Production & Industrial Engineering

General Engineering

Vol. II : Applied Mechanics

Comprehensive Theory

with **Solved Examples** and **Practice Questions**

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General Engineering

VOLUME II

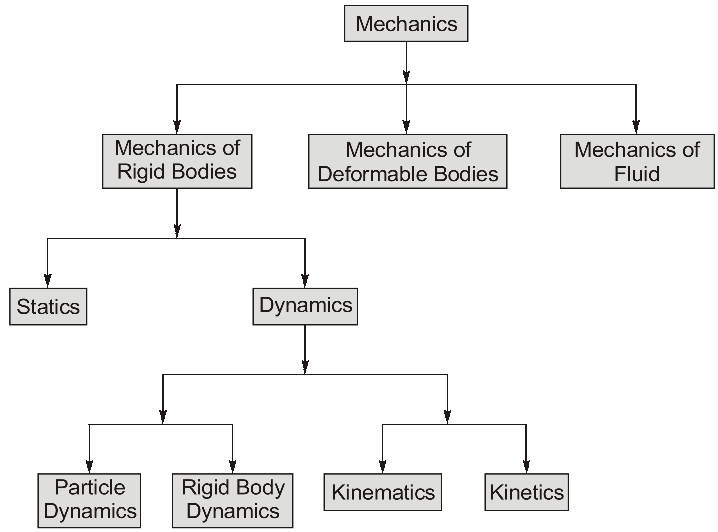
Applied Mechanics

Section I: Engineering Mechanics

INTRODUCTION

Applied mechanics (also **engineering mechanics**) is a branch of the physical sciences and the practical application of mechanics. Pure mechanics describes the response of bodies (solids and fluids) or systems of bodies to external forces. Some examples of mechanical systems include the flow of a liquid under pressure, the fracture of a solid from an applied force, or the vibration of an ear in response to sound. A practitioner of the discipline is known as a **mechanician.**

Applied mechanics describes the behavior of a body, in either a beginning state of rest or of motion, subjected to the action of forces. Applied mechanics, bridges the gap between physical theory and its application to technology. It is used in many fields of engineering, especially mechanical engineering and civil engineering. In this context, it is commonly referred to as **Engineering Mechanics**. Much of modern engineering mechanics is based on Isaac Newton's laws of motion while the modern practice of their application can be traced back to Stephen Timoshenko, who is said to be the father of modern engineering mechanics. Mechanics is classified as follows :



Statics: It is that branch of Engineering Mechanics, which deals with the forces and their effects, while acting upon the bodies at rest.

Dynamics: It is that branch of Engineering Mechanics, which deals with the forces and their effects, while acting upon the bodies in motion. The subject of dynamics may be further sub-divided into the following two branches :

1. Kinetics, and
2. Kinematics.

Kinetics: It is the branch of dynamics, which deals with the bodies in motion due to the application of forces.

Kinematics: It is that branch of dynamics, which deals with the bodies in motion, without any reference to the forces which are responsible for the motion.

2.1 Force

Force can be defined as an action which changes or tends to change the state of rest or of uniform motion of a body. In order to represent the force acting on a body, the magnitude of the force, its point of action and direction of its action should be known.

There are different types of forces such as gravitational, electrical, magnetic or those caused by mass and acceleration.

According to Newton's second law of motion, force may be expressed as:

$$\text{Force} = \text{Mass} \times \text{Acceleration}$$

One Newton force is defined as that which gives an acceleration of 1 m/s^2 when applied to a body of 1 kg in the direction of motion.

2.1.1 Effects of a Force

A force may produce the following effects in a body, on which it acts :

1. It may change the motion of a body. i.e. if a body is at rest, the force may set it in motion. And if the body is already in motion, the force may accelerate it.
2. It may retard the motion of a body.
3. It may retard the forces, already acting on a body, thus bringing it to rest or in equilibrium. We shall study this effect in chapter 5 of this book.
4. It may give rise to the internal stresses in the body, on which it acts. We shall study this effect in the chapters 'Analysis of Perfect Frames' of this book.

2.1.2 Characteristics of Force

In order to determine the effects of a force, acting on a body, we must know the following characteristics of a force :

1. Magnitude of the force (i.e., 100 N, 50 N, 20 kN, 5 kN, etc.)
2. The direction of the line, along which the force acts (i.e., along OX, OY, at 30° North of East etc.). It is also known as line of action of the force.
3. Nature of the force (i.e., whether the force is push or pull). This is denoted by placing an arrow head on the line of action of the force.
4. The point at which (or through which) the force acts on the body.

