

# WORKDOOK 2026



### **Computer Science & IT**

Discrete & Engineering Mathematics



© Copyright: Subject matter to MADE EASY Publications, New Delhi. No part of this book may be reproduced or utilised in any form without the written permission.

## **Propositional Logic**



### T1 : Solution

(a)  

$$[(p \land q) \rightarrow (p \lor q)] \lor \sim p \lor q \equiv \sim (p \land q) \lor (p \lor q) \lor \sim p \lor q$$

$$\equiv (\sim p \lor \sim q) \lor (p \lor q) \lor \sim p \lor q$$

$$\equiv (\sim p \lor p) \lor (\sim q \lor q) \lor \sim p \lor q$$

$$\equiv T \lor T \lor \sim p \lor q$$

$$\equiv T$$

### T2: Solution

(d)

$$\exists x (P(x) \to \exists y \ Q(y)) \cong \neg \forall x \neg (P(x) \to \exists y \ Q(y))$$
$$\cong \exists x (\neg P(x) \lor \exists y \ Q(y))$$
$$\cong \exists x (\neg \exists y \ Q(y) \to \neg P(x))$$
$$\cong \neg \forall x (P(x) \land \neg \exists y \ Q(y))$$

### T3 : Solution

### (b)

For every person x, if person x is female and person x is a parent, then there exists a person y such that person x is the mother of person y.

F(x): x is female P(x): x is a parent.

M(x, y) : x is the mother of y

 $\forall x \left( \left( F(x) \land P(x) \right) \to \exists y M(x, y) \right)$ 

 $\cong \forall x \exists y ((F(x) \land P(x)) \rightarrow M(x, y))$ 

www.madeeasypublications.org





### T4 : Solution

### (b)

Given:  $\forall x \in \mathbb{R}$ , if x > 2 then  $x^2 > 4$ 

Contrapositive is:  $\forall x \in \mathbb{R}$ , if  $x^2 \le 4$  then  $x \le 2$ 

Converse is:  $\forall x \in \mathbb{R}$ , if  $x^2 > 4$  then x > 2

Inverse is:  $\forall x \in \mathsf{R}$ , if  $x \le 2$  then  $x^2 \le 4$ 

### T5 : Solution

### (c)

 $\forall x \forall y \forall z ((Apple (x) \land Apple (y) \land Apple (z)) \rightarrow (x = y \lor x = z \lor y = z))$ 

### T6 : Solution

### (a)

 $\ln I_1$  both hypothesis are true and conclusion is also true by Modes Ponens.

Socrates is human : p

Socrates is mortal : q

 $p \rightarrow q$ 

р

 $\therefore$  q  $\Rightarrow$  by Modus Ponens

 $\ln I_2$  both hypothesis are true and conclusion is also true by Modus Tollens.

MADE EASY is closed today : q

It will rain today : p

 $p \rightarrow q$ 

~ q

 $\overline{\therefore -p} \Rightarrow$  by Modus Tollens

### T7 : Solution

### (d)

р	q	$p \rightarrow q$	$\sim (p \rightarrow q)$	~q	$\sim (p \rightarrow q) \rightarrow \sim q$
Т	Т	Т	F	F	Т
Т	F	F	Т	Т	Т
F	Т	Т	F	F	Т
F	F	Т	F	Т	Т

р	q	$p \rightarrow q$	$\sim q \rightarrow \sim p$	$(p \to q) \leftrightarrow (\sim q \to \sim p)$
Т	Т	Т	Т	Т
Т	F	F	F	Т
F	Т	Т	Т	Т
F	F	Т	Т	Т

©	Copyright	
---	-----------	--

MADE	EASY
	Publications

www.madeeasypublications.org



### **T8** : Solution

### (d) (i)

$$\sim (\forall x) \exists y P(x, y) \equiv (\exists x) (\forall y) [\sim P(x, y)]$$

$$\exists x \forall y [\sim P(x, y)] \equiv (\exists x) (\forall y) [\sim P(x, y)]$$

