}$$

Similarly

$$\vec{F}_2 = [-0.9285\hat{i} + 0.3714\hat{k}] F_2 \quad \text{--- (2)}$$

$$\Delta \vec{F}_3 = [-0.8575\hat{i} - 0.5145\hat{j}] F_3 \quad \text{--- (3)}$$

In equilibrium

$$(\sum \vec{F})_{\text{ext}} = 0$$

$$\Rightarrow \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \vec{F}_{\text{app}} = 0$$

from above eqn (1), (2) & (3)

$$\begin{aligned} \text{In } x\text{-dir} \rightarrow \\ -0.7454 F_1 - 0.9285 F_2 - 0.8575 F_3 + 800 = 0 \end{aligned}$$

$$\Rightarrow 0.7454 F_1 + 0.9285 F_2 + 0.8575 F_3 = 800 \quad \text{--- (4)}$$

Similarly in y-dir

$$0.2981 F_1 - 0.5145 F_3 = 0 \quad \text{--- (5)}$$

$$\Rightarrow \boxed{F_3 = 0.5794 F_1}$$

In z-dir

$$-0.5962 F_1 + 0.3714 F_2 = 0 \quad \text{--- (6)}$$

from eqn (4), (5) & (6)

$$\begin{bmatrix} 0.7454 & 0.9285 & 0.8575 \\ 0.2981 & 0 & -0.5145 \\ -0.5962 & 0.3714 & 0.5794 \end{bmatrix} \begin{bmatrix} F_1 \\ F_2 \\ F_3 \end{bmatrix} = \begin{bmatrix} 800 \\ 0 \\ 0 \end{bmatrix}$$

by solving —

$$\left[\begin{array}{l} F_1 = 295.9966 \text{ kN} \\ F_2 = 475.1567 \text{ kN} \\ F_3 = 171.4997 \text{ kN} \end{array} \right] \underline{\underline{\text{Ans}}}$$

- Q.6 (c) (i) Show that the first law of thermodynamics leads to the fact that heat interaction is a path function.
- (ii) A perfect gas undergoes a cycle comprises of three processes. It is first compressed isothermally from 1 bar and 27°C to one-fifth of its initial volume. The energy is then added at constant pressure, increasing the temperature of gas and the cycle is completed by isentropic expansion to original conditions. Take $c_p = 1.25 \text{ kJ/kgK}$ and $R = 0.5 \text{ kJ/kgK}$. Calculate the maximum cycle temperature and pressure. Also find the net work transfer.

[10 + 10 marks]

(i)

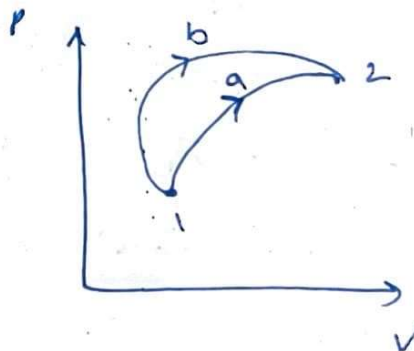
1st law of thermodynamics

$$\delta Q = dE + \delta w$$

$$\Rightarrow \delta w = \delta Q - dE$$

We know that for closed system $\delta w = \int p dv$

↳ i.e. $w = \text{area under curve projected on volume axis}$



for 1a2 & 1b2 Path work is not
same \therefore area under curve is diff.

$$\Rightarrow W_{1a2} \neq W_{1b2}$$

$$\Rightarrow (\delta Q - dE)_{1a2} \neq (\delta Q - dE)_{1b2}$$

but we know that internal energy
is point fn (path independent)

$$\text{so } dE_{1a2} = dE_{1b2}$$

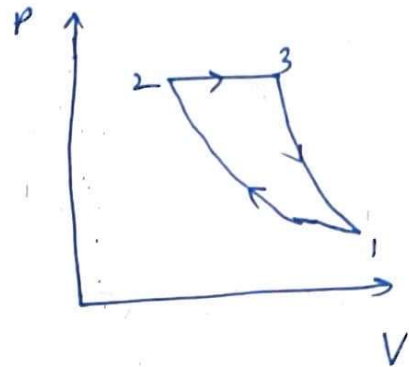
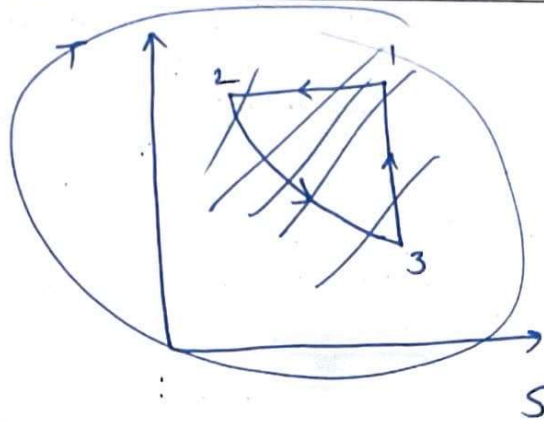
$$\Rightarrow \delta Q_{1a2} - \cancel{dE_{1a2}} \neq \delta Q_{1b2} - \cancel{dE_{1b2}}$$

