

POSTAL Book Package

2023

Mechanical Engineering

Conventional Practice Sets

Fluid Mechanics and Fluid Machinery

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Fluid Properties

- Q1** The velocity distribution for flow over a flat plate is given by $u = \frac{3}{4}y - y^2$ in which u is the velocity in metre per second at a distance y metre above the plate. Determine the shear stress at $y = 0.15$ m. Take dynamic viscosity of fluid as 8.5 poise.

Solution:

Given, $u = \frac{3}{4}y - y^2$

Viscosity, $\mu = 8.5 \text{ poise} = \frac{8.5}{10} \text{ Ns/m}^2$ ($\because 10 \text{ poise} = 1 \text{ Ns/m}^2$)

$\therefore \frac{du}{dy} = \frac{3}{4} - 2y$

At $y = 0.15$, $\frac{du}{dy} = \frac{3}{4} - 2 \times 0.15 = 0.75 - 0.30 = 0.45$

$$\tau = \mu \frac{du}{dy}$$

$$= \frac{8.5}{10} \times 0.45 \text{ N/m}^2 = 0.3825 \text{ N/m}^2$$

- Q2** The space between two square flat parallel plates is filled with oil. Each side of the plate is 60 cm. The thickness of the oil film is 12.5 mm. The upper plate, which moves at 2.5 metre per sec requires a forces of 9.18 N to maintain the speed. Determine:

- (i) the dynamic viscosity of the oil in poise, and
 (ii) the kinematic viscosity of the oil in stoke if the specific gravity of the oil is 0.95.

Solution:

Given: Each side of a square plate = 60 cm = 0.60 m

\therefore Area, $A = 0.6 \times 0.6 = 0.36 \text{ m}^2$

Thickness of oil film, $\Delta y = 12.5 \text{ mm} = 12.5 \times 10^{-3} \text{ m}$

Velocity of upper plate, $u = 2.5 \text{ m/sec}$

\therefore Change of velocity between plates,

$$\Delta u = 2.5 \text{ m/sec}$$

Force required on upper plate, $F = 98.1 \text{ N}$

\therefore Shear stress, $\tau = \frac{\text{Force}}{\text{Area}} = \frac{F}{A}$

$$= \frac{98.1 \text{ N}}{0.36 \text{ m}^2} = 27.25 \text{ N/m}^2$$

(i) Let μ = Dynamic viscosity of oil

$$\tau = \mu \frac{du}{dy}$$

or $27.25 = \mu \times \frac{2.5}{12.5 \times 10^{-3}}$

$\therefore \mu = 27.25 \times \frac{12.5 \times 10^{-3}}{2.5} = 0.13625 \text{ Ns/m}^2$ ($\because 1 \text{ Ns/m}^2 = 10 \text{ poise}$)
 $= 0.13625 \times 10 = 1.3625 \text{ Poise}$

(ii) Specific gravity of oil,

$S = 0.95$

Let

ν = kinematic viscosity of oil

Mass density of oil,

$\rho = S \times 1000 = 0.95 \times 1000 = 950 \text{ kg/m}^3$

Using the relation,

$$\nu = \frac{\mu}{\rho}$$

We get,

$$\begin{aligned} \nu &= \frac{0.13625 \text{ Ns/m}^2}{950 \text{ kg/m}^3} = 1.434 \times 10^{-4} \text{ m}^2/\text{sec} \\ &= 1.434 \times 10^4 \text{ cm}^2/\text{s} \\ &= 1.434 \text{ stokes} \end{aligned}$$

Q3 Calculate the dynamic viscosity of an oil, which is used for lubrication between a square plate of size $0.8 \text{ m} \times 0.8 \text{ m}$ and an inclined plane with angle of inclination 30° as shown in figure. The weight of the square plate is 300 N and it slides down the inclined plane with a uniform velocity of 0.3 m/s . The thickness of oil film is 1.5 mm .

Solution:

Given: Area of plate,

$A = 0.8 \times 0.8 = 0.64 \text{ m}^2$

Angle of plane,

$\theta = 30^\circ$

Weight of plate,

$W = 300 \text{ N}$

Velocity of plate,

$u = 0.3 \text{ m/s}$

Thickness of oil film,

$t = dy = 1.5 \text{ mm} = 1.5 \times 10^{-3} \text{ m}$

Let the viscosity of fluid between plate and inclined plane is μ .