Above logic is true.

$$\sim (\forall x) P(x) \equiv \exists x [\sim P(x)]$$
$$\exists x [\sim P(x)] \equiv \exists x [\sim P(x)]$$

Above logic is true.

$$(iii) \sim (\exists x)(\forall y)[P(x,y) \lor Q(x,y)] \equiv (\forall x)(\exists x)[\sim P(x,y) \land \sim Q(x,y)]$$

 $(\forall x)(\exists x)[\sim P(x,y) \land \sim Q(x,y)] \equiv (\forall x)(\exists x)[\sim P(x,y) \land \sim Q(x,y)]$ 

Above logic is true.

Since all the above option are correct.

### **T9**: Solution

### (c)

 $\neg \forall z [P(z) \rightarrow (\neg Q(z) \rightarrow P(z))]$   $\exists z \neg [\neg P(z)] \lor \neg (\neg Q(z) \lor P(z))]$   $\exists z \neg [\neg P(z) \lor (Q(z) \lor P(z))]$   $\exists z \neg [P(z) \land (\neg Q(z) \land \neg P(z))]$   $\exists z [P(z) \land \neg Q(z) \land \neg P(z)]$ [::  $P \cdot \neg P = 0$ ]

### T10 : Solution

### (b)

Option (a) is correct because every valid formula is tautology and every tautology is satisfiable. Option (b) is incorrect because some satisfiable are tautology. Option (c) is correct because no contradiction is satisfiable.

#### T11 : Solution

### (c)

There are atmost two apples :  $\forall x \ \forall y \ \forall z \ ((Apple (x) \land Apple (y) \land Apple (z)) \rightarrow (x = y \lor x = z \lor y = z))$ There are exactly two apples :  $\exists x \ \exists y \ (Apple (x) \land Apple (y) \land (x \neq y) \land \forall z \ (Apple (z) \rightarrow ((z = x) \lor (z = y))))$ There is atmost one apple :  $\forall x \ \forall y \ ((Apple (x) \land Apple (y)) \rightarrow (x = y \lor y = x)))$ There is exactly one apple :  $\exists x \ (Apple (x) \land \forall y \ (Apple (y) \rightarrow (x = y)))$ 



### T12 : Solution

(c)

 $\forall x \in \mathbb{N} [x \neq 7 \land \operatorname{Prime}(x) \to \neg \operatorname{Divisibleby7}(x)] \cong \\ \forall x \in \mathbb{N} [x = 7 \lor \neg \operatorname{Prime}(x) \lor \neg \operatorname{Divisibleby7}(x)] \cong \\ \neg \exists x \in \mathbb{N} [x \neq 7 \land \operatorname{Prime}(x) \land \operatorname{Divisibleby7}(x)] \\ \text{All represents that "no prime except 7 is divisible by 7".} \end{cases}$ 

### T13 : Solution

### (a)

Everybody loves Mahesh:  $\forall x \text{ Loves } (x, \text{ Mahesh})$ Everybody loves somebody:  $\forall x \exists y \text{ Loves } (x, y)$ There is somebody whom everybody loves:  $\exists y \forall x \text{ Loves } (x, y)$ There is somebody whom no one loves:  $\exists y \forall x \neg \text{ Love } (x, y)$ 

### T14 : Solution

### (d)

 $\begin{aligned} \forall x \ P(x) \to \forall x \ [P(x) \lor Q(x)] \text{ is valid} \\ \exists x \ \exists y \ P(x,y) \to \exists y \ \exists x \ P(x,y) \text{ is valid} \\ \exists x \ [R(x) \lor S(x)] \to \exists x \ R(x) \lor \exists x \ S(x) \text{ is also valid} \end{aligned}$ 

### T15 : Solution

(b)  $\neg (\neg p \lor q) \lor (r \to \neg s) \cong (p \land \neg q) \lor (\neg r \lor \neg s) \cong (p \lor \neg r \lor \neg s) \land (\neg q \lor \neg r \lor \neg s)$ 

### T16 : Solution

### (d)

P1, P2 and P3 are equivalent. All are representing the same statement: "there are exactly two apples".