$$\Rightarrow \boxed{\delta Q_{1a2} \neq \delta Q_{1b2}} \text{ HP}$$

So the heat interaction is different
for both the paths so
Heat interaction will be a path fn.

PTO

(ii)

Given

$$P_1 = 1 \text{ bar}$$

$$T_1 = 300 \text{ K}$$

$$V_2 = \frac{V_1}{5}$$

$$P_2 = 5 \text{ bar}$$

$$T_2 = 300 \text{ K}$$

$$P_3 = 5 \text{ bar}$$

$$T_3 = 571.206 \text{ K}$$

$$C_p = 1.25 \text{ kJ/kg K}$$

$$R = 0.5 \text{ kJ/kg K}$$

$$C_p = \frac{\gamma R}{\gamma - 1}$$

$$\Rightarrow 1.25 = \frac{\gamma \cdot 0.5}{\gamma - 1}$$

$$= 0.5\gamma$$

from,

$$P_1 V_1 = R T_1$$

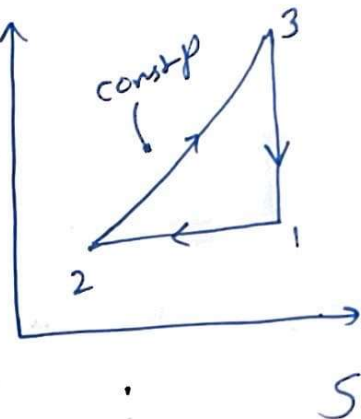
$$\Rightarrow V_1 = \frac{0.5 \times 300}{1} = 1.5 \text{ m}^3/\text{kg}$$

$$\Rightarrow V_2 = 0.3 \text{ m}^3/\text{kg}$$

Now for 1-2 const. T

$$\frac{P_2}{P_1} = \frac{V_1}{V_2} \quad (\text{Boyle's law})$$

$$\Rightarrow P_2 = 5 \text{ bar}$$

for 2-3 const P so $P_3 = P_2 = 5 \text{ bar}$ Assumptions

① gas is an Ideal

② 3-1 Reversible Adiabatic

③ closed system

for 3-1 → isentropic (Assuming Reversible Adiabatic)

$$\frac{T_1}{T_3} = \left(\frac{P_1}{P_3} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\Rightarrow \frac{300}{T_3} = \left(\frac{1}{5} \right)^{\frac{1.667-1}{1.667}}$$

$$\Rightarrow T_3 = 571.2065 \text{ K}$$

So max cycle Temp = $T_3 = 571.2065 \text{ K}$
& max cycle Pressure = $P_2 = P_3 = 5 \text{ bar}$ Ans

Now Net work transfer = ?

$$W_{\text{net}} = w_{12} + w_{23} + w_{31} \quad R(T_3 - T_2):$$

$$= R T_1 \ln \left(\frac{P_1}{P_2} \right) + P \left(v_3 - v_2 \right) + \frac{R(T_3 - T_2)}{\gamma - 1}$$

$$= 0.5 \times 300 \ln \left(\frac{1}{5} \right) + 0.5 (571.2065 - 300) + \frac{0.5 (571.2065 - 300)}{1.667 - 1}$$

$$W_{\text{net}} = -241.4156 + 135.60325 + 203.40385$$

$$W_{\text{net}} = 97.5915 \text{ kJ/kg}$$

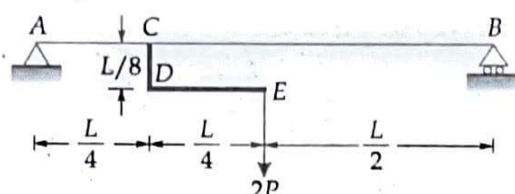
net work transfer in cycle.

- Q.7 (a) A rigid and insulated tank of volume 2.5 m^3 contains an ideal gas at 1 bar and 320 K. The tank is connected to a line carrying the same gas at 25 bar and 550 K. The valve in between the tank and the line is opened allowing the gas to enter the tank till the gas pressure in the tank rises to 25 bar and then closed. Determine the final temperature of the gas in the tank and the amount of gas that entered the tank. Neglect the effects of kinetic energy and potential energy.