2.1.3 Principle of Physical Independence of Force

It states that if a number of forces are simultaneously acting on a particle, then the resultant of these forces will have the same effect as produced by all the forces.

Example 2.86 A solid round bar 3 m long and 5 cm in diameter is used as a strut with both ends hinged. Determine the crippling (or collapsing) load. Take $E = 2.0 \times 10^5$ N/mm^2.

Solution :

Given :

Length of bar, $l = 3$ m $= 3000$ mm

Diameter of bar, $d = 5$ cm $= 50$ mm

Young's modulus, $E = 2.0 \times 10^5$ N/mm^2

Moment of inertia $I = \frac{\pi}{64} \times 5^4 = 30.68$ cm^4 $= 30.68 \times 10^4$ mm^4

Let P = Crippling load

As both the ends of the bar are hinged, hence the crippling load is given by equation

$$\therefore \quad P = \frac{\pi^2 EI}{l^2} = \frac{\pi^2 \times 2 \times 10^5 \times 30.68 \times 10^4}{3000^2} = 67288 \text{ N} = 67.288 \text{ kN.}$$

Example 2.87 A column of timber section 15 cm × 20 cm is 6 metre long both ends being fixed. If the Young's modulus for timber = 17.5 kN/mm^3, determine :

(i) Crippling load and

(ii) Safe load for the column if factor of safety = 3.

Solution :

Given :

Dimension of section = 15 cm × 20 cm

Actual length, $l = 6$ m $= 6000$ mm

Young's modulus, $E = 17.5$ kN/mm^2

(i) Let P = Crippling load

We know that

$$P = \frac{\pi^2 EI}{L_e^2} \quad \text{...(i)}$$

where L_e = Effective length

$$= \frac{l}{2} \quad \text{(when both the ends are fixed i}$$

$$= \frac{6000}{2} = 3000 \text{ mm} \quad (\because l = 6000 \text{ mm})$$

I = Least value of moment of inertia

Moment of inertia of the section about X-X axis.

$$I_{XX} = \frac{15 \times 20^3}{12} = 10000 \text{ cm}^4 = 10000 \times 10^4 \text{ mm}^4$$

And moment of inertia of the section about Y-Y axis,

$$I_{YY} = \frac{20 \times 15^3}{12} = 5625 \text{ cm}^4 = 5625 \times 10^4 \text{ mm}^4$$

Since I_{YY} is less than I_{XX}, therefore the column will tend to buckle in Y-Y direction.

And the value of I will be the least value of the two moment of inertia.

$$\therefore \quad I = 5625 \text{ cm}^4 = 5625 \times 10^4 \text{ mm}^4$$

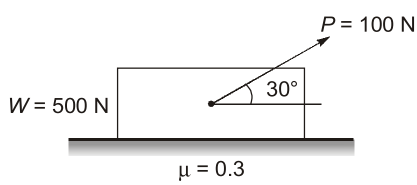
$$= \frac{\pi^2 \times 2.214 \times 10^4 \times \frac{\pi}{64} \times 5^4 \times 10^4}{4000 \times 4000} \qquad \left(\because I = \frac{\pi}{64} \times 5^4 \times 10^4 \text{ mm}^4\right)$$

$= 4189.99$ say 4190 N.

And $\quad$ Safe Load $= \dfrac{\text{Crippling load}}{\text{Factor of safety}} = \dfrac{4190}{4} = 1047.5$ N.

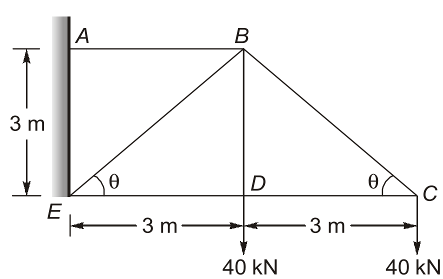
Student's Assignments 1

Q.1 A block weighing 500 N is lying on a rough surface. An inclined force of 100 N acts on the block as shown in the figure. If coefficient of friction between block and surface is 0.3, what is force of friction on block by surface when block is under the action of force?