### T17 : Solution

### (d)

All the statements give true as the truth value. None of them give false as the truth value.

$\sim$	~			1.1	
(C)	$( \cap$	nv	ria	ht	
~	~~	μ,	9		





### T18 : Solution

### (11)

We wish to make

 $\neg((p \Rightarrow q) \land (\neg r \lor \neg s)) = 1$  $\Rightarrow (p \Rightarrow q) \land (\neg r \lor \neg s) = 0$  $\Rightarrow (p \Rightarrow q) = 0 \qquad \dots(1)$ 

 $Or \quad \neg r \lor \neg s = 0$ 

Now (1) is satisfies only when p = 1 and q = 0.

Equation (2)  $\neg r \lor \neg s = 0$ , iff  $r \land s = 1$ 

i.e. r = 1 and s = 1

i.e. x is a perfect square and x is a prime number. Which is not possible so condition (2) cannot be satisfied by any x.

...(2)

So condition (1) must be satisfies which is p = 1 and q = 0 i.e.  $x \in \{8, 9, 10, 11, 12\}$  and x is not a composite.

Now the only value of x which satisfies this is x = 11.

So correct answer is x = 11.



## Combinatorics and Recurrence Relations



### T1 : Solution

(b)

Total number of letters = 15 Number of T's = 3 First place 12 letters other than T's at dot places. X. X

The number of ways =  $\frac{12!}{5!3!2!}$ 

Since no two T's are together, thus place T's at cross places whose number = 13

Their arrangements are =  $\frac{{}^{13}P_3}{3!}$ 

Total number of ways =  $\frac{12!}{5!3!2!} \times \frac{^{13}P_3}{3!}$ 

T2 : Solution

(b)

$$\sum_{k=0}^{n} \binom{n}{k} x^{k} \cdot y^{n-k} = (x+y)^{n}$$

$$\sum_{k=0}^{n} \binom{n}{k} (-1)^{k} \cdot 3^{n-k} = ((-1)+3)^{n} = 2^{n}$$



### T3 : Solution

### (c)

The candidate is unsuccessful if he fails in 9 or 8 or 7 or 6 or 5 papers.

: The number of ways to be unsuccessful

$$= {}^{9}C_{9} + {}^{9}C_{8} + {}^{9}C_{7} + {}^{9}C_{6} + {}^{9}C_{5}$$
  
$$= {}^{9}C_{0} + {}^{9}C_{1} + {}^{9}C_{2} + {}^{9}C_{3} + {}^{9}C_{4}$$
  
$$= \frac{1}{2} ({}^{9}C_{0} + {}^{9}C_{1} + {}^{9}C_{2} + \dots + {}^{9}C_{9})$$
  
$$= \frac{1}{2} (2^{9}) = 2^{8}$$

### T4 : Solution

(b)  

$$T(n) - 4T(n-1) + 3T(n-2) = 0$$
  
 $x^2 - 4x + 3 = 0$   
 $(x-3)(x-1) = 0 \implies x = 3, 1$   
General Solution:  $T(n) = A.3^n + B.1^n$   
 $= A.3^n + B$   
Given:  $T(0) = 0$  and  $T(1) = 2$   
By taking  $n = 0 \implies T(n) = A.3^n + B$   
 $T(0) = A + B \implies A + B = 0$  ...(i)  
By taking  $n = 1 \implies T(1) = A.3 + B \implies 3A + B = 2$  ...(ii)  
From (i) and (ii)  $\implies A = 1, B = -1$   
 $T(n) = A.3^n + B[\because$  Substitute  $A = 1$  and  $B = -1$ ]  
 $\implies T(n) = 3^n - 1$ 

