

GATE 2024 Exam Solutions



ELECTRONICS ENGINEERING

Exam held on 11/02/2024 Forenoon Session









Detailed Solutions

Exam held on:

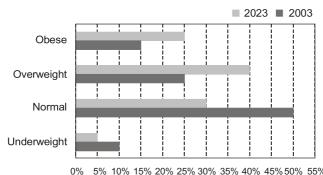
11-02-2024

Forenoon Session

SECTION - A

GENERAL APTITUDE

The bar chart shows the data for the percentage of population falling into different Q.1 categories based on Body Mass Index (BMI) in 2003 and 2023.



5% 10% 15% 20% 25% 30% 35% 40% 45% 50% 55%

Percentage of population

Based on the data provided, which one of the following options is INCORRECT?

- (a) The ratio of the percentage of population falling into overweight category to the percentage of population falling into normal category has increased in 20 years.
- (b) The ratio of the percentage of population falling into obese category to the percentage of population falling into normal category has decreased in 20 years.
- (c) The ratio of the percentage of population falling into underweight category to the percentage of population falling into normal category has decreased in 20 years.
- (d) The percentage of population falling into normal category has decreased in 20 years.

Ans. (b)

End of Solution

- Sequence the following sentences (P, Q, R, S) in a coherent passage: Q.2
 - P: Shifu's student exclaimed, "Why do you run since the bull is an illusion?"
 - Q: Shifu said. "Surely my running away from the bull is also an illusion."
 - R: Shifu once proclaimed that all life is illusion.
 - S: One day, when a bull gave him chase. Shifu began running for his life.
 - (a) RSPQ

(b) SPRQ

(c) SRPQ

(d) RPQS

Ans. (a)

End of Solution

- Five years ago, the ratio of Aman's age to his father's age was 1:4, and five years from Q.3 now, the ratio will be 2:5. What was his father's age when Aman was born?
 - (a) 32 years

(b) 35 years

(c) 28 years

(d) 30 year

LAUNCHING

MADE ERSY 2.0

DYNAMIC & IMPROVED FEATURES

- More efficient teaching
- Improved content
- Interactive technology
- Affordable fee structure
- New courses for GATE, ESE, UGC, SSC & other competitive Exams
- Basic concepts of engineering for college students
- Integrated offline & online batches
- Students centric approach
- Backup class provision
- Skill and industry oriented courses

○ 9021300500 **⊕** www.madeeasy.in

Delhi | Bhopal | Jaipur | Hyderabad | Kolkata | Pune



Ans. (d)

Five year ago

Son's age = x

Father's age = 4x

Five year after

Son's age = x + 10

$$\frac{x+10}{4x+10} = \frac{2}{5}$$

$$5x + 50 = 8x + 20$$

$$3x = 30$$

$$x = 10$$

Son's age five year ago = 10

Father's age five year age = 40

At the time of son's birth father's age = 40 - 10 = 30 year

End of Solution

- The greatest prime factor of $(3^{199} 3^{196})$ is Q.4
 - (a) 11

(b) 13

(c) 3

(d) 17

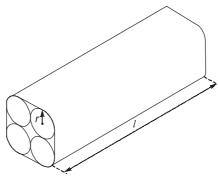
Ans. (b)

$$= 3^{196}(3^3 - 1) = 3^{196} \times 26 = 2 \times 3^{196} \times 13$$

Highest prime factors = 13

End of Solution

Q.5 Four identical cylindrical chalk-sticks, each of radius r = 0.5 cm and length l = 10 cm. are bound tightly together using a duct tape as shown in the following figure



The width of the duct tape is equal to the length of the chalk-stick. The area (in cm²) of the duct tape required to wrap the bundle of chalk-sticks once, is

(a) $10(8 + \pi)$

(b) $20(4 + \pi)$

(c) $10(4 + \pi)$

(d) $20(8 + \pi)$

Ans. (c)

End of Solution

Page



11-02-2024

Forenoon Session

Q.6 Two identical sheets A and B. of dimensions 24 cm \times 16 cm, can be folded into half using two distinct operations. FO1 or FO2.

In FO1. the axis of folding remains parallel to the initial long edge, and in FO2, the axis of folding remains parallel to the initial short edge.

If sheet A is folded twice using FO1, and sheet B is folded twice using FO2, the ratio of the perimeters of the final shapes of A and B is

(a) 11:18

(b) 18:11

(c) 11:14

(d) 14:11

Ans. (d)

Condition 1:

Folding first time

8

Folding first time

24

Perimeter = 2(24 + 4) = 56 cm

Condition 2:

Folding first time

12

Folding second time

16

Perimeter = 2(16 + 6) = 44 cm Ratio = 56 : 44 = 14 : 11

End of Solution

Q.7 If ' \rightarrow ' denotes increasing order of intensity, then the meaning of the words [charm \rightarrow enamor \rightarrow bewitch] is analogous to [bored \rightarrow _____ weary].

Which one of the given options is appropriate to fill the blank?

(a) worsted

(b) dead

(c) jaded

(d) baffled

Ans. (c)

End of Solution



Announcing

FOUNDATION COURSE For **ESE+GATE 2025 • GATE 2025**

The foundation batches are taught comprehensively which cover the requirements of all technical-syllabus based exams.

OFFLINE BATCHES AT DELHI

Commencing from

• **EE, EC & IN:** 15th Feb & 29th Feb • **CS:** 15th Feb & 5th Mar

• **CE**: 15th Feb & 26th Feb

• **ME**: 15th Feb & 29th Feb

LIVE-ONLINE BATCHES

Commencing from

Evening Batches: Hinglish

• **CS**: 20th Feb

• **EE/EC/IN**: 20th Feb

• **CE**: 20th Feb • **ME**: 20th Feb

Evening Batches

English: 20th Feb

Morning Batches

Hinglish: 22nd Feb

Stream: CE

www.madeeasyprime.com © 9021300500

Low Cost EMI Facility Available

Admissions open

Delhi Centre: 44-A/1, Kalu Sarai, Near Hauz Khas Metro Station, New Delhi - 110016 | Ph: 9021300500



11-02-2024

Forenoon Session

Q.8 For a real number x > 1,

$$\frac{1}{\log_2 x} + \frac{1}{\log_3 x} + \frac{1}{\log_4 x} = 1$$

The value of x is

(a) 24

(b) 12

(c) 4

(d) 36

Ans. (a)

$$\log_x^2 + \log_x^3 + \log_x^4 = 1$$
$$\log_x^{24} = 1$$
$$x = 24$$

End of Solution

Q.9 P, Q, R, S, and T have launched a new startup. Two of them are siblings. The office of the startup has just three rooms. All of them agree that the siblings should not share the same room.

If S and Q are single children, and the room allocations shown below are acceptable to all,

then, which one of the given options is the siblings?

(a) T and R

(b) T and Q

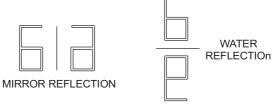
(c) P and S

(d) P and T

Ans. (d)

End of Solution

Examples of mirror and water reflections are shown in the figures below:



An object appears as the following image after first reflecting in a minor and then reflecting on water.







