# **POSTAL** Book Package

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# **CIVIL ENGINEERING**

# **Design of Steel Structures**

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## **Rivets & Bolts**

## Rivets

Q1 Determine the rivet value of 18 mm diameter rivets connecting 10 mm plate and is in: (i) single shear, and (ii) double shear. The permissible stresses for rivets in shear and bearing are 80 MPa and 250 MPa respectively and for plate in bearing is 250 MPa.

#### **Solution:**

Gross diameter of rivets, d = 18 + 1.5 = 19.5 mm

Strength of rivet

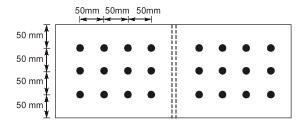
(i) In bearing = 
$$\sigma_{pf} \times d \times t = 250 \times 19.5 \times 10 = 48750 \text{ N} = 48.75 \text{ kN}$$

(ii) In single shear = 
$$\tau_{vf} \times \frac{\pi}{4} \times d^2 = 80 \times \frac{\pi}{4} \times (19.5)^2 = 23891.8 \text{ N} = 23.89 \text{ kN}$$

(iii) In double shear = 
$$2 \times \tau_{vf} \times \frac{\pi}{4} \times d^2 = 2 \times 23891.8 = 47783.6 \text{ N} = 47.78 \text{ kN}$$

 $\therefore$  Rivet value in single shear = smaller of (i) and (ii) = 23.89 kN and Rivet value in double shear = smaller of (i) and (iii) = 47.78 kN

A double cover butt riveted joint is used to connect two flat plates of 200 mm width and 14 mm thickness as shown in the figure. There are twelve power driven rivets of 20 mm diameter at a pitch of 50 mm in both directions on either side of the plate. Two cover plates of 10 mm thickness are used. Find the capacity of the joint in tension considering bearing and shear ONLY, with permissible bearing and shear stresses as 300 MPa and 100 MPa respectively.



#### **Solution:**

Strength of one rivet in double shear

= 
$$2 \times \frac{\pi (O')^2}{4} \times \sigma_s = 2 \times \frac{(20 + 1.5)^2 \pi}{4} \times 100 \times 10^{-3}$$
  
= 72.61 kN

Strength of the riveted joint in double shear

$$=12 \times 72.61 = 871.32 \text{ kN}$$

Strength of one rivet in bearing =  $d't \times \sigma_b$ 

$$= (20 + 1.5) \times 14 \times 300 \times 10^{-3} = 90.3 \text{ kN}$$



Strength of the riveted joint in bearing

$$= 12 \times 90.3 = 1083.6 \text{ kN}$$

Thus the strength of joint will be governed by shearing and it will be equal to 871.32 kN

Two plates each 12 mm thick are joined by double riveted double cover butt joint as shown in figure below. Using 20 mm diameter rivets, design the pitch of the rivets. Take  $\sigma_{at}$  = 150 MPa. Also find the efficiency of the joint. (Consider power driver shop rivet.)

#### **Solution:**

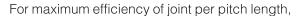
Gross diameter of the rivets = 20 + 1.5 = 21.5 mm

For power driven shop rivets  $\sigma_{nf} = 300 \text{ MPa}$ 

and  $\tau_{\rm vf} = 100 \, \rm MPa$ 

Strength of rivets in bearing = 
$$\frac{300}{1000} \times 21.5 \times 12 = 77.4 \text{ kN}$$

Strength of rivets in double shear = 
$$\frac{2 \times 100}{1000} \times \frac{\pi}{4} (21.5)^2 = 72.6 \text{ kN}$$



Strength of plate per pitch =  $2 \times \text{Rivet value}$ 

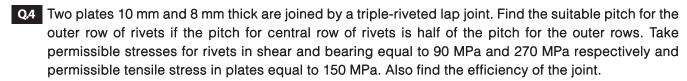
or 
$$\sigma_{at} \times (p-d) \times t = 2 \times 72.6 \times 1000 \text{ N}$$

or 
$$150 \times (p-21.5) \times 12 = 2 \times 72.6 \times 1000 \text{ N}$$

or 
$$p = 102.17 \text{ mm (say } 100 \text{ mm)}$$

Minimum permissible pitch =  $2.5 \times d = 2.5 \times 21.5 = 53.75$  mm

Efficiency of joint = 
$$\frac{150 \times (100 - 21.5) \times 12}{150 \times 100 \times 12} \times 100 = 78.5\%$$