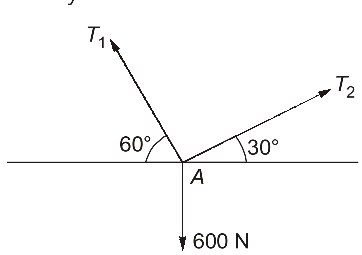
(a) 60 N (b) 135 N
(c) 86.6 N (d) None of these

Q.2 Force in member *CB* is



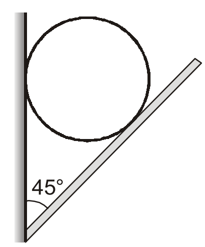
(a) $40\sqrt{2}$ kN (b) 40 kN
(c) $40/\sqrt{2}$ kN (d) 20 kN

Q.3 If point *A* is in equilibrium under the action of the applied force, the value of tensions T_1 and T_2 are respectively



(a) 520 N and 300 N (b) 300 N and 520 N
(c) 450 N and 150 N (d) 150 N and 450 N

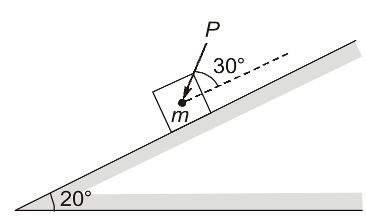
Q.4 A uniform sphere of weight 50 N is lying between two inclined planes at an angle of 45°. The reaction experienced by sphere due to vertical wall is___________N.



Q.5 A force, $F = (10 + 0.50x)$ acts on a particle in the x-direction, where F is in Newton and x in meter. What will be the work done by this force during a displacement from $x = 0$ to $x = 3.0$ m?

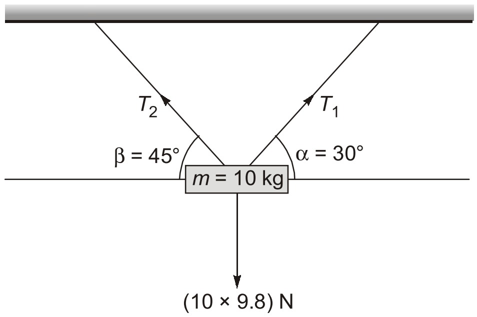
(a) 32.25 J (b) 34.5 J
(c) 16.12 J (d) 17.25 J

Q.6 What value of constant force *P* is required to bring the 100 kg body, which starts from rest, to a velocity of 25 m/s in 50 m? (Neglect friction)



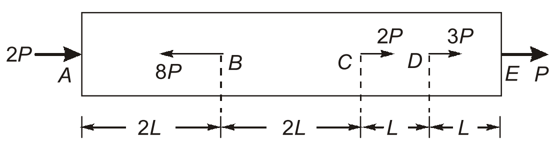
(a) 334.26 N (b) 578.1 N
(c) 289.5 N (d) 450.6 N

Q.7 A body of mass 10 kg is suspended by two strings making angle 30° and 45° with the horizontal as shown in figure. Sum of tension in the string is________ N.



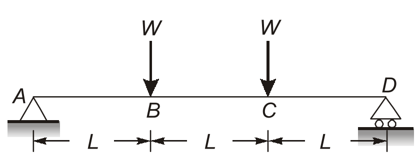
Q.8 The resultant of two forces acting at an point at an angle of 135° is perpendicular to the smaller of the two forces. If the greater force is 25 N then the difference in magnitude of the resultant force and the smaller force is _______ N.

Q.9 For the given prismatic bar as shown in the figure, what will be the value of maximum tensile and compressive loads?



(a) 6P, –2P (b) 4P, –2P
(c) 6P, 2P (d) 4P, 2P

Q.10 A simple supported beam is shown in the figure. What will be the shape of elastic curve between point *B* and *C*?



(a) Straight line (b) Parabolic
(c) Circular (d) Cubic

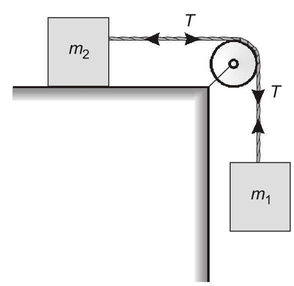
Q.11 If a wire of 10 mm dia is bend around a large cylinder of diameter 3 m, then the value of max. stress (in MPa) produced in wire will be _______. [Take modulus of elasticity of both wire and cylinder is 200 GPa]

Q.12 For a ductile material principal stresses are 200 MPa and – 100 MPa. The value of working stress for ductile material using maximum distortion energy theory will be_________MPa.