Detailed Solutions

Exam held on:

11-02-2024

Forenoon Session

The original object is (b) • • (d) • • (c) • (b) Ans. **End of Solution**



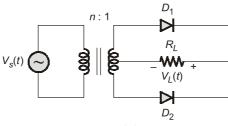
11-02-2024

Forenoon Session

SECTION - B

TECHNICAL

Q.1 In the circuit shown, the n: 1 step-down transformer and the diodes are ideal. The diodes have no voltage drop in forward biased condition. If the input voltage (in Volts) is $V_s(t) = 10 \sin \omega t$ and the average value of load voltage $V_l(t)$ (in Volts) is 2.5/ π , the value



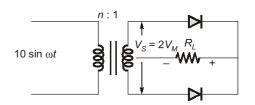
- (a) 8
- (c) 4

- (b) 12
- (d) 16

Ans. (c)

> $V_{DC} = \frac{2V_M}{\pi} = \frac{2.5}{\pi}$ Given, $V_M = \frac{2.5}{2}$ $2V_M = V_S = 2.5 \text{ V}$ *:*. $n: 1 = \frac{V_P}{V_s}: 1$ $=\frac{10}{2.5}:1$

> > n = 4



:.

End of Solution

Q.2 Let $\rho(x, y, z, t)$ and u(x, y, z, t) represent density and velocity, respectively, at a point (x, y, z) and time t. Assume $\frac{\partial \rho}{\partial t}$ is continuous. Let V be an arbitrary volume in space enclosed by the closed surface S and \hat{n} be the outward unit normal of S.

Which of the following equations is/are equivalent $\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho u) = 0$?

- (a) $\int_{V} \frac{\partial \rho}{\partial t} dv = \int_{V} \nabla \cdot (\rho u) dv$
- (b) $\int_{V} \frac{\partial \rho}{\partial t} dv = -\oint_{S} \rho u \cdot \hat{n} ds$
- (c) $\int_{V} \frac{\partial \rho}{\partial t} dv = \oint_{S} \rho u \cdot \hat{n} ds$ (d) $\int_{V} \frac{\partial \rho}{\partial t} dv = -\int_{V} \nabla \cdot (\rho u) dv$

Ans. (b, d)

End of Solution



ESE 2025

GATE + ESE 2025



- GATE Exclusive GATE + ESE
 - CS, EE, CE, ME, EC, IN

CE, EE, ME, EC

- **ϭ** GATE + SES-GS
- GATE + ESE + SES-GS

CS, EE, CE, ME, EC, IN

CE, EE, ME, EC

Note: Printed study materials will be sent to your door step.



www.madeeasyprime.com



- GATE Exclusive
 - CS, EE, CE, ME, EC, IN, CH
- GATE + ESE

CE, EE, ME, EC

GATE + SES-GS

CS, EE, CE, ME, EC, IN, CH

GATE + ESE + SES-GS

CE, EE, ME, EC



www.madeeasyprime.com

Delhi Centre : 44-A/1, Kalu Sarai, Near Hauz Khas Metro Station, New Delhi - 110016 Ph: 9021300500 MADE EASY Centres : Delhi | Bhopal | Hyderabad | Jaipur | Kolkata | Pune www.madeeasy.in



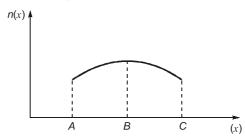
Detailed Solutions

Exam held on:

11-02-2024

Forenoon Session

Q.3 The free electron concentration profile n(x) in a doped semiconductor at equilibrium is shown in the figure, where the points A, B, and C mark three different positions. Which of the following statements is/are true?



- (a) For x between B and C, the electron diffusion current is directed from C to B.
- (b) For x between B and A. the electric field is directed from A to B.
- (c) For x between B and A, the electron drift current is directed from B to A.
- (d) For x between B and C, the electric field is directed from B to C.

Ans. (a, c, d)

End of Solution

Q.4 A machine has a 32-bit architecture with 1-word long instructions. It has 24 registers and supports an instruction set of size 40. Each instruction has five distinct fields, namely opcode, two source register identifiers, one destination register identifier, and an immediate value. Assuming that the immediate operand is an unsigned integer, its maximum value

Ans. (2047)

Given 32-bit architecture {1 word long instructions}

$$1 \text{ word} = 32\text{-bits}$$

Number of registers = 24, bits required \Rightarrow 2ⁿ = 24

$$n = \log_{2}(24)$$

$$\therefore$$
 $n = 5$ -bits

Number instructions = 40

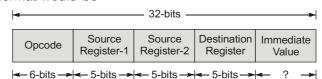
 \therefore Opcode bits would be $2^n = 40$

$$n = \log_2(40)$$

$$n = 6-\text{bits}$$

Each register field requires 5-bits.

Instruction format would be



 \therefore Immediate value bits = 32 - (6 + 5 + 5 + 5) = 32 - 21 = 11-bits

The range of unsigned values = 0 to $2^n - 1$

$$= 0 \text{ to } 2^{11} - 1 = 0 \text{ to } (2048 - 1) = 0 \text{ to } 2047$$

.. Maximum unsigned integer = 2047

End of Solution

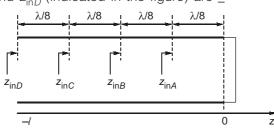
Page



11-02-2024

Forenoon Session

Q.5 Consider a lossless transmission line terminated with a short circuit as shown in the figure below. As one moves towards the generator from the load, the normalized impedances $z_{{\rm in}A^{\rm ,}}~z_{{\rm in}B^{\rm ,}}~z_{{\rm in}C}$ and $z_{{\rm in}D}$ (indicated in the figure) are _

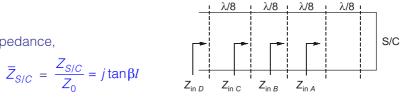


- (a) $z_{\text{in}A} = +0.4j \Omega$, $z_{\text{in}B} = \infty$, $z_{\text{in}C} = -0.4j \Omega$, $z_{\text{in}D} = 0$
- (b) $Z_{\text{in}A} = -1j \Omega$, $Z_{\text{in}B} = 0$, $Z_{\text{in}C} = +1j \Omega$, $Z_{\text{in}D} = \infty$
- (c) $z_{\text{in}A} = \infty$, $z_{\text{in}B} = +0.4j \Omega$, $z_{\text{in}C} = 0$, $z_{\text{in}D} = +0.4j \Omega$
- (d) $Z_{\text{in}A} = +1j\Omega$, $Z_{\text{in}B} = \infty$, $Z_{\text{in}C} = -1j\Omega$, $Z_{\text{in}D} = 0$

Ans.

 $Z_{s/c} = jZ_0 \tan \beta l$.