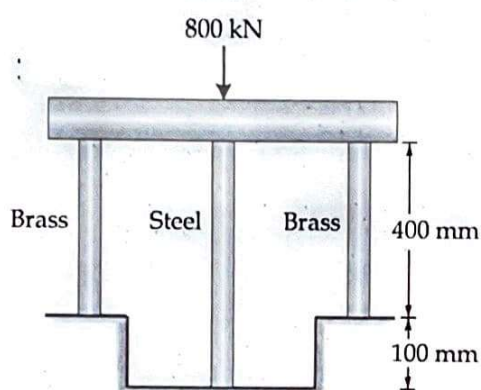
[Assume $R = 0.287 \text{ kJ/kgK}$; $c_p = 1.005 \text{ kJ/kgK}$ and $\gamma = 1.4$ for ideal gas]

[20 marks]

- Q.7 (b) (i) A simply supported beam ACB supports a vertical load $2P$ by means of a bracket CDE, as shown in figure below. Draw SFD and BMD for the beam.



- (ii) A steel rod and two brass rods, together support a load of 800 kN as shown in figure below. Young's modulus of steel and brass are 200 GPa and 100 GPa, respectively. Cross-sectional area of steel and brass rod are 2500 mm^2 and 1500 mm^2 , respectively. Calculate the stresses in the rods.



[10 + 10 marks]

- Q.7 (c) (i) Sketch the Mollier diagram and briefly explain its essential features.
- (ii) A rigid and sealed tank of volume 1 m^3 is initially filled with dry saturated steam at 230°C and left in the room. After a while the temperature of the steam is reduced to 190°C . Determine the final conditions of steam in the tank and the amount of energy transferred as heat. (Refer steam table attached)

[8 + 12 marks]

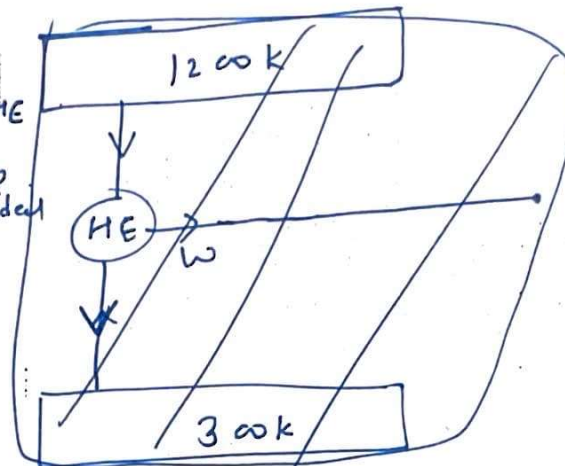
- Q.8 (a) A heat engine operating between two reservoirs at 1200 K and 300 K is used to drive a heat pump which extracts heat from the reservoir at 300 K at a rate twice that at which the engine rejects heat to it. If the efficiency of the engine is 40% of the maximum possible and the COP of the heat pump is 60% of the maximum possible, then determine:
- the temperature of the reservoir to which the heat pump rejects heat.
 - the rate of heat rejection from the heat pump if the rate of heat supply to the engine is 100 kW.

[20 marks]

Given

$$\eta_{HE} = 0.4 \eta_{CHE}$$

$$COP_{HP} = 0.6 COP_{ideal}$$



from 1st law
 $Q_1 = W + Q_2$
 $\Rightarrow Q_3 = W + 2Q_2$

(i) $\eta_{CHE} = 1 - \frac{300}{1200} = 0.75$

$$\Rightarrow \boxed{\eta_{HE} = 0.3}$$

$$\eta_{HE} = \frac{W}{Q_1} = 0.3$$

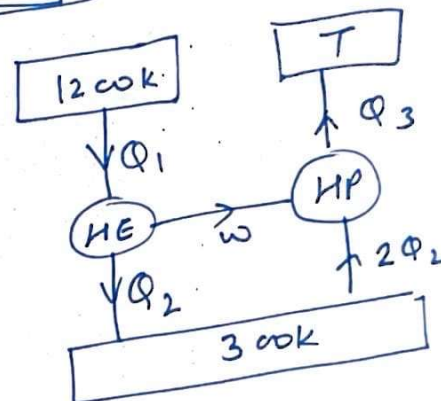
$$\Rightarrow W = 0.3(W + Q_2)$$

$$\Rightarrow \boxed{W = \frac{3}{7} Q_2} \quad \text{--- (1)}$$

$$COP_{HP} = 0.6 \times \frac{T}{T - 300} = \frac{Q_3}{W}$$

$$\Rightarrow \frac{0.6T}{T - 300} = 1 + \frac{2Q_2}{W} = 1 + 2 \times \frac{7}{3} \quad (\text{from eqn (1)})$$