Q.13 A long column whose one end is fixed and another is free having a length of 800 mm and radius of gyration as 10 mm. The value of buckling stress will be _________ MPa.
[Take Young's modulus of material as 150 GPa]

Student's Assignments 2

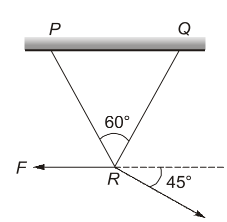
Q.14 In the given figure, two bodies of masses m_1 and m_2 are connected by a light inextensible string passes over a smooth pulley. Mass m_2 lies on a smooth horizontal plane. When mass m_1 moves downwards, the acceleration (in m/s²) of the two bodies is equal to



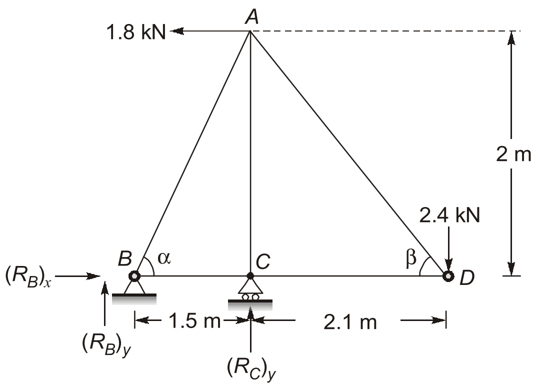
(a) $\dfrac{m_2 g}{m_1 - m_2}$ (b) $\dfrac{m_1 g}{m_1 - m_2}$

(c) $\dfrac{m_1 g}{m_1 + m_2}$ (d) $\dfrac{m_2 g}{m_1 + m_2}$

Q.15 The force *F* such that both the bars *PR* and *QR* (*PR* and *QR* are equal in length) as shown in the figure are identically loaded, is __________ kN.



Q.16 A truss is loaded as shown in figure. What will be the value of force in member *AC* & *AD*?



(a) 3.36 kN & 3.48 kN respectively
(b) 2.52 kN & 3.48 kN respectively
(c) 3.36 kN & 2.52 kN respectively
(d) 3.48 kN & 3.36 kN respectively

Q.17 A steel cube of side 1 m is placed at a depth of *h* m in the sea water. What will be the value of *h*, for which change in volume is 0.05%? **Take:** E = 200 GPa and μ = 0.3. Unit weight of sea water = 10.08 kN/m^3.

(a) 8333 m (b) 8267 m
(c) 1066 m (d) 1080 m

Q.18 A ring mass of 60 kg encircles a bar and falls through a distance *h* before checked by a stop fixed to the bottom of the bar which hangs vertically from the rigid support. The bar is of steel which has modulus of elasticity of 2.05×10^5 N/mm^2, and is 40 mm in diameter and 2.5 m long. If the maximum instantaneous extension in the bar is 1.25 mm. What is the value of *h*?

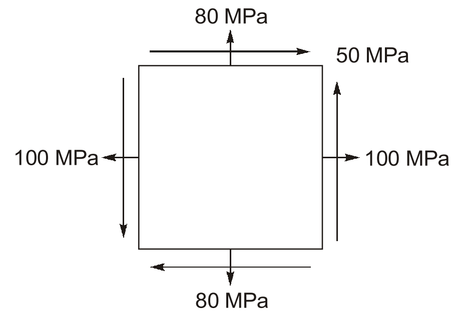
(a) 588.61 mm (b) 125.01 mm
(c) 135.53 mm (d) 136.78 mm

Q.19 A tapering rod of length 500 mm fixed at both ends is subjected to a rise in temperature by 5°C. Take E = 200 GPa and $\alpha = 12 \times 10^{-6}$ per °C. If its diameter uniformly increases from 70 mm to 140 mm, the maximum stress produced in the rod is __________MPa.

Q.20 A cantilever beam which is having deflection of $\frac{WL^3}{8EI}$ under a total load of W, where L is length of beam, E is modulus of elasticity and I is moment of inertia. What is the total strain energy due to bending ?

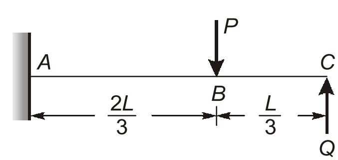
(a) $\frac{W^2L^3}{16EI}$ (b) $\frac{W^2L^3}{40EI}$
(c) $\frac{W^2L^3}{24EI}$ (d) $\frac{W^2L^3}{32EI}$

Q.21 Bi-axial state of stress at a point is shown below. What will be the value of principal stresses and maximum in-plane shear stress.



(a) σ_1 = 141 MPa, σ_2 = 39 MPa, τ_{max} = 50 MPa
(b) σ_1 = 141 MPa, σ_2 = 39 MPa, τ_{max} = 70.5 MPa
(c) σ_1 = 282 MPa, σ_2 = 78 MPa, σ_{max} = 70.5 MPa
(d) σ_1 = 141 MPa, σ_2 = 39 MPa, σ_{max} = 51 MPa

Q.22 The ratio of force *P* to force *Q* such that deflection at point *C* becomes zero is _________.