**T5** : Solution

(a)

Put

$$x + y + z = 17$$
  

$$x \ge 1, y \ge 1, z \ge 1$$
  

$$x = 1 + u, y = 1 + v, z = 1 + w$$

 $\Rightarrow$  U + V + W = 14

Now number of solutions in non-negative integers

$$\begin{pmatrix} 14+3-1\\14 \end{pmatrix} = \begin{pmatrix} 16\\14 \end{pmatrix} = \begin{pmatrix} 16\\2 \end{pmatrix} = 120$$

www.madeeasypublications.org





### T6 : Solution

### (b)

Example: In how many ways can the pack of 52 cards be partitioned into 4 sets of size B.

$$\begin{pmatrix} 52\\13 \end{pmatrix} \begin{pmatrix} 39\\13 \end{pmatrix} \begin{pmatrix} 26\\13 \end{pmatrix} \begin{pmatrix} 13\\13 \end{pmatrix} = \frac{(52)!}{(13!)^4}$$

All partitions are not distinct. Each distinct partition arises in 4! ways. Therefore # ways =  $\frac{(52)!}{(13!)^4 \cdot 4!}$ 

Similarly,

# $\frac{\prod_{i=0}^{m-1} \binom{mn-in}{n}}{m!} = \frac{(mn)!}{(n!)^m \cdot m!}$

### T7 : Solution

### (a)

 $T(n) = C_1 \cdot 3^n + C_2 \cdot 2^n$ General solution: [Where Homogeneous part:  $(x-3) = 0 \implies x = 3$ ] Particular solution:  $C_2.2^n$ T(0) = 1, T(1) = 3. T(0) + 2' = 3 + 2 = 5 $T(n) = C_1 \cdot 3^n + C_2 \cdot 2^n$ 
$$\begin{split} T(0) &= C_1 . 3^0 + C_2 . 2^0 \Rightarrow 1 = C_1 + C_2 \\ T(1) &= C_1 . 3' + C_2 . 2' \Rightarrow 5 = 3C_1 + 2C_2 \end{split}$$
 $\overline{C_1 = 3, C_2 = -2}$   $T(n) = 3.3^n - 2.2^n = 3^{n+1} - 2^{n+1}$ *.*..

### **T8** : Solution

### (c)

Each question can be answered in 4 ways.

The number of ways =  $4^{65}$ *.*..

### **T9** : Solution

### (c)

$$T(n) = 10.T(n-1)-25.T(n-2)$$

$$\Rightarrow 25T(n-2) - 10.T(n-1) + T(n) = 0$$

$$\Rightarrow 25 - 10x - x^{2} = 0$$

$$\Rightarrow (x-5)^{2} = 0$$

$$T(n) = C_{1} \cdot 5^{n} + C_{2} \cdot n \cdot 5^{n}$$

$$T(0) = 5, T(1) = 5$$

$$T(0) = C_{1} \cdot 5^{\circ} + C_{2} \cdot 0 \cdot 5^{\circ}$$

$$\Rightarrow 5 = C_{1}$$





$$T(1) = C_1 \cdot 5^1 + C_2 \cdot 1 \cdot 5^1$$

$$5 = 5C_1 + 5C_2$$

$$\Rightarrow \qquad C_1 + C_2 = 1$$

$$\Rightarrow \qquad C_2 = 1 - C_1 = 1 - 5 = 4$$

$$\therefore \qquad T(n) = 5 \cdot 5^n + (-4)n \cdot 5^n$$

$$= 5^{n+1} - 4n \cdot 5^n$$

### T10 : Solution

### (10)

We wish to find coefficient of  $x^{12}$  in  $(x^3 + x^4 + x^5 + \dots)^3$  $= (x^3(1 + x^1 + x^2 + \dots))^3$   $= x^9(1 + x + x^2 \dots)^3$   $= \frac{x^9}{(1 - x)^3} = x^9 \sum_{r=0}^{\infty} {}^{3-1+r}C_r X^r = x^9 \sum_{r=0}^{\infty} {}^{r+2}C_r X^r$ Now to make  $x^{12}$  we need to put r = 3