⇒ Normalized impedance,



$$\overline{Z}_{S/C} = \frac{Z_{S/C}}{Z_0} = j \tan \beta l$$

$$\overline{Z}_{\text{in }A} = j \tan \left(\frac{2\pi}{\lambda} \cdot \frac{\lambda}{8} \right) = j \tan (\pi/4) = j1 \Omega$$

$$\overline{Z}_{\text{in }B} = j \tan \left(\frac{2\pi}{\lambda} \cdot \frac{\lambda}{4} \right) = \infty$$

$$\overline{Z}_{\text{in }C} = j \tan \left(\frac{2\pi}{\lambda} \cdot \frac{3\lambda}{8} \right) = -j \, 1 \, \Omega$$

$$\overline{Z}_{\text{in }D} = j \tan \left(\frac{2\pi}{\lambda} \cdot \frac{\lambda}{2} \right) = 0$$

End of Solution

- Q.6 A causal and stable LTI system with impulse response h(t) produces an output y(t) for an input signal x(t). A signal x(0.5t) is applied to another causal and stable LTI system with impulse response h(0.5t). The resulting output is _____
 - (a) 2y(0.5t)

(b) 4y(0.5t)

(c) 0.25y(2t)

(d) 0.25y(0.25t)

Ans. (a)

$$y(t) = x(t) * h(t)$$

 $x(t) \leftrightarrow X(\omega)$

$$x(0.5t) \leftrightarrow 2 \times (2\omega)$$

$$h(0.5t) \leftrightarrow 2H(2\omega)$$

$$y(t) \leftrightarrow Y(\omega)$$

$$Y(\omega) \leftrightarrow X(\omega) \times H(\omega)$$

After scaling,

 $Y_1(\omega) = 2 \times (2\omega) \times 2 H(2\omega)$



Rank Improvement Course for GATE 2025

LIVE-ONLINE COURSE Streams:

CS, CE, EE, ME, EC

Commencing from 3 JUNE, 2024

Teaching Hours:

300 to 350 hours

Course Validity:

Till GATE 2025 Exam

- ✓ Comprehensive problem-solving sessions by India's top faculties.
- Focus on improving accuracy & speed.
- Newly develop workbooks (e-copy) in line with recent trends in GATE.

Download the App



Android



iOS



Detailed Solutions

Exam held on:

11-02-2024

Forenoon Session

= 4 X(2
$$\omega$$
) × H(2 ω)
After taking inverser Fourier transform
 $y_1(t) = 2y(0.5t)$

End of Solution

Q.7 For the Boolean function

$$F(A, B, C, D) = \Sigma m(0, 2, 5, 7, 8, 10, 12, 13, 14, 15)$$

the essential prime implicants are ____

(a) $BD, \overline{B}\overline{D}, AB$

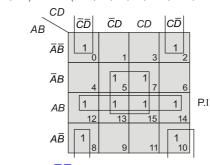
(b) $BD, \bar{B}\bar{D}$

(c) $AB, \overline{B}\overline{D}$

(d) BD, AB

Ans. (b)

 $f(A, B, C, D) = \Sigma m(0.2, 5, 7, 8, 10, 12, 13, 14, 15)$



BDΒĐ

E.P.I E.P.I

End of Solution

The general form of the complementary function of a differential equation is given by Q.8 $y(t) = (At + B)e^{-2t}$, where A and B are real constants determined by the initial condition. The corresponding differential equation is _

(a)
$$\frac{d^2y}{dt^2} + 5\frac{dy}{dt} + 6y = f(t)$$

(b)
$$\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 4y = f(t)$$

(c)
$$\frac{d^2y}{dt^2} + 4y = f(t)$$

(d)
$$\frac{d^2y}{dt^2} + 3\frac{dy}{dt} + 2y = f(t)$$

Ans. (b)

·: Given

Complementary function = $(At + B)e^{-2t} \approx (C_1 + C_2t)e^{-2t}$

i.e. roots of auxiliary equation are m = -2, -2

AE is (m + 2) (m + 2) = 0

$$m^2 + 4m + 4 = 0$$

Replace $m \to D$ we get,

$$(D^2 + 4D + 4)y = 0$$

i.e. the required different

$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 4y = f(t)$$

End of Solution

Corporate Office: 44-A/1, Kalu Sarai, New Delhi - 110016 | Ph: 9021300500

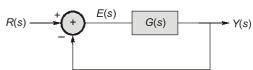
Page



11-02-2024

Forenoon Session

In the feedback control system shown in the figure below $G(s) = \frac{6}{s(s+1)(s+2)}$. Q.9



R(s), Y(s), and E(s) are the Laplace transforms of r(t), y(t), and e(t), respectively. If the input r(t) is a unit step function, then _____

(a) $\lim e(t) = 0$

(b) $\lim e(t)$ does not exist, e(t) is oscillatory

(c) $\lim_{t \to \infty} e(t) = \frac{1}{3}$

(d) $\lim_{t \to \infty} e(t) = \frac{1}{4}$

Ans. (b)

Given system is



$$G(s) = \frac{6}{s(s+1)(s+2)}$$

The characteristic equation,

$$1 + G(s) = 0$$

$$1 + \frac{6}{s(s+1)(s+2)} = 0$$

$$s(s + 1) (s + 2) + 6 = 0$$

 $s^3 + 3s^2 + 2s + 6 = 0$

Clearly, here the internal coefficient product is equal to external coefficient product i.e.,

$$3 \times 2 = 6 \times 1$$

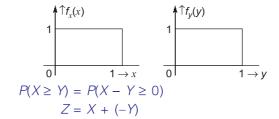
Hence, the given system is marginally stable system.

 \therefore e(t) not exist because system is oscillatory system.

End of Solution

Q.10 Suppose X and Y are independent and identically distributed random variables that are distributed uniformly in the interval [0, 1]. The probability that $X \ge Y$ is _____.

Ans. (0.5)

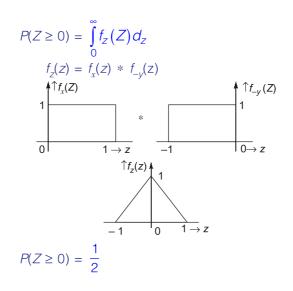


Let



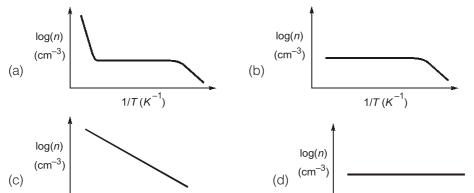
11-02-2024

Forenoon Session



End of Solution

For non-degenerately doped n-type silicon, which one of the following plots represents Q.11 the temperature (T) dependence of free electron concentration (n)?



Ans. (a)

End of Solution

 $1/T(K^{-1})$

In a number system of base r, the equation $x^2 - 12x + 37 = 0$ has x = 8 as one of Q.12 its solutions. The value of r is _____.

Ans. (11)

End of Solution

Q.13 An amplitude modulator has output (in Volts)

 $1/T(K^{-1})$

$$s(t) = A\cos(400\pi t) + B\cos(360\pi t) + B\cos(440\pi t)$$

The carrier power normalized to 1 Ω resistance is 50 Watts. The ratio of the total sideband power to the total power is 1/9. The value of B (in Volts. rounded off to two decimal places) is _____.



11-02-2024

Forenoon Session

Ans. (2.5)

$$P_{C} = \frac{A^{2}}{2} = 50$$

$$A = 10$$

$$\frac{P_{SB}}{P_{t}} = \frac{\mu^{2}}{2 + \mu^{2}} = \frac{1}{9}$$

$$\mu = \frac{1}{2}$$

$$B = \frac{A_{c}\mu}{2} = \frac{10}{2} \times \frac{1}{2} = 2.5$$

End of Solution

- A White Gaussian noise w(t) with zero mean and power spectral density $\frac{N_o}{2}$, when applied to a first-order RC low pass filter produces an output n(t). At a particular time $t = t_k$, the variance of the random variable $n(t_k)$ is _____.