$$\Rightarrow \frac{0.6T}{T - 300} = 1 + \frac{14}{3} = \frac{17}{3}$$



$$\Rightarrow \frac{180}{T-300} = \frac{17}{3}$$

$$\Rightarrow 17T - 5100 = 540$$

$$\Rightarrow T = 331.76 \text{ K}$$

$$1.8T = 17T - 5100$$

$$\Rightarrow 15.2T = 5100$$

$$\Rightarrow T = 335.526 \text{ K}$$

So the Temp. of reservoir will be ~~335.526~~ K to which the HP is rejecting heat.

ii) 

$Q_3 = ?$ Given
 $Q_1 = 100 \text{ kW}$

Now, $\eta_{HE} = \frac{W}{Q_1} = 0.3$

$\Rightarrow W = 30 \text{ kW}$

for HP

$$(\text{COP})_{HP} = 0.6 \times \frac{335.526}{335.526 - 300} = \frac{Q_3}{W}$$

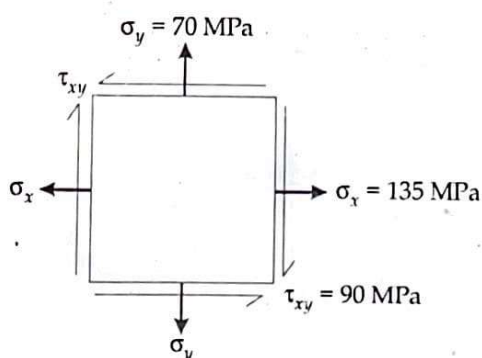
$\Rightarrow \frac{Q_3}{W} = 5.6667$

$\Rightarrow Q_3 = 5.6667 \times 30$

$\Rightarrow Q_3 = 170.0013 \text{ kW}$ Ans

So rate of Heat rejection from heat pump will be 170.0013 kW.

- Q.8 (b) At a certain point in a piece of elastic material, there are normal tensile stresses of magnitude 135 MPa (in x -direction), 70 MPa acting orthogonally to each other. In addition, there is a shearing stress of 90 MPa acting normal to the normal stresses. Calculate : (i) the magnitude and direction of the principal stresses, (ii) the magnitude and direction of the maximum shearing stress, (iii) the normal and shearing stress on a plane inclined at 30° to the direction of 135 MPa stress.



A-

Given

$$\sigma_x = 135 \text{ MPa}$$

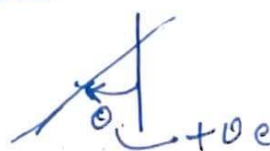
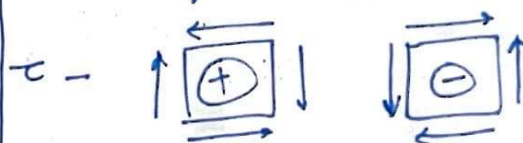
$$\sigma_y = 70 \text{ MPa}$$

$$\tau_{xy} = +90 \text{ MPa}$$

Sign conv

[20 marks]

$\sigma \rightarrow$ Tensile = $+ve$
Comp = $-ve$



(i) We know that

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$\Rightarrow \sigma_{1,2} = \frac{135 + 70}{2} \pm \sqrt{\left(\frac{135 - 70}{2}\right)^2 + 90^2}$$

$$\Rightarrow \sigma_{1,2} = 102.5 \pm 95.6883$$

$$\Rightarrow \sigma_1 = 198.1883 \text{ MPa}$$

$$\& \sigma_2 = 6.8117 \text{ MPa}$$

Ans

$$\tan 2\theta_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y} = \frac{2 \times 90}{135 - 70}$$

$$\Rightarrow \tan 2\theta_p = 2.7692$$

$$\Rightarrow \theta_{p_1} = 35.072^\circ \quad \Delta \quad \theta_{p_2} = 90 + \theta_{p_1} = 125.072^\circ$$

$$\sigma_n = \frac{\sigma_x + \sigma_y}{2} + \left(\frac{\sigma_x - \sigma_y}{2}\right) \cos 2\theta + \tau_{xy} \sin 2\theta$$

$$\Rightarrow \sigma_n = 102.5 + 32.5 \times \cos(2 \times 35.072) + 90 \sin(2 \times 35.072)$$