#### **Solution:**

Diameter of rivets = 
$$6.01\sqrt{t} = 6.01\sqrt{8} = 16.9$$
 mm say 18 mm

Strength of rivets in single shear

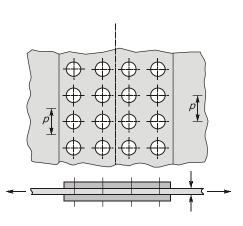
$$= \frac{90}{1000} \times \frac{\pi}{4} \times (19.5)^2 = 26.88 \text{ kN}$$

Strength of rivets in bearing on 8 mm plate =  $\frac{270}{1000} \times 19.5 \times 8 = 42.12 \text{ kN}$ 

For plate A in figure the most critical section will be along 1-1 or 2-2

(i) Strength of plate per pitch along 1-1 = 
$$\frac{150}{1000}$$
 × (p - 19.5) × 8

$$=1.2 p - 23.4 kN$$



(ii) Strength of plate per pitch along 2-2 =  $\frac{150}{1000}$  × (p - 2 × 19.5) × 8 + 26.88

$$=1.2 p - 19.92 kN$$

Comparing (i) and (ii) above, section 1-1 is weaker.

:. Strength of plate per pitch 1.2 p - 23.4 kN

For maximum efficiency of joint,

Strength of plate per pitch = Strength of rivets per pitch

$$\Rightarrow$$
 1.2 p - 23.4 = 4 × 26.88

$$\Rightarrow$$
  $p = 109.1 \,\mathrm{mm} \,\mathrm{say} \,110 \,\mathrm{mm}$ 

Minimum permissible pitch =  $2.5 \times 21.5 = 53.75$  mm

.. Use pitch of 110 mm for outer row of rivets.

Efficiency of joint = 
$$\frac{4 \times 26.88 \times 1000}{150 \times 110 \times 8} \times 100 = 81.45\%$$

O.5 Design a riveted splice for a tie of a steel bridge, 20 cm wide, 20 mm thick carrying an axial tensile force of 50,000 kg. Use 12 mm thick cover plates, 22 mm diameter rivets. Permissible stresses:

tension in plates = 1500 kg/cm<sup>2</sup>

shear in rivets = 1000 kg/cm<sup>2</sup>

bearing in rivets = 3000 kg/ cm<sup>2</sup>

Give a neat sketch of the arrangement.

#### **Solution:**

Taking  $g = 10 \text{ m/s}^2 \text{ and } 1 \text{ kg/cm}^2 = 0.1 \text{ N/mm}^2$ 

∴ Axial tensile force, 
$$P = \frac{50,000 \times 10}{1000} = 500 \text{ kN}$$

Nominal diameter of rivets = 22 mm

∴ Gross diameter of rivets d' = 22 + 1.5 = 23.5 mm

Designing the splice as a double cover butt joint as it will give maximum efficiency.



Given that thickness of cover plates = 12 mm

Width of main plate = 20 cm = 200 mm

Thickness of main plate = 20 mm

Assuming the width of cover plate = 200 mm

Strength of rivet in double shear= 
$$\frac{\pi}{4}(d')^2 \times f_s \times 2 = \frac{\pi}{4} \times (23.5)^2 \times \frac{100}{1000} \times 2 = 86.75 \text{ kN}$$

Strength of rivet in bearing = 
$$a''t f_b = 23.5 \times 20 \times \frac{300}{1000} = 141 \text{ kN}$$

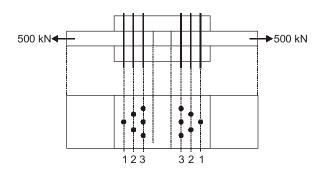
∴ Rivet value,  $R_{c} = 86.75 \text{ kN}$ 

Number of rivets, 
$$n = \frac{P}{R_{c}} = \frac{500}{86.75} = 5.76 \approx 6$$



The rivets can be arranged in diamond pattern

Checking the strength of cover plate and main plate in tearing



As we know that 3-3 is critical for cover plates.

∴Strength of cover plates in tearing at 3-3 ≥ 500 kN

$$\Rightarrow$$
 (200 – 3 × 23.5) × 2 × 12 ×  $\frac{150}{1000}$  = 466.2 kN < 500. Hence unsafe.