(b) $\frac{2N_o}{RC}$

(c) $\frac{N_o}{BC}$

(d) $\frac{N_o}{2BC}$

Ans. (a)

White noise
$$W(t)$$
 RC $E[W(t)] = 0$ RC $E[W(t)] = 0$ $E[W$

$$E[n(t)] = E[W(t)] \cdot H(0)$$

 $E[n(t)] = 0$
 $E[n^2(t)] = \{E(n(t))^2 + \text{var}[n(t)]$
 $\text{var}[n(t)] = E[n^2(t)]$

at $t = t_k$

$$\begin{aligned} \text{var}[n(t)]_{t=t_{k}} &= E[n^{2}(t_{k})] = E[n(t_{k}) \cdot n(t_{k})] = R_{n}(0) \\ S_{n}(f) &= S_{M}(f) \cdot |H(f)|^{2} \\ &= \frac{N_{0}}{2} \cdot \frac{1}{1 + (\omega RC)^{2}} \\ R_{n}(\tau) &= \text{IFT}[S_{n}(f)] = \frac{N_{0}}{4RC} \cdot e^{\frac{-|\tau|}{RC}} \\ R_{n}(0) &= \frac{N_{0}}{4RC} \end{aligned}$$

End of Solution

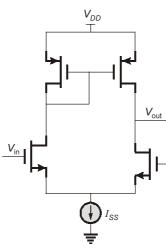


11-02-2024

Forenoon Session

Q.15 For the closed loop amplifier circuit shown below, the magnitude of open loop low frequency small signal voltage gain is 40. All the transistors are biased in saturation. The current source Iss is ideal. Neglect body effect. channel length modulation and intrinsic device capacitances. The closed loop low frequency small signal voltage gain

 $\frac{v_{\mathrm{out}}}{v_{\mathrm{in}}}$ (rounded off to three decimal places) is _____.



- (a) 0.976
- (c) 0.488

- (b) 1.000
- (d) 1.025

Ans. (a)

$$A_{OL} = 40$$

Given circuit is differential amplifier with current mirror active load.

$$V_f = V_{\text{out}}$$

$$\frac{V_f}{V_{out}} = \beta = 1$$

$$A_{CL} = \frac{A_{OL}}{1 + \beta A_{OL}} = \frac{40}{1 + 1 \times 40}$$

$$A_{Cl} = 0.976$$

End of Solution

Q.16 A digital communication system transmits through a noiseless bandlimited channel $[-W\ W]$. The received signal z(t) at the output of the receiving filter is given by

 $z(t) = \sum_{n} b[n] x(t - nT)$ where b[n] are the symbols and x(t) is the overall system response

to a single symbol. The received signal is sampled at t = mT. The Fourier transform of x(t) is X(t). The Nyquist condition that X(t) must satisfy for zero intersymbol interference at the receiver is _____.



Conventional Questions Practice Programmefor **ESE & State Exams**

Commencing from 4th March, 2024

OFFLINE & ONLINE COURSE

Streams: CE, EE, ME, EC

Teaching Hours: 300 to 350 hours

Course Duration:

100 days

Special offer valid till 4th March, 2024

Offline Course

Fee : ₹18,000 +GST ₹16,000 +GST

Ex. MADE EASY: ₹15,000 +GST ₹13,000 +GST

Live-Online Course

Fee: ₹14,000 +GST

- In-depth discussion on conventional questions.
- Helps to improve answer writing and presentation skills.
- Mains workbooks and Mains Test Series will be provided in this course.

Note: Offline classes will be conducted at Delhi Centre.

Delhi Centre: 44-A/1, Kalu Sarai, Near Hauz Khas Metro Station, New Delhi - 110016 | Ph: 9021300500 | MADE EASY Centres: Delhi | Bhopal | Hyderabad | Jaipur | Kolkata | Pune | www.madeeasy.in



(a)
$$\sum_{m=-\infty}^{\infty} X\left(f + \frac{m}{T}\right) = T$$

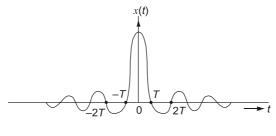
(b)
$$\sum_{m=-\infty}^{\infty} X\left(f + \frac{m}{T}\right) = \frac{1}{T}$$

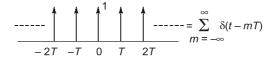
(c)
$$\sum_{m=-\infty}^{\infty} X(f+mT) = T$$

(d)
$$\sum_{m=-\infty}^{\infty} X(f+mT) = \frac{1}{T}$$

Ans. (a)

For zero ISI, x(t) should have zero crossings at $\pm T$, $\pm 2T$, $\pm 3T$





$$x(t)\sum_{m=-\infty}^{\infty}\delta(t-mT)=x(0)\delta(t)$$

$$\frac{1}{T} \sum_{m=-\infty}^{\infty} X \left(f - \frac{m}{T} \right) = x(0)$$

$$\sum_{m=-\infty}^{\infty} X \left(f - \frac{m}{T} \right) = x(0)T$$

(or)
$$\sum_{m=0}^{\infty} X\left(f + \frac{m}{T}\right) = x(0)T$$

End of Solution

Q.17 For a causal discrete-time LTI system with transfer function

$$H(z) = \frac{2z^2 + 3}{\left(z + \frac{1}{3}\right)\left(z - \frac{1}{3}\right)}$$

which of the following statements is/are true?

- (a) The system is stable.
- (b) The final value of the impulse response is 0.
- (c) The system is a minimum phase system.
- (d) The initial value of the impulse response is 2.

(a, b, d) Ans.

Given:
$$H(z) = \frac{2z^2 + 3}{\left(z + \frac{1}{3}\right)\left(z - \frac{1}{3}\right)}$$



System is non-minimum phase system. Since zero are lying outside the unit circle.

$$h(\infty) = \lim_{z \to 1} (z - 1) \frac{2z^2 + 3}{\left(z + \frac{1}{3}\right) \left(z - \frac{1}{3}\right)} = 0$$

$$h(0) = \lim_{z \to \infty} \frac{\left(2z^2 + 3\right)}{\left(z + \frac{1}{3}\right)\left(z - \frac{1}{3}\right)} = \lim_{z \to \infty} \frac{z^2 \left[2 + \frac{3}{z^2}\right]}{z^2 \left[1 + \frac{1}{3z}\right] \left[1 - \frac{1}{3z}\right]}$$

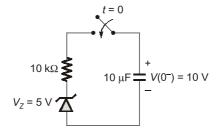
$$\lim_{z \to \infty} \frac{\left[2 + \frac{3}{z^2}\right]}{\left[1 + \frac{1}{3z}\right] \left[1 - \frac{1}{3z}\right]} = \frac{2}{1 \times 1} = 2$$

$$Z = -\frac{1}{3}, Z = \frac{1}{3}$$

$$|z| = \frac{1}{3} = 0.33$$

System is stable. Since |pole| < 1 i.e. pole are lying inside the unit circle.

Q.18 As shown in the circuit, the initial voltage across the capacitor is 10 V, with the switch being open. The switch is then closed at t = 0. The total energy dissipated in the ideal Zener diode ($V_z = 5$ V) after the switch is closed (in mJ, rounded off to three decimal places) is _____.