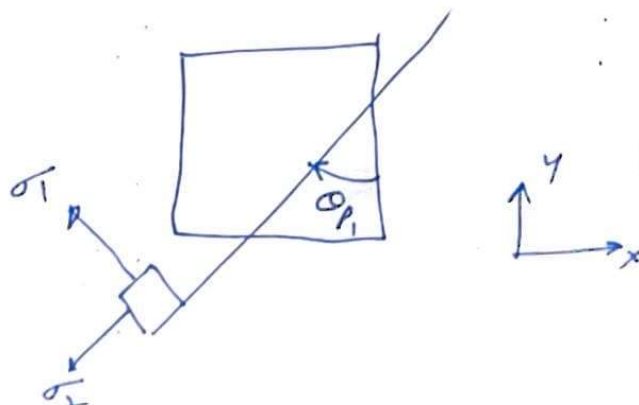
$$\Rightarrow \sigma_n = 198.188 \text{ MPa}$$

\Rightarrow Major principal stress

$$\sigma_1 = 198.1883 \text{ MPa at } \theta_{p_1} = 35.072^\circ$$

$$\& \text{Minor } \sigma_2 = 6.8117 \text{ MPa at } \theta_{p_2} = 125.072^\circ$$

from vertical
face ($x \rightarrow$)
in cw dirⁿ



(ii)

$$\tau_{\max} = \frac{\sigma_1 - \sigma_2}{2} \Rightarrow \tau_{\max} = 95.6083 \text{ MPa}$$

↓
In plane

$$\& \theta_s = \theta_p + 45^\circ$$

$$\Rightarrow \theta_s = 80.072^\circ \quad \underline{\underline{\text{Ans}}}$$

$$(\tau_{\max})_{\text{abs}} = \frac{\sigma_1 - 0}{2} = 99.0941 \text{ MPa}$$

(iii)

$$\sigma_{x'} = \frac{\sigma_x + \sigma_y}{2} + \left(\frac{\sigma_x - \sigma_y}{2} \right) \cos 2\theta + \tau_{xy} \sin 2\theta$$

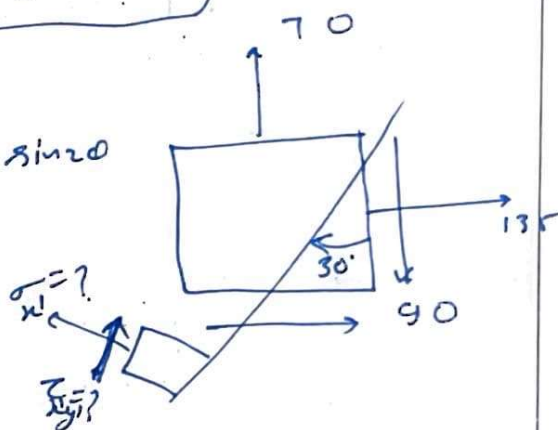
$$\Rightarrow \sigma_{x'} = 102.5 + 32.5 \cos 60^\circ + 90 \sin 60^\circ$$

$$\Rightarrow \sigma_{x'} = 196.6922 \text{ MPa} \quad \underline{\underline{\text{Ans}}} \text{ (Tensile)}$$

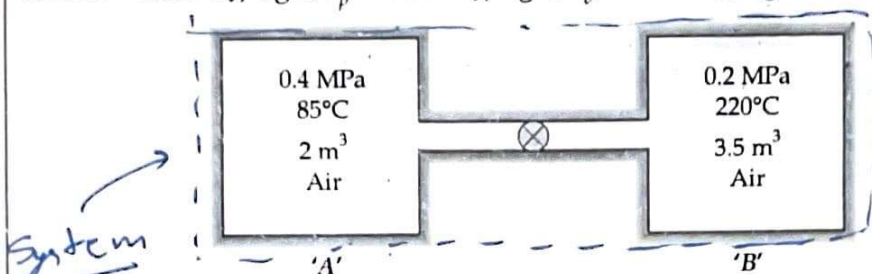
$$\tau_{x'y'} = - \left(\frac{\sigma_x - \sigma_y}{2} \right) \sin 2\theta + \tau_{xy} \cos 2\theta$$

$$\Rightarrow \tau_{x'y'} = -32.5 \sin 60^\circ + 90 \cos 60^\circ$$

$$\Rightarrow \tau_{x'y'} = 16.8542 \text{ MPa} \quad \underline{\underline{\text{Ans}}} \text{ (cw)}$$



- Q.8 (c) Two vessels, A and B of volume 2 m^3 and 3.5 m^3 respectively, are connected by a tube of negligible volume through a valve as shown below. Vessel A contains air at 0.4 MPa , 85°C while vessel B contains air at 0.2 MPa , 220°C . Determine the total change of entropy, when the valve is opened and assuming the mixing to be complete and adiabatic. For air take $R = 0.287 \text{ kJ/kgK}$; $c_p = 1.005 \text{ kJ/kgK}$; $c_v = 0.717 \text{ kJ/kgK}$.