Now to make  $x^{12}$  we need to put r = 3So coefficient of  $x^{12}$  is  ${}^{3+2}C_3 = {}^5C_3 = {}^5C_2 = 10$ 



## **Set Theory and Algebra**



### T1 : Solution

(d)

$$f : N \to Z$$
$$f(0) = f(2) = 3$$

 $\Rightarrow$  f is not injective

Clearly *f* is not surjective, all numbers in Z do not have preimages in N (example: 0 has no preimage) *f* is function which is not injective and not surjective.

### T2 : Solution

### (d)

Countable sets : Finite Set, N, O<sup>+</sup>, Z<sup>+</sup>, Z<sup>-</sup>, Z denumerable

Uncountable sets : Real numbers

: Set of real numbers in the interval [0, 1] is uncountable because they can not be enumerated.

### T3 : Solution

### **(b)** (*i*)

 $|x - y| \le 2$ If we take y = (x)then  $|x - (x)| \le 2$  True So it is reflexive.

- (*ii*) If we do |x y| or |y x|, answer will be same. So it is symmetric.
- (*iii*) If we do [x (x 2)] the [(x 2) (x 4)], the [x (x 4)] not follow the condition So it is not transitive.

```
© Copyright
```





### T4 : Solution (c) $f(x) = (5x + 1)^2$ $y = (5x + 1)^2$ $\Rightarrow$ $\sqrt{y} = 5x + 1$ $\Rightarrow$ $\sqrt{y} - 1 = 5x$ $\Rightarrow$ $x = \frac{\sqrt{y} - 1}{5}$ (:: swap x and y for inverse) $\Rightarrow$ $y = \frac{1}{5} \left( \sqrt{x} - 1 \right)$ $\Rightarrow$ $f^{-1}(x) = \frac{1}{5}(\sqrt{x}-1)$ $\Rightarrow$ T5 : Solution (d) $x^* y = x + y + xy$ Let *e* be the identity $x^*e = x + e + xe$ [Put e = 0] x = x

$$\therefore \quad \boxed{e=0} \quad \Rightarrow \quad 0 \text{ is the identity of S}$$

Let y is the inverse of x

Then

$$x^* y = e \Longrightarrow x^* y = 0$$
$$x + y + xy = 0$$

$$\Rightarrow \qquad x + y + xy = 0$$
$$\Rightarrow \qquad x + y(1 + x) = 0$$

$$\Rightarrow \qquad y = \frac{-x}{1+x}$$

$$\Rightarrow 1 + x \neq 0 \Rightarrow x \neq -1$$

Inverse of 
$$x = \frac{-x}{1+x}$$
;  $\forall x \in \mathbb{R} \setminus \{-1\}$ 

 $\therefore$  S = R\{-1} is an abelian group.

[Note: S is Commutative and Associative over \*]





### T6 : Solution

(c)



Same Venn diagram can be produced for both S1 and S2.

∴ S1 = S2

### T7 : Solution

(c)

$$-1 \le \sin x \le +1$$
  
$$-5 \le 5 \sin x \le 5$$
  
$$-2 \le 3 + 5 \sin x \le 8$$
  
$$-2 \le f(x) \le 8$$

 $\Rightarrow$  Range is: [-2, 8]

### T8 : Solution

### (d)

R = {(1, 1), (1, 2), (1, 3), (1, 4), (2, 1), (2, 2), (2, 3), (3, 1), (3, 2), (4, 1)} R is not reflexive: (3, 3) ∉ R R is symmetric: if  $(x + y) \le 5 \Rightarrow (y + x) \le 5$ R is not antisymmetric: (1, 2) and (2, 1) in R R is not transitive: (3, 1) and (1, 3) in R, but (3, 3) ∉ R  $\therefore$  R is symmetric

### **T9** : Solution

(d)

 $X = \{\{\}, \{a\}\}$ 

Power set =  $\{\{ \}, \{\{ \}\}, \{\{ \}\}, \{\{ \}\}, \{a\}\}\}$ 

power set contain 2<sup>n</sup> element of original set.