Ans. (0.125)

For t > 0: Capacitor starts discharging through 10 K resistor and zener diode.

$$V_c(t) = 10e^{-t/RC}, R \times C = 0.1 \text{ sec}$$

Zener diode remains on till V_C becomes 5 V.

$$5 = 10e^{-t_1/RC} \implies t_1 = RC \ln 2 = 0.0693 \text{ sec}$$

Current in the circuit is $i(t) = I_0 e^{-t/RC}$

where

$$I_0 = \frac{10-5}{10 \text{ k}} = 0.5 \text{ mA}$$

Total energy dissipated in zener diode is,

$$W = \int_{0}^{t_1} V_Z \times i(t) dt$$





11-02-2024

Forenoon Session

$$W = \int_{0}^{0.0693} 5 \times 0.5e^{-t/RC} \text{ mJ}$$
$$= 2.5[-0.1] \left[e^{-t/0.1} \right]_{0}^{0.0693}$$
$$W = 0.125 \text{ mJ}$$

End of Solution

- Q.19 Let \hat{i} and \hat{j} be the unit vectors along x and y axes, respectively and let A be a positive constant. Which one of the following statements is true for the vector fields $\vec{F}_1 = A(\hat{i}y + \hat{j}x)$ and $\vec{F}_2 = A(\hat{i}y \hat{j}x)$?
 - (a) Neither \vec{F}_1 nor \vec{F}_2 is an electrostatic field.
 - (b) Only \vec{F}_2 is an electrostatic field
 - (c) Only \vec{F}_1 is an electrostatic field.
 - (d) Both \vec{F}_1 and \vec{F}_2 are electrostatic fields.

Ans. (c)

For an electrostatic field, $\nabla \times \overline{F} = 0$

$$\overline{F}_{1} = A \left[y\hat{i} + x\hat{j} \right]$$

$$\Delta \times \overline{F}_{1} = A \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ y & x & 0 \end{vmatrix}$$

$$= A \left[0\hat{i} - 0\hat{j} + (1 - 1)\hat{k} \right]$$

$$= 0$$

$$\overline{F}_{2} = A \left[y\hat{i} - x\hat{j} \right]$$

Hence, \overline{F}_1 is electrostatic, \overline{F}_2 is not electrostatic.

End of Solution



- In the context of Bode magnitude plots, 40 dB/decade is the same as Q.20
 - (a) 12 dB/octave

(b) 10 dB/octave

(c) 6 dB/octave

(d) 20 dB/octave

Ans. (a)

> $20 \times ndB/decade = 6 \times n dB/octave$ 40dB/decade = 12 dB/octave

> > End of Solution

Let R and R^3 denote the set of real numbers and the three dimensional vector space Q.21 over it, respectively. The value of α for which the set of vectors

$$\{[2 -3 \alpha], [3 -1 3], [1 -5 7]\}$$

does not form a basis of R^3 is _____.

- Ans. (5)
 - : Given vectors form basis so there must be L.I and its condition is,

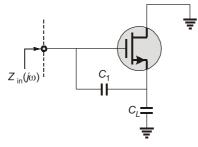
$$|A| \neq 0$$

$$\begin{vmatrix} 2 & 3 & 1 \\ -3 & -1 & -5 \\ a & 3 & 7 \end{vmatrix} \neq 0$$

$$2[-7 + 15] - 3[-21 + 5a] + 1[-9 + a] \neq 0$$

 $16 + 63 - 15a - 9 + a \neq 0$
 $-14a \neq -70$
 $\Rightarrow \qquad a \neq 5$

In the circuit below, assume that the long channel NMOS transistor is biased in saturation. Q.22 The small signal trans-conductance of the transistor is g_m Neglect body effect, channel length modulation and intrinsic device capacitances. The small signal input impedance $Z_{\rm in}(j\omega)$ is _____.



- (a) $\frac{-g_m}{C_1 C_L \omega^2} + \frac{1}{j\omega C_1} + \frac{1}{j\omega C_L}$ (b) $\frac{-g_m}{C_1 C_L \omega^2} + \frac{1}{j\omega C_1 + j\omega C_L}$

(c) $\frac{1}{j\omega C_1} + \frac{1}{j\omega C_1}$

(d) $\frac{g_m}{C_1 C_I \omega^2} + \frac{1}{j \omega C_1} + \frac{1}{j \omega C_I}$

Page



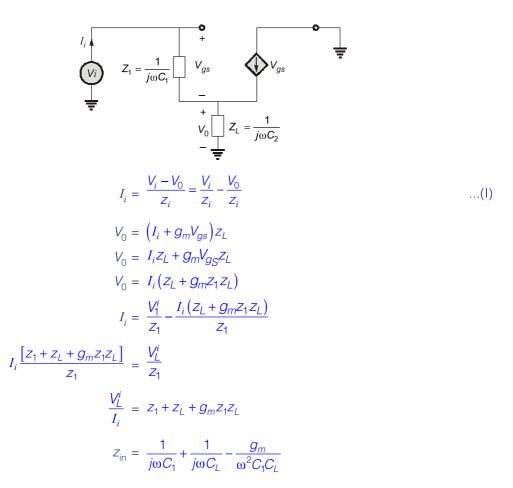
Detailed Solutions

Exam held on:

11-02-2024

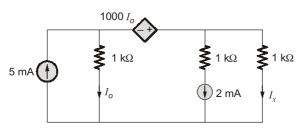
Forenoon Session





End of Solution

Q.23 In the given circuit, the current I_r (in mA) is ____.



Ans. (2)

 V_1 and V_2 are super node. KCL at V_1 and V_2 . $V_1 = \frac{V_1}{10^3} + \frac{V_2}{1 \times 10^3} + 2 \times 10^{-3} = 5 \times 10^{-3} \dots (i)$ $I_0 = \frac{V_1}{10^3}$ $I_0 = \frac{V_1}{10^3} = 10^3 \times \frac{V_1}{10^3} = V_1$



$$V_2 = 2V_1$$

 $V_1 = \frac{V_2}{2}$...(ii)

Put in equation (i)

$$\frac{1}{2}V_2 + V_2 = 3$$

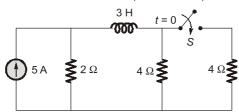
$$V_2 = 2 \text{ V}$$

$$I_x = \frac{V_2}{10^3} = 2 \text{ mA}$$

$$I_x = 2 \text{ mA}$$

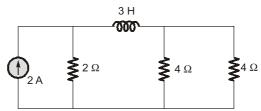
End of Solution

In the circuit given below, the switch S was kept open for a sufficiently long time and Q.24 is closed at time t = 0. The time constant (in seconds) of the circuit for t > 0 is _____.

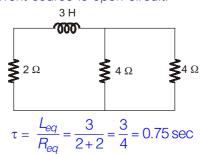


Ans. (0.75)

After the switch closed



For time constant, current source is open circuit.



٠.

Q.25 A source transmits symbols from an alphabet of size 16. The value of maximum achievable entropy (in bits) is _____.

(4)Ans.

$$H_{\text{max}} = \log_2 16 = 4$$

End of Solution



SSC-JE RRB-JE State-JE/AE

FOUNDATION COURSES TECHNICAL & NON-TECHNICAL

Streams : CE, ME, EE | MODE : ONLINE

- Classes by experienced and renowned faculties.
- Well-researched study material.
- Interaction facility for doubt removal.