[20 marks]

Find $\Delta S = ?$
Before mixing
for vessel A

$$m_A = \frac{P_A V_A}{R T_A}$$

$$\Rightarrow m_A = \frac{400 \times 2}{0.287 \times 358}$$

$$\Rightarrow m_A = 7.7862 \text{ kg}$$

for vessel B

$$m_B = \frac{200 \times 3.5}{0.287 \times 493}$$

$$\Rightarrow m_B = 4.9473 \text{ kg}$$

After mixing

$$m_{\text{final}} = m_A + m_B$$

$$\Rightarrow m_T = 12.7335 \text{ kg}$$

$$V_T = V_A + V_B$$

$$\Rightarrow V_T = 5.5 \text{ m}^3$$

Assumptions

① Air ~~is~~ an ideal gas.
work as

② final volume of
air will be V_T for
each vessel's air

$$P_f V_f = m_T R T_f$$

$$\Rightarrow P_f = \frac{12.7335 \times 0.287 \times T_f}{5.5}$$

$$\Rightarrow P_f = 0.6645 T_f$$

①

from 1st law for entire system
 $\cancel{Q} = \Delta U + \cancel{W}$ ($W=0 \because$ no work done)
 $Q=0 \because$ adiabatic

$$\Rightarrow \Delta U_A + \Delta U_B = 0$$

$$m_A c_v (T_f - T_A) + m_B c_v (T_f - T_B) = 0$$

$$\Rightarrow 7.7862 (T_f - 358) + 4.9473 (T_f - 493) = 0$$

$$\Rightarrow 12.7335 T_f = 5226.4785$$

$$\Rightarrow \boxed{T_f = 410.45 \text{ K}}$$

from eqn (1) $\boxed{P_f = 272.7447 \text{ kPa}}$

$$\begin{aligned} \bullet (\Delta S)_A &= m_A \left[C_v \ln \frac{T_f}{T_A} + R \ln \left(\frac{V_f}{V_A} \right) \right] \\ &= 7.7862 \left[0.717 \ln \frac{410.45}{358} + 0.287 \ln \frac{5.5}{2} \right] \end{aligned}$$

$$\Rightarrow \boxed{(\Delta S)_A = 3.0238 \text{ kJ/K}}$$

$$\bullet \Delta S_B = 4.9473 \left[0.717 \ln \left(\frac{410.45}{493} \right) + 0.287 \ln \frac{5.5}{3.5} \right]$$

$$\Rightarrow \boxed{\Delta S_B = -0.6101 \text{ kJ/K}}$$

So total change of entropy $\rightarrow 0$

$$(\Delta S)_{\text{Total}} = (\Delta S)_A + (\Delta S)_B + \cancel{(\Delta S)_{\text{surr}}}$$

$$\Rightarrow \boxed{(\Delta S)_T = 3.0137 \text{ kJ/K}} \quad \underline{\underline{\text{Ans}}}$$

Saturated Water and Steam (Temperature-based), Contd.

