Production & Industrial Engineering

Operations Research and Operations Management

Comprehensive Theory with Solved Examples and Practice Questions





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Operations Research and Operations Management

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CHAPTER 02

Queuing Theory

INTRODUCTION

One of the major issues in the analysis of any traffic system is the analysis of delay. Delay is a more subtle concept. It may be defined as the difference between the actual travel time on a given segment and some ideal travel time of that segment. This raises the question as to what is the ideal travel time. In practice, the ideal travel time chosen will depend on the situation; in general, however, there are two particular travel times that seem best suited as benchmarks for comparison with the actual performance of the system. These are the travel time under free flow conditions and travel time at capacity.

Most recent research has found that for highway systems, there is comparatively little difference between these two speeds. That being the case, the analysis of delay normally focuses on delay that results when demand exceeds its capacity; such delay is known as queuing delay, and may be studied by means of queuing theory. This theory involves the analysis of what is known as a queuing system, which is composed of a server; a stream of customers, who demand service; and a queue, or line of customers waiting to be served.

2.1 Issues involved in Waiting Line

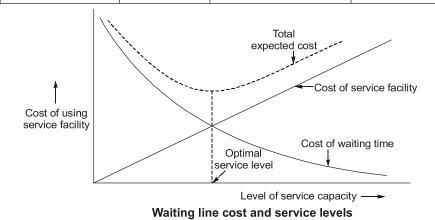
The most important issue in waiting line problem is to decide the best level of service that the organisation should provide. For example, to cope up with the railway reservation queue, how many counters must be opened? If the counters are too less, there will be very long queue, resulting in long waiting time. This results in dissatification among the customers. However, if the service counters are too many the counters may remain unoccupied for quite some time. This would result in loss to the service organisation. An important issue to understand in queuing problem is about arrival pattern. Generally, the arrival of customers is random, which may be governed by a probability distribution. Besides this, the arrival may also be governed by hours of a day, season, days of month, etc. For example, the arrival at railway reservation booth is more at morning hours as compared to afternoon. Similarly, longer queues may be observed at rail reservation counters when summer vacation are or puja vacation are due. The management may open more or less service counters, depending upon the arrival; but each extra counter means additional cost in running this service. Use of computers in processing data and updating files at the service counter is now very common. The reason is simple. Computer is very fast, accurate, programmable, good in storage and retrieval features for data, and consistent. A reduced and dependable service time is what customer and management want.

The key issue in waiting line is to provide a compromise between good service (by less service time) and less cost in running the service points. Figure 2.1 illustrates that the total expected cost of service, which is the sum of providing service and cost of waiting time, is minimum at certain service level. This service level should be optional service level.



			_		
S. No.	Application Area	Arrival	Waiting Line	Service Facility	
1	Factory	Material/tools	In-process inventory (WIP)	P) Work stations	
2	Assembly line	Sub-assemblies	WIP	Employees currently processing the WIP	
3	Machine maintenance	Repair tools & equipment	Machines needing repair	Maintenance crew	
4	Airport	Aeroplanes	Aeroplanes ready to fly	Runway	
5	Bank	Customer	Deposit/withdrawal	Bank employee & computer	
6	Walk-in-interview	Job seekers	Applicants	Interviewers	
7	Phone exchange	Dialled number	Caller	Switchboard	
8	Govt. office	Files	Backlog files	Clerks	
9	Post office	Letters	Mailbox	Postal employees	
10	Executive note	Dictation note	Letters to be typed	Secretary	
11	Grocery shop	Customers	Customer on the counter	Checkout clerks and bag packers	
12	Traffic light	Vehicles	Vehicles in line	Traffic signals crossing	
13	Car service station	Cars	Unserviced cars	Service facilities	
14	Railways	Passengers	Waiting passengers on platform/waiting room		
15	Tool crib	Mechanics	Waiting mechanics	Store keeper	
16	Hospital	Patients	Sick people	Doctor & operation facility	

Table. Some Applications of Waiting Line Problem



Characteristics of Queuing Process

One thing we have to remember is that when we speak of queue, we have to deal with two elements, i.e. Arrivals and Service facility. Entire queuing system can be completely described by:

- (a) The input (Arrival pattern)
- (b) The service mechanism or service pattern,
- (c) The queue discipline and
- (d) Customer behavior.