RECORDED CLASSES Admissions open



www.madeeasyprime.com

Download MADE EASY PRIME app





Android

iOS

Low Cost EMI Facility Available



11-02-2024

Forenoon Session

Perfect

- Q.26 A uniform plane wave with electric field $\vec{E}(x) = A_y \hat{a}_y e^{-j\frac{2\pi x}{3}}$ V/m is travelling in the air (relative permittivity, $\epsilon_r = 1$ and relative permeability, $\mu_r = 1$) in the +x direction (A_y is a positive constant, \hat{a}_y is the unit vector along the y axis). It is incident normally on an ideal electric conductor (conductivity, $\sigma = \infty$) at x = 0. The position of the first null of the total magnetic field in the air (measured from x = 0, in metres) is ______.
 - (a) -6

(b) $-\frac{3}{2}$

(c) -3

(d) $-\frac{3}{4}$

air

Ans. (d)

At perfect conductor,

$$\Gamma = -1$$

 \Rightarrow

$$\Gamma = 1 \boxed{\pi}$$

As we know that H_{\min} occurs at E_{\max} . Hence, $E_{\max} = E_0[1 + |\Gamma|]$



So, $2\beta x_{\text{max}} = 2n\pi + \theta_{\Gamma}$

$$\Rightarrow \frac{4\pi}{\lambda}x_{\text{max}} = 2n\pi + \pi$$

$$\Rightarrow x_{\text{max}} = (2n+1)\frac{\lambda}{4}; \quad n = 0, 1, 2, 3...$$

So, for 1^{st} value of x for H-field to be zero is

$$x_{\text{max}} = \frac{\lambda}{4}$$
 [at $n = 0$]

Now, from the equation given,

$$\beta = \frac{2\pi}{3}$$

$$\Rightarrow$$

$$\frac{2\pi}{\lambda} = \frac{2\pi}{3}$$

$$\Rightarrow$$

$$\lambda = 3$$

Hence,

$$x_{\text{max}} = \frac{3}{4}$$

If the reference is not at interference then $x = -\frac{3}{4}$.

End of Solution



11-02-2024

Forenoon Session

- The information bit sequence (1 1 1 0 1 0 1 0 1) is to be transmitted by encoding with Q.27 Cyclic Redundancy Check 4 (CRC-4) code, for which the generator polynomial is $C(x) = x^4 + x + 1$. The encoded sequence of bits is _
 - (a) {1 1 1 0 1 0 1 0 1 1 1 0 1}
- (b) {1 1 1 0 1 0 1 0 1 1 1 1 0}
- (c) {1 1 1 0 1 0 1 0 1 0 1 0 0}
- (d) {1 1 1 0 1 0 1 0 1 1 1 0 0}

Ans. (d)

Given information bit sequence $\rightarrow d = 111010101$

Generator polymial $\rightarrow C(x) = x^4 + x + 1$

C = 10011

Generator polynomial having 5 bits, so append 5 - 1 = 4 bits to information sequence.

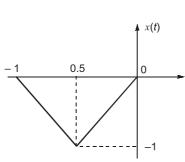
$$d = 1 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 0$$

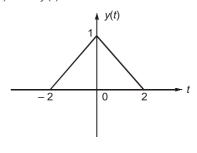
10011)1110101010000 (11 10011 Ø111001010000 10011 Ø11111010000 10011 Ø1100010000 10011 Ø101110000 10011 ØØ1000000 10011 ØØØ1100

Encoded sequence = 1 1 1 0 1 0 1 0 1 1 1 0 0

End of Solution

Consider two continuous time signals x(t) and y(t) as shown below





If X(t) denotes the Fourier transform of x(t), then the Fourier transform of y(t) is _

(a) $-\frac{1}{4}X(f/4)e^{-j\pi f}$

(b) $-4X(4f)e^{-j\pi f}$

(c) $-4X(4f)e^{-j4\pi f}$

(d) $-\frac{1}{4}X(f/4)e^{-j4\pi f}$

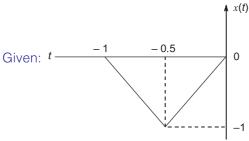
Page



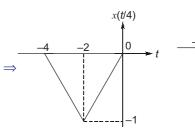
11-02-2024

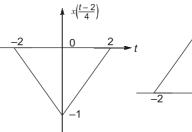
Forenoon Session

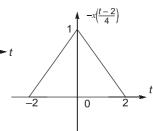
Ans. (c)



Length of x(t) is 1 and length of y(t) is 4.







$$y(t) = -x\left(\frac{t-2}{4}\right)$$

$$y(t) = -x\left(\frac{t}{4} - \frac{2}{4}\right) = -x\left(\frac{t}{4} - \frac{1}{2}\right)$$

On taking Fourier transform, we get

$$x(t) \leftrightarrow X(t)$$

$$x\left(\frac{t}{4} - \frac{1}{2}\right) \leftrightarrow 4X(4f)e^{-j4\pi f}$$

$$-x\left(\frac{t}{4} - \frac{1}{2}\right) \longleftrightarrow -4X(4f)e^{-j4\pi f}$$

End of Solution

Q.29 Consider a system S represented in state space as

$$\frac{dx}{dt} = \begin{bmatrix} 0 & -2 \\ 1 & -3 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} r, y = \begin{bmatrix} 2 & -5 \end{bmatrix} x$$

Which of the state space representations given below has/have the same transfer function as that of S?

(a)
$$\frac{dx}{dt} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} r, y = \begin{bmatrix} 0 & 2 \end{bmatrix} x$$
 (b)
$$\frac{dx}{dt} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 1 \\ 0 \end{bmatrix} r, y = \begin{bmatrix} 1 & 2 \end{bmatrix} x$$

(c)
$$\frac{dx}{dt} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} x + \begin{bmatrix} -1 \\ 3 \end{bmatrix} r, y = \begin{bmatrix} 1 & 1 \end{bmatrix} x$$
 (d)
$$\frac{dx}{dt} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \end{bmatrix} r, y = \begin{bmatrix} 1 & 2 \end{bmatrix} x$$

Ans. (b, c)

From given state model, (observable form)

$$TF = C[(sI - A)^{-1}B] + D$$
 ...(B)

Page



11-02-2024

Forenoon Session

$$= \frac{(2s+1)}{s^2 + 3s + 2}$$

From this controllable form can be written as

$$X^{0} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

$$Y = [1 \ 2] X + [0]u$$

TF = $\frac{2s+1}{s^2+3s+2} = \frac{-1}{s+1} + \frac{3}{s+2}$ Another possibility,

$$X^{0} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} X + \begin{bmatrix} -1 \\ 3 \end{bmatrix} V$$

Diagonal form of state mode.