T °C	P _{sat} MPa	Volume, m ³ /kg v _f	Volume, m ³ /kg v _g	Energy, kJ/kg u _f	Energy, kJ/kg u _g	Enthalpy, kJ/kg h _f	Enthalpy, kJ/kg h _g	Entropy, kJ/(kg K) s _f	Entropy, kJ/(kg K) s _g
200	1.5549	0.00115653	0.12721	850.47	2504.2	852.27	2792.0	2.3305	6.4302
201	1.5877	0.00115809	0.12467	854.94	2504.7	856.78	2792.6	2.3400	6.4227
202	1.6210	0.00115967	0.12218	859.42	2505.1	861.30	2793.2	2.3494	6.4152
203	1.6549	0.00116126	0.11976	863.90	2505.5	865.82	2793.7	2.3588	6.4078
204	1.6893	0.00116286	0.11739	868.38	2506.0	870.35	2794.3	2.3683	6.4001
205	1.7243	0.00116448	0.11508	872.87	2506.4	874.88	2794.8	2.3777	6.3926
206	1.7598	0.00116610	0.11282	877.37	2506.8	879.42	2795.3	2.3871	6.3851
207	1.7959	0.00116774	0.11061	881.86	2507.3	883.96	2795.9	2.3964	6.3776
208	1.8326	0.00116939	0.10846	886.37	2507.5	888.51	2796.3	2.4058	6.3701
209	1.8698	0.00117105	0.10635	890.88	2507.9	893.07	2796.8	2.4152	6.3626
210	1.9077	0.00117272	0.10429	895.39	2508.3	897.63	2797.3	2.4245	6.3551
211	1.9461	0.00117441	0.10228	899.91	2508.7	902.20	2797.7	2.4339	6.3476
212	1.9851	0.00117611	0.10031	904.44	2509.0	906.77	2798.1	2.4432	6.3401
213	2.0247	0.00117782	0.09839	908.97	2509.3	911.35	2798.5	2.4526	6.3326
214	2.0650	0.00117954	0.09651	913.50	2509.6	915.94	2798.9	2.4619	6.3251
215	2.1058	0.00118128	0.09467	918.04	2509.9	920.53	2799.3	2.4712	6.3176
216	2.1473	0.00118303	0.09288	922.58	2510.2	925.12	2799.7	2.4805	6.3101
217	2.1891	0.00118479	0.09119	927.12	2510.5	929.71	2800.1	2.4898	6.3026
218	2.2322	0.00118657	0.08954	931.69	2510.8	934.34	2800.5	2.4991	6.2951
219	2.2766	0.00118836	0.08793	936.26	2511.1	938.96	2800.9	2.5084	6.2876
220	2.3216	0.00119017	0.08636	940.82	2511.4	943.58	2801.3	2.5177	6.2801
221	2.3673	0.00119198	0.08486	945.39	2511.7	948.21	2801.7	2.5269	6.2726
222	2.4136	0.00119382	0.08340	949.97	2512.0	952.85	2802.1	2.5362	6.2651
223	2.4606	0.00119567	0.08197	954.55	2512.3	957.49	2802.5	2.5455	6.2576
224	2.5083	0.00119753	0.08057	959.14	2512.6	962.14	2802.9	2.5547	6.2501
225	2.5567	0.00119940	0.07919	963.74	2512.9	966.80	2803.3	2.5640	6.2426
226	2.6058	0.00120130	0.07784	968.31	2513.2	971.46	2803.7	2.5732	6.2351
227	2.6556	0.00120320	0.07651	972.95	2513.5	976.13	2804.1	2.5824	6.2276
228	2.7060	0.00120512	0.07520	977.56	2513.8	980.81	2804.5	2.5917	6.2201
229	2.7571	0.00120706	0.07391	982.19	2514.1	985.50	2804.9	2.6009	6.2126
230	2.8088	0.00120902	0.07264	986.81	2514.4	990.19	2805.3	2.6101	6.2051
231	2.8611	0.00121098	0.07139	991.44	2514.7	994.90	2805.7	2.6193	6.1976
232	2.9140	0.00121297	0.07016	996.68	2515.0	999.60	2806.1	2.6285	6.1901
233	2.9675	0.00121497	0.06895	1001.97	2515.3	1004.3	2806.5	2.6377	6.1826
234	3.0216	0.00121699	0.06776	1007.26	2515.6	1009.0	2806.9	2.6469	6.1751
235	3.0763	0.00121902	0.06659	1012.55	2515.9	1013.7	2807.3	2.6561	6.1676
236	3.1316	0.00122108	0.06543	1017.84	2516.2	1018.4	2807.7	2.6653	6.1601
237	3.1875	0.00122315	0.06428	1023.13	2516.5	1023.1	2808.1	2.6745	6.1526
238	3.2439	0.00122523	0.06314	1028.42	2516.8	1027.8	2808.5	2.6837	6.1451
239	3.2998	0.00122731	0.06201	1033.71	2517.1	1032.5	2808.9	2.6929	6.1376
240	3.3562	0.00122940	0.06089	1039.00	2517.4	1037.2	2809.3	2.7021	6.1301

Saturated Water and Steam (Temperature-based), Contd.