Providing two rivets at 3-3, then

Strength of cover plats in tearing at 3-3 = 
$$(200 - 2 \times 23.5) \times 24 \times \frac{150}{1000}$$

$$= 550.8 \, kN > 500 \, kN \, (Hence safe)$$

Thus 2 rivets can be provided at 3-3, Hence safe

Thus arranging rivets in chain pattern, in 3 pairs of two rivets each.

- 1-1 is critical for main plate,
- .: Strength of main plate in tearing at 1-1 > 500 ≥ 500 kN

⇒ = 
$$(200 - 2 \times 23.5) \times 20 \times \frac{150}{1000} = 459 \text{ kN} < 500 \text{ kN}$$
. Hence unsafe

Thus one rivet can be provided at 1-1.

We can provide three rivets at 2-2, thus checking for tearing of main plate at 2-2

$$\Rightarrow = (200 - 3 \times 23.5) \times 20 \times \frac{150}{1000} + R_v > 500$$

$$\Rightarrow = (200 - 3 \times 23.5) \times 20 \times \frac{150}{1000} + 86.75$$

Thus, providing two rivets at 2-2

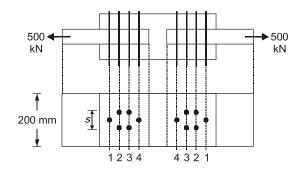
Strength of main plate in tearing at 2-2

$$= (200 - 2 \times 23.5) \times 20 \times \frac{150}{1000} + 86.75$$

$$= 545.75 > 500$$
. Hence safe.

Thus at 1-1 at the most one rivet can be provided. Two rivets can be provided at 2-2. Two rivets can be provided at 3-3. We have to create 4-4 in order to incorporate the remaining one rivet. Thus the arrangement will be as given below.





Equating the strength of rivet per pitch length to the strength of plate per pitch length in tearing.

$$R_v = (S - 23.5) \times 20 \times \frac{150}{1000}$$

$$\Rightarrow 86.75 = (S - 23.5) \times 20 \times \frac{150}{1000}$$

⇒ 
$$S = 52.42 \text{ mm} = 60 \text{ mm} \neq 2.5 \times 22 = 55 \text{ mm}$$

### **Bolts**

- Q.6 Determine the strength of 20 mm diameter bolt of grade 4.6 for the following cases.
  - (a) Lap joint.
  - (b) Single cover butt joint with 10 mm thick cover plate.
  - (c) Double cover butt joint with 8 mm thick cover plates.

The main plates to be joined are 14 mm thick. Use Fe410 grade steel.

#### **Solution:**

For Fe410 steel,  $f_{y} = 410 \text{ N/mm}^2$ ,  $f_{y} = 250 \text{ N/mm}^2$ 

For 4.6 grade bolt,  $f_{ub} = 400 \text{ N/mm}^2$ ,  $f_v = 240 \text{ N/mm}^2$ 

Partial factor of safety for bolt material  $(\gamma_{mb}) = 1.25$ 

Net tensile stress area for 20 mm diameter bolt  $(A_{nb}) = 245 \text{ mm}^2 \left( \simeq 0.78 \times \frac{\pi}{4} \times 20^2 \right)$ 

## (a) Lap joint

In lap joint, the bolts are in single shear

.. Shear strength of bolt in single shear

$$V_{dsb} = \frac{f_{ub} A_{nb}}{\sqrt{3} \gamma_{mb}}$$

$$= \frac{400 \times 245}{\sqrt{3} \times 1.25} N = 45.26 \text{ kN}$$

Strength of bolt in bearing  $(V_{dpb}) = 2.5 k_b dt \frac{f_U}{\gamma_{mb}}$ 

For 20 mm diameter bolt, diameter of bolt hole  $(d_0) = 22 \text{ mm}$ 

End distance 
$$(e) = 33 \, \text{mm}$$

Let pitch 
$$(p) = 50 \text{ mm}$$



$$k_b = \text{ minimum of } \begin{cases} \frac{e}{3d_0} = \frac{33}{3 \times 22} = 0.5 \\ \frac{p}{3d_0} - 0.25 = \frac{50}{3 \times 22} - 0.25 = 0.508 \\ \frac{f_{ub}}{f_u} = \frac{400}{410} = 0.976 \\ 1.0 \end{cases}$$

$$= 0.5$$

$$\therefore V_{dpb} = 2.5 k_b \frac{dt f_u}{\gamma_{mb}}$$

$$= 2.5 \times 0.5 \times 20 \times 14 \times \frac{410}{1.25} N = 114.8 \text{ kN}$$