End of Solution

- Q.30 A full scale sinusoidal signal is applied to a 10-bit ADC. The fundamental signal component in the ADC output has a normalized power of 1 W, and the total noise and distortion normalized power is 10 μ W. The effective number of bits (rounded off to the nearest integer) of the ADC is ___
 - (a) 10

(b) 9

(c) 8

(d) 7

(c) Ans.

$$\frac{S}{N_q} = \frac{1}{10 \times 10^{-6}}$$

$$\frac{S}{N_q} = 10^5$$

$$\left(\frac{S}{N_q}\right)_{dB} = 10 \log_{10} 10^5$$
$$= 50 \text{ dB}$$

$$1.76 + 6.02n = 50$$

$$n = 8.01$$

rounded off to nearest integer $\rightarrow n \simeq 8$

End of Solution

For the two port network shown below, the value of the Y_{21} parameter (in Siemens) is Q.31

Corporate Office: 44-A/1, Kalu Sarai, New Delhi - 110016 | **Ph:** 9021300500

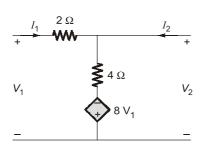


11-02-2024

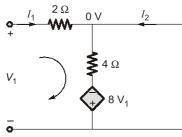
Forenoon Session

Ans. (1.5)

Given two-port network,



$$Y_{21} = \frac{I_2}{V_1} \Big|_{V_2 = 0}$$



by applying KVL in the loop,

$$V_1 - 2I_1 - 4(I_1 + I_2) + 8V_1 = 0$$

 $9V_1 - 6I_1 - 4I_2 = 0$

but

$$I_1 = \frac{V_1 - 0}{2} \Rightarrow \frac{V_1}{2} = I_1$$

$$\therefore 9V_1 - 6\left(\frac{V_1}{2}\right) - 4I_2 = 0$$

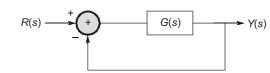
$$6V_1 = 4I_2$$

$$\frac{I_2}{V_1} = \frac{6}{4} = \frac{3}{2} = 1.5 \text{ S}$$

End of Solution

Q.32 Consider a unity negative feedback control system with forward path gain

$$G(s) = \frac{K}{(s+1)(s+2)(s+3)}$$
 as shown.



The impulse response of the closed-loop system decays faster than e^{-t} if ______

(a) $-4 \le K \le -1$

(b) $1 \le K \le 5$

(c) $7 \le K \le 21$

(d) $-24 \le K \le -6$



Forenoon Session

Ans. (b)

Given,
$$G(s) = \frac{K}{(S+1)(S+2)(S+3)}$$

Impulse response of system is

$$Y(S) = \frac{K}{(S+1)(S+2)(S+3)+K}$$

Given: At impulse response of closed loop system decay faster than e^{-t} Hence, put s = s - 1,

.. The new characteristic equation is,

$$(s-1+1)(s-1+2)(s-1+3)+K=0$$

 $s(s+1)(s+2)+K=0$

$$s^3 + 3s^2 + 2s + K = 0$$

By RH criterion,

$$\begin{vmatrix}
s^3 & 1 & 2 \\
s^2 & 3 & K \\
s^1 & \frac{6-K}{3} & \\
s^0 & K
\end{vmatrix}$$

$$\therefore K > 0; \qquad \frac{6 - K}{3} > 0 \implies K < 6$$

$$\therefore 0 < K < 6$$

Hence, option (b) satisfies above range of K.

End of Solution

Q.33 Consider the Earth to be a perfect sphere of radius R. Then the surface area of the region, enclosed by the 60°N latitude circle, that contains the north pole in its interior is _____

(a)
$$(2-\sqrt{3})\pi R^2$$

(b)
$$\frac{(\sqrt{2}-1)\pi R^2}{2}$$

(c)
$$\frac{(2+\sqrt{3})\pi R^2}{8\sqrt{2}}$$

(d)
$$\frac{2\pi R^2}{3}$$

Ans. (a)

From the figure

Earth's North pole = 90°

Earth's equator = 0°

In spherical co-ordinate system

Earth's North pole, $\theta = 0^{\circ}$

Earth's equator, $\theta = 90^{\circ}$

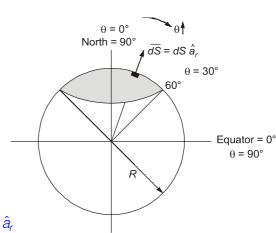
The area of the shaded portion,

$$\overline{dS} = dS \hat{a}_r$$

Hence, in spherical coordinate system

$$\Rightarrow$$

$$\overline{dS} = r^2 \sin\theta d\theta d\phi \hat{a}_r$$





POSTAL BOOK **PACKAGES**

PACKAGES

- ESE • GATE
- PSUsCSE
- SSC-JE
 RRB-JE
- STATE SERVICES EXAMS

Streams:

CE, CS, EE, ME, EC, IN, PI, CH

逆 For online purchase, visit :

www.madeeasypublications.org

MADE EASY Delhi Centre: 44-A/1, Kalu Sarai, Near Hauz Khas Metro Station, New Delhi - 110016 | Ph: 9021300500



$$S = \int dS = \int r^2 \sin\theta d\theta d\phi$$

$$= r^2 \int_{\theta=0^{\circ}}^{30^{\circ}} \sin\theta d\theta \int_{\phi=0}^{2\pi} d\phi \quad \text{at } r = R$$

$$= R^2 - \left[-\cos\theta \Big|_0^{30^{\circ}} \right] \cdot \phi \Big|_0^{2\pi}$$

$$= R^2 \left\{ -\left[\cos 30^{\circ} - \cos 0^{\circ} \right] \right\} \cdot 2\pi$$

$$= R^2 \left\{ -\left[\frac{\sqrt{3}}{2} - 1 \right] \right\} \cdot 2\pi = R^2 \cdot \frac{2 - \sqrt{3}}{2} \cdot 2\pi$$

$$= (2 - \sqrt{3})\pi R^2$$

End of Solution

- The photocurrent of a PN junction diode solar cell is 1 mA. The voltage corresponding Q.34 to its maximum power point is 0.3 V. If the thermal voltage is 30 mV, the reverse saturation current of the diode (in nA, rounded off to two decimal places) is ___
- Ans.

Note: In this question voltage corresponds to max. power, V_m is given $V_m = 0.3 \text{ Volt}$ $(V_{OC}$ is not given be careful)

$$I_0 = \frac{I_L}{\left(1 + \frac{V_m}{V_T}\right)} e^{V_m/V_T} - 1 = \frac{1 \text{ mA}}{\left(1 + \frac{0.3}{0.03}\right)} e^{0.3/0.03} - 1$$
$$= 4.127 \text{ nA} \simeq 4.13 \text{ nA}$$

End of Solution

Q.35 A continuous time signal $x(t) = 2 \cos (8\pi t + \pi/3)$ is sampled at a rate of 15 Hz. The sampled signal $x_s(t)$ when passed through an LTI system with impulse response

$$h(t) = \left(\frac{\sin 2\pi t}{\pi t}\right) \cos(38\pi t - \pi/2)$$

produces an output $x_0(t)$. The expression for $x_0(t)$ is _

- (a) $15 \sin(38\pi t + \pi/3)$
- (b) $15 \cos(38\pi t \pi/6)$
- (c) $15 \sin(38\pi t + \pi/6)$
- (d) $15 \sin(38\pi t \pi/3)$

Ans. (b)

$$x(t) = 2\cos\left(8\pi t + \frac{\pi}{3}\right), \quad \omega_o = 8\pi$$

$$f_s = 15 \text{ Hz}$$

$$x(t) \xrightarrow{\text{sample}} x_s(t) \xrightarrow{h(t)} x_o(t)$$

$$\Rightarrow h(t) = \frac{\sin 2\pi t}{\pi t} \cos\left(38\pi t - \frac{\pi}{2}\right)$$

Corporate Office: 44-A/1, Kalu Sarai, New Delhi - 110016 | Ph: 9021300500

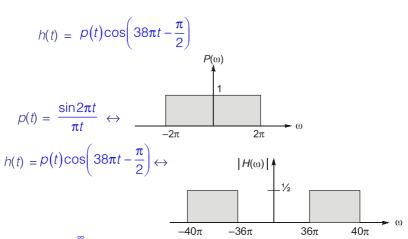
Page



11-02-2024

Forenoon Session

Let
$$p(t) = \frac{\sin 2\pi t}{\pi t}$$



 $X_s(\omega) = f_s \sum_{n=1}^{\infty} X(\omega - n\omega_s)$ After sampling:

Frequency components present in sampler output $n\omega_s \pm \omega_o$

 ω_o , $\omega_s + \pm \omega_o$, $2\omega_s \pm \omega_o$,

 8π , $30\pi \pm 8\pi$, $60\pi \pm 8\pi$, ...