Component of weight W , along the plane = $W \cos 60^\circ = 300 \cos 60^\circ = 150 \text{ N}$

Thus the shear force, F , on the bottom surface of the plate = 150 N

and shear stress,

$$\tau = \frac{F}{\text{Area}} = \frac{150}{0.64} \text{ N/m}^2$$

Now,

$$\tau = \mu \frac{du}{dy}$$

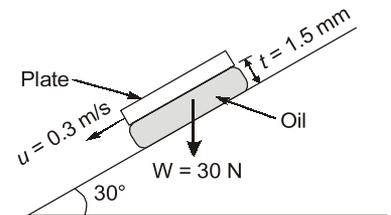
Assuming linear velocity profile,

du = change of velocity = $u - 0 = 0.3 \text{ m/sec}$

$dy = t = 1.5 \times 10^{-3} \text{ m}$

$\therefore \frac{150}{0.64} = \mu \times \frac{0.3}{1.5 \times 10^{-3}}$

$\mu = \frac{150 \times 1.5 \times 10^{-3}}{0.64 \times 0.3} = 1.17 \text{ Ns/m}^2 = 11.7 \text{ Poise}$



Q6 Find the surface tension in a soap bubble of 40 mm diameter when the inside pressure is 2.5 N/m² above atmospheric pressure.

Solution:

Given: Diameter of bubble, $d = 40 \text{ mm} = 40 \times 10^{-3} \text{ m}$
Pressure in excess of outside, $p = 2.5 \text{ N/m}^2$

For a soap bubble,
$$\Delta p = \frac{8\sigma}{d}$$

or
$$2.5 = \frac{8 \times \sigma}{40 \times 10^{-3}}$$

$$\sigma = \frac{2.5 \times 40 \times 10^{-3}}{8} = 0.0125 \text{ N/m}$$

Q7 The pressure outside the droplet of water of diameter 0.04 mm is 10.32 N/cm² (atmospheric pressure). Calculate the pressure within the droplet if surface tension is given as 0.0725 N/m of water.

Solution:

Given, diameter of droplet, $d = 0.04 \text{ mm} = 0.04 \times 10^{-3} \text{ m}$
Pressure outside the droplet = 10.32 N/cm² = 10.32 × 10⁴ N/m²
Surface tension, $\sigma = 0.0725 \text{ N/m}$

The **pressure inside the droplet**, in excess of outside pressure is given by

$$p = \frac{4\sigma}{d}$$

$$= \frac{4 \times 0.0725}{0.04 \times 10^{-3}} = 7250 \text{ N/m}^2$$

$$= \frac{7250 \text{ N}}{10^4 \text{ cm}^2} = 0.725 \text{ N/cm}^2$$

$$\begin{aligned} \text{Pressure inside the droplet} &= \Delta p + \text{pressure outside the droplet} \\ &= 0.725 + 10.32 = 11.045 \text{ N/cm}^2 \end{aligned}$$

Q8 Calculate the capillary effect in mm in a glass tube 3 mm in diameter when immersed in (a) water (b) mercury. Both the liquids are at 20°C and the values of the surface tensions for water and mercury at 20°C in contact with air are respectively 0.0736 N/m and 0.51 N/m. Contact angle for water = 0° and for mercury = 130°.

Solution:

The capillary rise (or depression) is given as

$$h = \frac{2\sigma \cos \theta}{\rho g r}$$

(a) For water $\theta = 0$, $\cos \theta = 1$
 $\sigma = 0.0736 \text{ N/m}$
 $\rho g = 9810 \text{ N/m}^3$
 $d = 3 \text{ mm}$

$$r = \frac{3}{2} = 1.5 \text{ mm} = 1.5 \times 10^{-3} \text{ m}$$

By substitution, we get
$$h = \frac{2 \times 0.0736 \times 1}{9810 \times 1.5 \times 10^{-3}}$$

$$= 1.00 \times 10^{-2} \text{ m} = 10 \text{ mm}$$

(b) For mercury $\theta = 130^\circ$, $\cos \theta = -0.6428$
 $\sigma = 0.51 \text{ N/m}$
 $\rho g = (13.6 \times 9810) \text{ N/m}^3$
 $r = \frac{3}{2} = 1.5 \text{ mm} = 1.5 \times 10^{-3} \text{ m}$

By substitution, we get $h = \frac{2 \times 0.51 \times (-0.6425)}{13.6 \times 9810 \times 1.5 \times 10^{-3}}$
 $= -3.276 \times 10^{-3} \text{ m}$
 $= -3.276 \text{ mm}$

The negative (-) sign in the case of mercury indicates that there is capillary depression.