Thus strength of bolt = Minimum of  $V_{dsb}$  and  $V_{dob}$  = 45.26 kN

#### (b) Single cover butt joint with 10 mm thick cover plate

Here also the bolt will be in single shear and bearing. The considered thickness for bearing will be the minimum of aggregate thickness of cover plate and minimum thickness of main plates to be jointed i.e. t = 10 mm

As computed in part (a) above, strength of bolt in single shear ( $V_{dsb}$ ) = 45.26 kN

Strength of the bolt in bearing  $(V_{dsb}) = 2.5 k_b \frac{dt f_u}{g_{mb}}$ 

$$= 2.5 \times 0.5 \times 20 \times \frac{10 \times 410}{1.25}$$
N

= 82 kN

Thus strength of bolt = Minimum of  $V_{dsb}$  and  $V_{dpb}$ = 45.26 kN

#### (c) Double cover butt joint with 8 mm thick cover plates

Here the bolt will be in double shear and bearing. The considered thickness for bearing will be the minimum of aggregate thickness of cover plates and minimum thickness of main plates to be jointed i.e.

$$t = Minimum of (8 + 8, 14) mm = 14 mm$$

Strength of bolt in double shear  $(V_{dsb})$ 

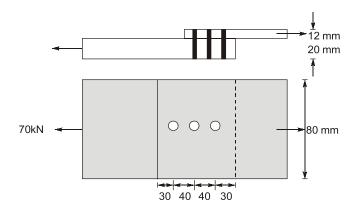
$$= 2 \times \frac{f_{ub} A_{nb}}{\sqrt{3} \gamma_{mb}} = 90.53 \text{ kN}$$

Strength of bolt in bearing ( $V_{\rm dpb}$ )

= 
$$2.5 k_b \frac{dt f_u}{\sqrt{3} \gamma_{mb}}$$
  
=  $2.5 \times 0.5 \times 20 \times 14 \times \frac{410}{1.25} N$   
=  $114.8 \text{ kN}$ 

Thus strength of bolt = Minimum of  $V_{\rm dsb}$  and  $V_{\rm dpb}$  = 90.53 kN

Q7 Design a lap joint between two plates as shown in figure below so as to transmit a factored load of 70 kN using M16 bolts of 4.6 and grade 410 grade steel plates.



#### **Solution:**

Strength calculation

Nominal diameter of the bolt d = 16 mm

 $\therefore$  Hole diameter = 16 + 2 = 18 mm

Bolts are in single shear & hence shear capacity of the bolt is

$$V_{usb} = \left(\frac{f_u}{\sqrt{3}}\right) \frac{(n_n A_{nb} + n_s A_{sb})}{\gamma_{mb}} = \frac{\left(\frac{400}{\sqrt{3}}\right) (1 \times 151)}{1.25} = 27.9 \text{ kN}$$

take

$$e = e_{min} = 1.5 d_0 = 1.5 \times 18 = 27 \text{ mm}$$
  
 $p = p_{min} = 2.5 d = 2.5 \times 16 = 40 \text{ mm}$ 

$$k_b = \min \left[ \frac{e}{3d_0}, \frac{p}{3d_0} - 0.25, \frac{f_{ab}}{f_U}, 1 \right]$$

$$\Rightarrow k_b = \min \left[ \frac{27}{3 \times 18}, \frac{40}{3 \times 18} - 0.25, \frac{40}{410}, 1 \right] = 0.49$$

$$V_{dpb} = 2.5k_b dt \frac{f_{ub}}{1.25}$$

$$= 2.5(0.49)(16)(12)\frac{410}{1.25}N = 77.1445 \text{ kNm}$$

Required number of bolts = 
$$\frac{70}{27.9}$$
 = 2.5 \(\simeq\) 3 bolts

Detailing:

Minimum pitch = 
$$2.5 \times d = 2.5 \times 16 = 40$$
 mm

Maximum edge distance =  $1.5 \times 18 = 27 \text{ mm}$ 

Provide three bolts as shown in figure above.

Two 10 mm thick plates are connected by lap joint to transmit a factored load of 100 kN using black bolts of 12 mm diameter and grade 4.6. What is the minimum number of bolts required for safe design? (Given  $f_u = 410 \text{ MPa}$ )