T °C	P _{sat} MPa	Volume, m ³ /kg v _f	Volume, m ³ /kg v _g	Energy, kJ/kg u _f	Energy, kJ/kg u _g	Enthalpy, kJ/kg h _f	Enthalpy, kJ/kg h _g	Entropy, kJ/(kg K) s _f	Entropy, kJ/(kg K) s _g
160	0.61823	0.00110190	0.30678	674.70	2587.7	675.47	2757.4	1.9426	6.7491
161	0.63412	0.00110316	0.29951	679.12	2588.3	679.82	2758.0	1.9525	6.7406
162	0.65033	0.00110438	0.29245	683.45	2588.9	684.17	2758.6	1.9625	6.7320
163	0.66686	0.00110559	0.28559	687.78	2589.5	688.52	2759.2	1.9725	6.7235
164	0.68373	0.00110680	0.27892	692.12	2590.1	692.88	2759.8	1.9824	6.7150
165	0.70093	0.00110803	0.27243	696.46	2590.7	697.24	2760.4	1.9923	6.7065
166	0.71848	0.00110926	0.26612	700.80	2591.3	701.60	2761.0	2.0022	6.6980
167	0.73638	0.00111050	0.25999	705.14	2591.9	705.96	2761.6	2.0121	6.6895
168	0.75462	0.00111175	0.25403	709.49	2592.5	710.33	2762.2	2.0220	6.6810
169	0.77322	0.00111300	0.24823	713.85	2593.1	714.71	2762.8	2.0318	6.6725
170	0.79219	0.00111427	0.24259	718.20	2593.7	719.08	2763.4	2.0417	6.6650
171	0.81152	0.00111554	0.23710	722.55	2594.3	723.46	2764.0	2.0515	6.6575
172	0.83122	0.00111682	0.23176	726.92	2594.9	727.85	2764.6	2.0613	6.6500
173	0.85130	0.00111811	0.22656	731.28	2595.5	732.23	2765.2	2.0711	6.6425
174	0.87176	0.00111941	0.22150	735.65	2596.1	736.63	2765.8	2.0809	6.6350
175	0.89260	0.00112072	0.21658	740.02	2596.7	741.02	2766.4	2.0907	6.6275
176	0.91384	0.00112204	0.21179	744.39	2597.3	745.42	2767.0	2.1005	6.6200
177	0.93547	0.00112336	0.20712	748.77	2597.9	749.82	2767.6	2.1103	6.6125
178	0.95751	0.00112470	0.20258	753.15	2598.5	754.23	2768.2	2.1201	6.6050
179	0.97995	0.00112604	0.19815	757.54	2599.1	758.64	2768.8	2.1299	6.5975
180	1.0028	0.00112740	0.19384	761.92	2599.7	763.05	2769.4	2.1397	6.5900
181	1.0261	0.00112876	0.18964	766.31	2599.9	767.47	2770.0	2.1495	6.5825
182	1.0498	0.00113013	0.18555	770.71	2600.1	771.90	2770.6	2.1593	6.5750
183	1.0739	0.00113151	0.18157	775.10	2600.3	776.32	2771.2	2.1691	6.5675
184	1.0985	0.00113290	0.17769	779.51	2600.5	780.75	2771.8	2.1789	6.5600
185	1.1235	0.00113430	0.17390	783.92	2600.7	785.19	2772.4	2.1887	6.5525
186	1.1489	0.00113571	0.17021	788.33	2600.9	789.63	2773.0	2.1985	6.5450
187	1.1748	0.00113713	0.16662	792.73	2601.1	794.07	2773.6	2.2083	6.5375
188	1.2011	0.00113856	0.16311	797.15	2601.3	798.52	2774.2	2.2181	6.5300
189	1.2280	0.00114000	0.15969	801.57	2601.5	802.97	2774.8	2.2279	6.5225
190	1.2552	0.00114145	0.15636	806.00	2601.7	807.43	2775.4	2.2377	6.5150
191	1.2830	0.00114291	0.15311	810.42	2601.9	811.89	2776.0	2.2475	6.5075
192	1.3112	0.00114438	0.14994	814.86	2602.1	816.36	2776.6	2.2573	6.5000
193	1.3399	0.00114586	0.14685	819.29	2602.3	820.83	2777.2	2.2671	6.4925
194	1.3691	0.00114736	0.14383	823.74	2602.5	825.31	2777.8	2.2769	6.4850
195	1.3988	0.00114886	0.14089	828.18	2602.7	829.79	2778.4	2.2867	6.4775
196	1.4290	0.00115037	0.13802	832.64	2602.9	834.28	2779.0	2.2965	6.4700
197	1.4597	0.00115189	0.13522	837.09	2603.1	838.77	2779.6	2.3063	6.4625
198	1.4900	0.00115343	0.13248	841.54	2603.3	843.26	2780.2	2.3161	6.4550
199	1.5227	0.00115497	0.12982	846.00	2603.5	847.76	2780.8	2.3259	6.4475
200	1.5549	0.00115653	0.12721	850.47	2603.7	852.27	2781.4	2.3357	6.4400