Q.9 Determine capillarity rise between two thin vertical plates spaced 't' distance apart. Calculate the distance between the plates when the capillarity rise is not to exceed 60 mm. Assume surface tension of water at 20°C as 0.075 N/m.

Solution:

For two vertical plates, 't' distance apart

Let width of plate be 'b' and contact angle be 'θ'

Force due to surface tension = Force due to gravity

$$2\sigma \cos \theta b = \rho g (b \times t)h$$

Height of capillarity rise,

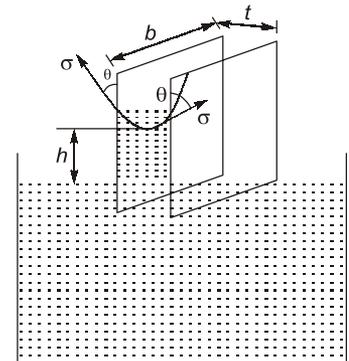
$$h = \frac{2\sigma \cos \theta}{\rho g t}$$

For $\sigma = 0.075 \text{ N/m}$ and $h = 60 \text{ mm}$

Assuming $\theta = 0^\circ$ i.e., $\cos \theta = 1$

$$0.06 = \frac{2 \times 0.075 \times 1000}{9.81 \times 1000 \times t}$$

$$t = 0.255 \text{ mm}$$



Q.10 The density of sea water at free surface where pressure is 98 kPa is 1030 kg/m³. Taking bulk modulus of sea water to be 2.34 × 10⁹ N/m² (assume constant), determine the density and pressure at a depth of 2500 m. Neglect the effect of temperature

Solution:

Calculation of density:

$$K = 2.34 \times 10^9 \text{ N/m}^2$$

$$K = \rho \frac{dP}{d\rho}$$

Since

$$dP = \gamma dh$$

⇒

$$K = \frac{\rho \gamma dh}{d\rho} = \rho^2 g \frac{dh}{d\rho}$$

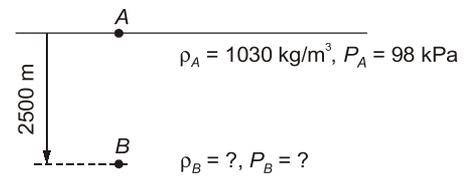
$$\int_{\rho_A}^{\rho_B} \frac{d\rho}{\rho^2} = \int_0^H \frac{g}{K} dh$$

⇒

$$\frac{1}{\rho(-1)} \Big|_{\rho_A}^{\rho_B} = \frac{g}{K} \times H$$

⇒

$$\frac{1}{\rho_A} - \frac{gH}{K} = \frac{1}{\rho_B}$$



∴

$$\rho_B = \frac{1}{\left(\frac{1}{\rho_A} - \frac{gH}{K}\right)}$$

$$\rho_B = \frac{1}{\frac{1}{1030} - \frac{9.81 \times 2500}{2.34 \times 10^9}} = 1041.24 \text{ kg/m}^3$$

Calculation of pressure:

$$K = \frac{dP}{\left(\frac{d\rho}{\rho}\right)}$$

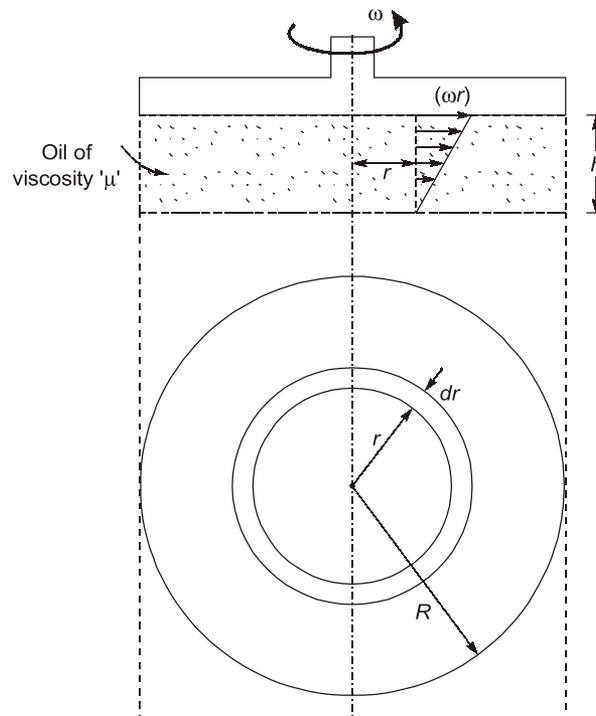
$$\int_{P_A}^{P_B} dP = K \int_{\rho_A}^{\rho_B} \frac{d\rho}{\rho}$$