ANSWERS

1. (c)	2. (a)	3. (a)	4. (50)
5. (a)	6. (a)	7. (159.60)	8. (0)
9. (c)	10. (c)	11. (666.67)	12. (264.6)
13. (57.83)	14. (c)	15. (141.4)	16. (a)
17. (b)	18. (c)	19. (240)	20. (b)
21. (d)	22. (1.9285)		

HINTS

1. (c)

Normal reaction,

$$N = 500 - P\sin 30°$$
$$= 500 - 100 \times 0.5 = 450 \text{ N}$$

Limiting Frictional force,

$$F_{max.} = \mu N = 0.3 \times 450 = 135 \text{ N}$$

But $F = 100 \cos 30° = 86.6 \text{ N} \le F_{max}$

So, Friction force $= 86.6$ N

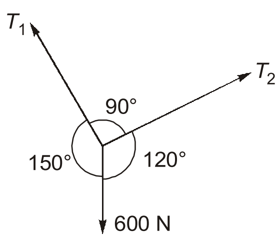
2. (a)

$$\tan\theta = \frac{3}{3} = 1 \Rightarrow \theta = 45°$$

$$F_{CB} \sin 45° = 40$$

$$\therefore \quad F_{CB} = 40\sqrt{2} \text{ kN}$$

3. (a)



By Lami's Theorem,

$$\frac{T_1}{\sin 120°} = \frac{T_2}{\sin 150°} = \frac{600}{\sin 90°}$$

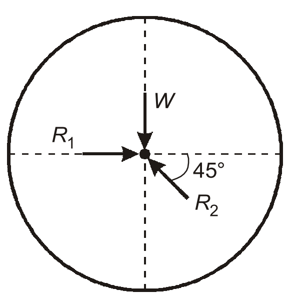
$$\therefore \quad T_1 = 600 \sin 120°$$

$$= 519.31 \simeq 520 \text{ N}$$

and $\quad T_2 = 600 \sin 150°$

$$T_2 = 300 \text{ N}$$

4. (50)



$$R_2 \cos 45° = R_1$$

$$R_2 \sin 45° = W$$

$$R_2 = W \times \sqrt{2}$$

$$R_1 = W \times \sqrt{2} \times \frac{1}{\sqrt{2}} = W$$

$$R_1 = 50 \text{ N} \qquad [\because W = 50 \text{ N}]$$

5. (a)

$$W = \int_0^3 F \cdot dx = \int_0^3 (10 + 0.5x)dx$$

$$= \left[10x + 0.50\frac{x^2}{2}\right]_0^3$$

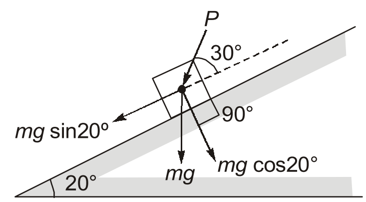
$$= \left[10 \times 3 + 0.5 \times \frac{3^2}{2} - 0\right] = 32.25 \text{ J}$$

6. (a)

$$V^2 = u^2 + 2as$$

$$(25)^2 = (0)^2 + 2 \times a \times 50$$

$$a = \frac{25 \times 25}{4 \times 25} = 6.25 \text{ m/s}^2$$



By Newton's second law,

$mg \sin 20° + P\cos 30° = 100 \times 6.25$

$P\cos 30° = 625 - 981 \sin 20° = 289.47824$

$$P = 334.26 \text{ N}$$

7. (159.60) (159 to 160)

$$\frac{10 \times 9.8}{\sin(180 - 30 - 45)} = \frac{T_1}{\sin 135} = \frac{T_2}{\sin 120}$$

$$\frac{98}{\sin 105} = \frac{T_1}{\sin 135} = \frac{T_2}{\sin 120}$$

$$T_1 = 98 \times \frac{\sin 135}{\sin 105} = 71.741 \text{ N}$$

$$T_2 = 98 \times \frac{\sin 120}{\sin 105} = 87.864 \text{ N}$$

$$T_1 + T_2 = 71.741 + 87.864 = 159.60 \text{ N}$$

8. (0)

Assume that force $\vec{Q}$ is greater one, $\vec{P}$ is smaller one and $\vec{R}$ is resultant of $\vec{P}$ and $\vec{Q}$.

In ΔOBC,

$$\cos 45° = \frac{R}{Q} = \frac{R}{25}$$

$$R = 25 \cos 45°$$

$$R = \frac{25}{\sqrt{2}} \text{ N}$$

$$\sin 45° = \frac{\vec{P}}{\vec{Q}} = \frac{P}{25}$$