2.2

Components of the queuing system are arrivals, the element waiting in the queue, the unit being served, the service facility and the unit leaving the queue after service. This is shown below in figure.



$$=\frac{\lambda}{\mu}=\frac{7.5}{20}=0.375$$

(ii) Average length of the queue (L_a)

$$=\frac{\rho^2}{1-\rho}=\frac{(0.375)^2}{1-0.375}=0.225=0.225$$
 person

(iii) Probability that it will take him more than 12 minutes altogether to wait for the phone to complete his call

=
$$e - (\mu - \lambda)\tau = e^{(7.5-20)\times\frac{12}{60}} = 0.082.$$



- As per queue discipline the following is not a negative behaviour of a customer:
 - (a) Balking
- (b) Reneging
- (c) Boarding
- (d) Collusion.
- Q.2 The expediting or follow up function in production control is an example of
 - (a) LIFO
- (b) FIFO
- (c) SIRO
- (d) Pre emptive
- Q.3 In M/M/S: N/FIFO the following does not apply
 - (a) Poisson arrival
 - (b) Limited service
 - (c) Exponential service
 - (d) Single server
- Q.4 The dead bodies coming to a burial ground is an example of:
 - (a) Pure Birth Process
 - (b) Pure Death Process
 - (c) Birth and Death Process
 - (d) Constant rate of arrival
- Q.5 The system of loading and unloading of goods usually follows:
 - (a) LIFO
- (b) FIFO
- (c) SIRO
- (d) SBP
- **Q.6** A steady state exist in a queue if:
 - (a) $\lambda > \mu$
- (b) $\lambda < \mu$
- (c) $\lambda \leq \mu$
- (d) λ≥μ
- Q.7 If the operating characteristics of a queue are dependent on time, then is said to be:
 - (a) Transient state
- (b) Busy state
- (c) Steady state
- (d) Explosive state.

- Q.8 A person who leaves the queue by losing his patience to wait is said to be:
 - (a) Reneging
- (b) Balking
- (c) Jockeying
- (d) Collusion
- Q.9 The characteristics of a queuing model is independent of:
 - (a) Number of service stations
 - (b) Limit of length of queue
 - (c) Service Pattern
 - (d) Queue discipline.
- Q.10 The unit of traffic intensity is:
 - (a) Poisson
- (b) Markow
- (c) Erlang
- (d) Kendall
- Q.11 In (M/M/1): ("/FCFS) model, the length of the system L_s is given by:
 - (a) $\rho^2 / 1 \rho$
- (b) $\rho/1 \rho$
- (c) $\lambda^2/(\mu-\lambda)$
- (d) $\lambda^2/\mu(\mu-\lambda)$
- Q.12 The queue discipline in stack of plates is :
 - (a) SIRO
- (b) Non-Pre-Emptive
- (c) FIFO
- (d) LIFO
- Q.13 SIRO discipline is generally found in:
 - (a) Loading and unloading
 - (b) Office filing
 - (c) Lottery draw
 - (d) Train arrivals at platform
- **Q.14** For a simple queue (M/M/1), $\rho = \lambda/\mu$ is known as:
 - (a) Poisson busy period
 - (b) Random factor
 - (c) Traffic intensity
 - (d) Exponential service factor



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is ir alre inte dist (a)	ndependent of the leady occurred price	s during a given time period number of arrivals that have or to the beginning of time arrivals follow	Q.23	booth is according an average time of 8	ephone calls at a tel to Poisson distributi minutes between two	on, with arrivals.	
The (a) (b)	e figure given repre	ngle Phase system gle-phase system		be exponentially 3.5 minutes. The phave to wait for morphone is free will be		with mean of at an arrival will nutes before the	
(d) Q.17 Wh	Multi channel mul nen the operating c stem dependent or	ti phase system characteristics of the queue n time, then it is said to be:	Q.24	is 15 customer/hou customers waiting	son arriving at a mob ir, probability of at lea in the queue is 40.96 store is custom	st three 6%. The	
(c) Q.18 Trat	Steady state Transient state ffic intensity is giv Mean arrival rate/I		Q.25	service time is 6 mi	n, arrival rate is 6/hr an n. What is the probab ess than 9 min in the s (b) 45.2% (d) 54.8%	ility that	
(c)	 (b) λμ (c) μ/λ (d) Number present in the queue / Number served 19 In Kenedall Notation - What does fourth turn 		Q.26	n service hr. What for one			
(a)	resent? Number of server			hour? (a) ₹26 (c) ₹22	(b) ₹16 (d) ₹18		
(b) Queue discipline(c) Queue length(d) Arrival probability distribution		Q.27 In a Queuing system, mean arrival time in 15 minute and mean service time is 10 min, then the number of jobs ahead will be			nin, then		
is 6 and cus dist in th	O For a telephone booth it is given that arrival rate is 6 person per hour with Poisson's distribution and it takes on an average 6 minute to leave a customer from telephone booth with exponential distribution. The expected number of customer in the queue is		Q.28	On a railway station reservation counter average 10 customers per hour visit for reservation. If the probability that serving a customer takes more han 12 minute is 8%. What will be the service rate? (a) 26.5 customers/hour			
	_	npty queue with Poisson's omer/hour and exponential		(c) 29 customers/ha	our		

service rate, $\mu = 10$ customer/hour will be___

Poisson's distribution and service time of 6 min

per customer with exponential distribution, what

is the probability that system is idle _____.