$$P_B - P_A = K [\ln \rho]_{\rho_A}^{\rho_B}$$

$$P_B = P_A + K \ln \left(\frac{\rho_B}{\rho_A} \right)$$

$$\begin{aligned} P_B &= 98 + 2.34 \times 10^6 \ln \left(\frac{1041.24}{1030} \right) \\ &= 25495.20 \text{ kPa} = 25.5 \text{ MPa} \end{aligned}$$

Q.11 Consider a fluid of viscosity μ between two circular parallel plates of radii 'R' separated by a distance 'h'. Upper plate is rotated at an angular velocity ω whereas bottom plate is held stationary. The velocity profile between two plate is linear. Estimate the torque experienced by the bottom plate.

Solution:Consider an annual ring with width dr at radius ' r '

Shear stress on the ring, $\tau = \mu \left(\frac{du}{dy} \right) = \mu \frac{\omega r}{h} \quad \dots(i)$

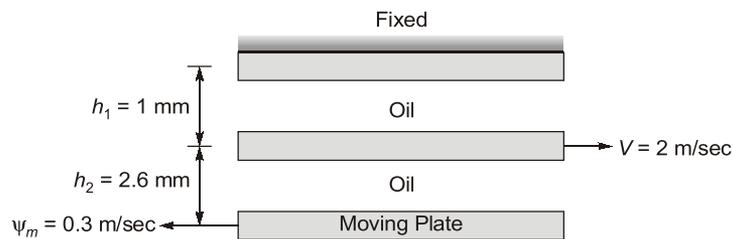
Force on the ring, $F = \tau \times \text{area of contact}$
 $= \left(\frac{\mu \omega r}{h} \right) (2\pi r dr)$

\therefore Torque on the ring, $dT = F.r = \left(\frac{2\pi\mu\omega}{h} \right) r^2 . dr . r$
 $= \left(\frac{2\pi\mu\omega}{h} \right) r^3 . dr$

\therefore Total torque on the disc, $T = \int_0^R \left(\frac{2\pi\mu\omega}{h} \right) r^3 dr$
 $= \left(\frac{2\pi\mu\omega}{h} \right) \left(\frac{R^4}{4} \right)$

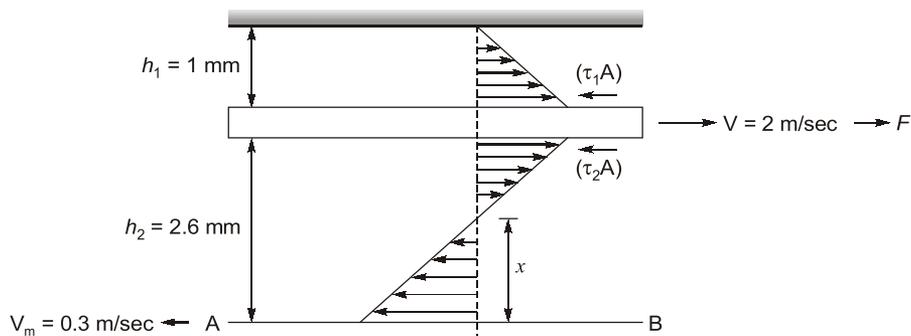
$$T = \frac{\pi\mu\omega R^4}{2h}$$

Q.12 A thin 40 cm x 40 cm flat plate is pulled at 2 m/sec horizontally through a 3.6 mm thick oil layer sandwiched between two plates, one stationary and other moving at a constant speed of 0.3 m/sec as shown in figure. Determine the force that is required to be applied on the plate to maintain this motion. Take ($\mu_{oil} = 0.027$ Pa-s).



Solution:

Given:



Let at a distance x from plate AB, where the velocity of oil will be zero.
 From the property of similarity of triangle

$$\frac{x}{2.6 - x} = \frac{0.3}{2}$$