### T10 : Solution

### (d)

N is countable set.

Hence, Subset of any countable set is also countable and product of two countable sets is also countable.

### T11 : Solution

### (c)

Commutative for multiplication of matrices does not hold.

AB ≠ BA

If AB is possible to multiply that does not mean that BA can also be multiplied. Moreover the result will not be the same except for the case when the 2 matrices are same.

#### T12 : Solution

(2)

$$f(n) = f\left(\frac{n}{2}\right) \text{ if } n \text{ is even}$$
  
$$f(n) = f(n+5) \text{ if } n \text{ is odd}$$

 $\langle \mathbf{n} \rangle$ 

 $f: N^+ \rightarrow N^+$ 

Now

$$f(2) = f\left(\frac{2}{2}\right) = f(1)$$
  

$$f(3) = f(3 + 5) = f(8) = f\left(\frac{8}{2}\right) = f(4)$$
  

$$= f\left(\frac{4}{2}\right) = f(2) = (1)$$

So

$$f(1) = f(2) = f(3) = f(4) = f(8)$$

Now let us find  $f(5) = f(5 + 5) = f(10) = f\left(\frac{10}{2}\right) = f(5)$  so f(5) = f(10)Now let us find f(9)

$$f(9) = f(9+5) = f(14) = f\left(\frac{14}{2}\right) = f(7)$$
$$= f(7+5) = f(12) = f\left(\frac{12}{2}\right) = f(6)$$

$$= f\left(\frac{6}{2}\right) = f(3)$$

So

f(9) = f(7) = f(6) = f(3) = f(1) = f(2) = f(4) = f(8)For n > 10, the function will be equal to one of f(1),  $f(2) \dots f(10)$ So the maximum number of distinct values f takes is only 2. First is f(1) = f(2) = f(3) = f(4) = f(8) = f(9) = f(7) = f(6)Second is f(5) = f(10)All other *n* values will give only one of these two values.

www.madeeasypublications.org

MADE EASY = Publications



### T13 : Solution

### (d)

If every subset of a lattice has LUB and GLB, then such a lattice is called as complete lattice. All of the given lattices are complete lattices, since all the lattices are having GLB and LUB.

### T14 : Solution

(d)

$$(A - B) - C = (A \cap \overline{B}) - C = A \cap \overline{B} \cap \overline{C}$$
$$(A - C) - (B - C) = (A \cap \overline{C}) - (B \cap \overline{C})$$
$$= (A \cap \overline{C}) \cap (\overline{B} \cup C)$$
$$= (A \cap \overline{C} \cap \overline{B}) \cup (A \cap \overline{C} \cap C)$$
$$= (A \cap \overline{C} \cap \overline{B}) \cup (A \cap \phi)$$
$$= (A \cap \overline{C} \cap \overline{B}) \cup \phi$$
$$= A \cap \overline{C} \cap \overline{B}$$

### T15 : Solution

### (c)

A distributive lattice need not be a complemented lattice. A complemented lattice may or may not be distributive lattice. However a complemented has to be bounded because the complement property requires 0 and 1 which when present will make the lattice bounded.