Q.22 For an arrival rate, $\lambda = 6$ customer per hour with

(d) 21.5 customers/hour

Q.29 On an average 120 patients per 24 hour require

the service of an emergency ward. On an average

a patient requires 10 minutes of active attention.

There is only one emergency ward which can

handle only one patient at a time. If it costs ₹100

per patient treated for clinic to obtain an average servicing time of 10 minutes, and that each minute of decrease in this average time would cost `10 per patient treated. If average size of queue is

reduced from $\left(\frac{25}{6}\right)$ to $\left(\frac{3}{2}\right)$ a patient then the

budget per patient of clinic will become ₹_

- Q.30 American bank has a single automated teller machine (ATM) located in a shopping centre. Data were collected during a period of peak usage on Saturday afternoon and it was found that the average time between customer arrivals is 2.1 minutes with a standard deviation of 0.8 minute. It was also found that it takes on an average 1.9 minutes for a customer to complete a transition with a standard deviation of 2 minutes. Expected server utilization in (%) is ___
- Q.31 American Vending Inc (AVI) supplies vended food to a large university. Because students of kick the machines out of anger and frustration, management has a constant repair problem. The machine breakdown on an average of three per hour and the breakdowns are distributed in a Poisson's manner. Downtime costs the company ₹25 per hour per machine, and each maintenance worker gets ₹4 per hour. One worker can service machine at an average rate of five per hour, distributed exponentially, two workers working together can service 7 per hour, distributed exponentially. The total cost per hour (in ₹) for two workers is _____.
- Q.32 On an average 5 customers reach a barber's shop every hour. The probability that exactly 3 customer will reach in a 30 minute period, assuming that arrival follows Poisson distribution is _____. (Write upto 3 decimal points)

ANSWERS

- **1.** (c) **2**. (d)
- 3. (d)
- **4**. (a)

- **5**. (a)
- **6**. (c)
- **7**. (a)

- **8**. (a)

- **9**. (d)
- **10**. (c)
- **11.** (b)
- **12**. (d)

- **13**. (c)
- **14**. (c)
- **15**. (b)
- **16**. (c)

- **17**. (c)
- **18**. (a)
- **19**. (b)
- **20**. (0.9)

- **21**. (5)
- **22.** (0.4)
- **23**. (6.36)
- **24.** (18.75)

- 25. (b)
- **26**. (c)
- **27**. (2)
- **28**. (a)
- **29**. (117.66) **30**. (90.5)
- **31**. (26.75)
- **32**. (0.214)

HINTS

19. (b)

a/b/c::d/e/f

d = Queue discipline

20. (0.9)

 $\lambda = 6$ customer per hour

 $\mu = \frac{60}{6} = 10$ customer per hour

 $\rho = \frac{\lambda}{10} = \frac{6}{10} = 0.6$

$$L_q = \frac{\rho^2}{1 - \rho}$$

$$=\frac{0.6^2}{1-0.6}=\frac{0.36}{0.4}=0.9$$

21. (5)

$$L'_q = \frac{1}{1-\alpha}$$

$$\rho = \frac{\lambda}{\mu} = \frac{8}{10} = 0.8$$

Length of non-empty queue,

$$L_q' = \frac{1}{1.08} = \frac{1}{0.2} = 5$$

22. (0.4)

 $\lambda = 6$ customer/hour

$$\mu = \frac{1}{6} \frac{\text{customer}}{\text{min}}$$
$$= \frac{60 \text{ customer}}{}$$

= 10 customer/hr

$$P_0 = 1 - \frac{\lambda}{\mu} = 1 - \frac{6}{10} = 0.4$$

23. (6.36)(6.30 to 6.40)

$$P(W_q \ge 12 \text{ min}) = \rho e^{-t/Ws}$$

where,

$$\rho = \frac{\lambda}{\mu} = \frac{1/8}{1/3.5} = \frac{3.5}{8} = 0.4375$$

$$W_s = \frac{L_s}{\lambda} = \frac{\lambda}{\lambda(\mu - \lambda)} = \frac{1}{(\mu - \lambda)}$$