### T16 : Solution

### (b)

(a, b) R(c, d) if  $a \le c$  or  $b \le d$  **P**: *R* is reflexive **Q**: *R* is transitive Since,  $(a, b) R(a, b) \Rightarrow a \le a$  or  $b \le b$   $\Rightarrow t$  or *t* Which is always True, *R* is reflexive. Now let us check transitive property Let  $(a, b) R(c, d) \Rightarrow a \le c$  or  $b \le d$ and  $(c, d) R(e, f) \Rightarrow c \le e$  or  $d \le f$ Now let us take a situation  $a \le c$  (True) or  $b \le d$  (false) and  $c \le e$  (False) or  $d \le f$ (True) Now we can get neither  $a \le e$  nor  $b \le f$ So, (a, b) R(c, d) and  $(c, d) R(e, f) \ne (a, b) R(e, f)$ . So clearly *R* is not transitive.

So P is true and Q is false. Choice (b) is correct.



### **Graph Theory**



### T1 : Solution

### (d)

To find maximum number of edges in the disconnected graph with *n*-vertices, form a complete graph with (n-1) vertices and 1 vertex is isolated. So the graph will be disconnected and addition of any edge will make the graph as connected.

: Maximum number of edges in disconnected graph can present:

$$^{(n-1)}C_2 = \frac{(n-1)(n-2)}{2}$$

### T2: Solution

(a)





Any planar graph  $G \Rightarrow \chi(G) \le 4$ Every face is bordered by exactly 3 edges  $\Rightarrow \chi(G) \ge 3$  $\therefore \qquad \chi(G) = 3 \text{ or } 4$ So,  $\chi(G)$  can never have the value 2





 $G_2$ : not Hamiltonian graph [:: Hamiltonian cycle does not exists in  $G_2$ ] :: Only  $G_1$  is Hamiltonian graph.

### T4 : Solution

### (d)

Let  $n = 2 \implies \#$  vertices = 8 [:: # vertices in G = 4n]



 $\Rightarrow$  3 components

[Note: For any n, the #components in G = 3]

### T5 : Solution

### (b)

 $V(C_1) = \{1, 3, 5, 7\} \Rightarrow m_1 = 4$   $V(C_2) = \{2, 6\} \Rightarrow m_2 = 2$  $V(C_3) = \{4, 8\} \Rightarrow m_3 = 2$ max = 4

In general, 'G' with 4n vertices has 3 components

© Copyright

*.*..



### T6 : Solution

### (b)

**Example:**  $C_{2n} \Rightarrow n = 2 \Rightarrow C_4$ 



A cycle graph with even vertices has 2 perfect matchings.

### T7 : Solution

### (c)

 $S_1$  is true but converse of  $S_1$  is not true. If a graphs is Hamiltonian that does not mean that  $d(v) \ge n/2$  for each vertex in G.

 $S_2$  is true and converse of  $S_2$  is also true because G is connected graph. If g is Eulerian then every vertex has to have even degree.

### **T8** : Solution

### (a)

 $G_1$  and  $G_2$  are isomorphic

 $a \rightarrow 1$   $b \rightarrow 3$   $c \rightarrow 4$   $d \rightarrow 5$   $e \rightarrow 6$  $f \rightarrow 2$ 

### T9 : Solution

### (c)

G is a planar graph. Every planar graph is 4-colorable. Every face is bordered by 3 edges.

So graph has possibilities of 3 or 4 colors.

 $k_3$  colored with 3 and  $k_4$  colored with 4 colors.





Detailed Explanations of Try Yourself Questions : GATE 2026

### T10 : Solution

(c)

 $S_1$ : The maximum number of edges =  $\frac{(n-1)(n-2)}{2}$  when a graph has disconnected into two components

where one component with a single vertex and other component is complete graph on (n-1) vertices.

- $\therefore$   $S_1$  is true.
- **S**<sub>2</sub>: G is a forest if and only if G has (n k) edges. If G is a forest, then each connected component is a tree.

**Example:** *G* has 10 vertices and 3 components. Two components are having a single vertex. Third component must be a tree with 7 edges i.e., *G* has 3 components with 7 edges where two components with no edge and third component with 7 edges.

 $\therefore$   $S_2$  is true.

#### 