 8π , 22π , 38π , 52p, 68π , ... (rad/sec)

System will pass ' 38π ' component of input.

$$x_o(t) = 2 \times \frac{f_s}{2} \cos \left[38\pi t + \frac{\pi}{3} - \frac{\pi}{2} \right] = 15 \cos \left(38\pi t - \frac{\pi}{6} \right)$$

End of Solution

Q.36 A 4-bit priority encoder has inputs D_3 , D_2 , D_1 and D_0 in descending order of priority. The two-bit output AB is generated as 00, 01, 10, and 11 corresponding to inputs D_3 , D_2 , D_1 and D_0 , respectively. The Boolean expression of the output bit B is ___

(a)
$$\overline{D_3}D_2 + \overline{D_3}\overline{D_1}$$

(b)
$$\overline{D_3}\overline{D_2}$$

(c)
$$\overline{D_3}\overline{D_1}$$

(d)
$$D_3 \overline{D_2} + \overline{D_3} D_1$$

Ans. (*)

Given 4-bit priority encoder has inputs D_3 , D_2 , D_1 and D_0 in descending order of priority.

D_3	D_2	D_1	D_0	Α	
0	0	0		0	0
0	0	1	X	0	1
0	1	X	X		
1	Χ	Χ	Χ	1	1

The Boolean expression of the output bit $B = \bar{D}_3 \bar{D}_2 D_1 + D_3$

Therefore, $B = D_3 + \overline{D}_2 D_1$

End of Solution



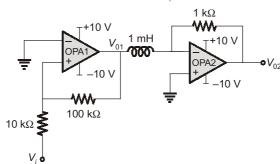
Detailed Solutions

Exam held on:

11-02-2024

Forenoon Session

The opamps in the circuit shown are ideal, but have saturation voltages of ±10 V. Q.37



Assume that the initial inductor current is 0 A. The input voltage (V_i) is a triangular signal with peak voltages of ±2 V and time period of 8 µs. Which one of the following statements is true?

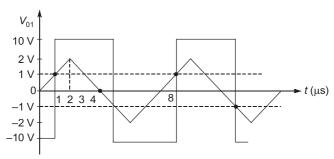
- (a) V_{01} is delayed by 1 μs relative to V_{i} , and V_{02} is a trapezoidal waveform.
- (b) V_{01} is delayed by 2 μs relative to V_{i} , and V_{02} is a triangular waveform.
- (c) V_{01} is not delayed relative to V_{i^*} and V_{02} is a trapezoidal waveform.
- (d) V_{01} is not delayed relative to V_{i} , and V_{02} is a triangular waveform.

Ans.

Opamp A_1 is non-inverting type Schmitt Trigger.

$$V_{UT} = \frac{R_1}{R_2} \times V_{Sat} = \frac{10}{100} \times 10 \text{ V} = 1 \text{ V}$$

$$V_{LT} = -\frac{R_1}{R_2} \times V_{\text{sat}} = \frac{-10}{100} \times 10 = -1 \text{ V}$$



 V_{O1} is square wave. It is delayed by 1 $\mu\mathrm{s}$ wrt input $V_{i^{*}}$ Opamp A_2 is integrator.

 V_{02} is getting saturated in less than half time period. Hence V_{02} is a combination of ramp and constant portion. Thus V_{02} resembles trapezoidal wave

End of Solution

Let z be a complex variable. If $f(z) = \frac{\sin(\pi z)}{z^2(z-2)}$ and C is the circle in the complex plane Q.38

with |z| = 3 then $\oint f(z)dz$ is _____



(a)
$$-\pi^2 j$$

(b)
$$j\pi\left(\frac{1}{2}-\pi\right)$$

(c)
$$j\pi\left(\frac{1}{2}+\pi\right)$$

(d)
$$\pi^2 j$$

Ans. (a)

Poles of
$$f(z)$$
 are $z = 2$ and 0 Double pole

$$R_1$$
 = Residue of $f(z)$ = at $(z = 2)$

$$= \lim_{z\to 2} (z-2)f(z) = \lim_{z\to 2} \left(\frac{\sin \pi z}{z^2}\right) = 0$$

$$R_2$$
 = Residue of $f(z)$ (at($z = 0, m = 2$)

$$R_2 = \frac{1}{|2-1|} \left[\frac{d^{2-1}}{dz^{2-1}} (z-0)^2 f(z) \right]_{z=0}$$

$$\left[\frac{d}{dz} \left[\frac{\sin \pi z}{z - 2}\right]\right]_{z = 0} = \left[\frac{(z - 2)\cos \pi z(\pi) - \sin \pi z}{(z - 2)^2}\right]_{z = 0}$$
$$= \frac{(0 - 2)\cos(2\pi) \cdot \pi - \sin 0}{(0 - 2)^2} = \frac{-2\pi}{4} = \frac{-\pi}{2}$$

By C - R.T,

$$I = \oint_{c} f(z)dz = 2\pi j (R_1 + R_2)$$
$$= 2\pi i \left(0 - \frac{\pi}{2}\right) = -\pi^2 j$$

End of Solution

Q.39 Consider a MOS capacitor made with p-type silicon. It has an oxide thickness of 100 nm, a fixed positive oxide charge of 10⁻⁸ C/cm² at the oxide-silicon interface, and a metal work function of 4.6 eV. Assume that the relative permittivity of the oxide is 4 and the absolute permittivity of free space is 8.85×10^{-14} F/cm. If the flatband voltage is 0 V, the work function of the p-type silicon (in eV, rounded off to two decimal places) is _____.

Ans. (4.32)

$$C_{ox} = \frac{\varepsilon_{Ox}}{t_{ox}} = \frac{4 \times 8.85 \times 10^{-14}}{100 \times 10^{-9} \times 100}$$

$$= 4 \times 8.85 \times 10^{-14} \times 10^{5} = 35.4 \times 10^{-9} \text{ F/cm}^{2}$$

$$V_{FB} = \frac{Q_{ox}}{C_{ox}} + \phi_{ms}$$

$$0 = \frac{Q_{ox}}{C_{ox}} + \phi_{ms}$$



$$\frac{Q_{ox}}{C_{ox}} = \frac{10^{-8}}{35.4 \times 10^{-9}} = \frac{10}{35.4} \text{ volt}$$

 $Q_{ox} \rightarrow \text{Positive}$

$$\therefore \quad \frac{Q_{ox}}{C_{ox}} \to \text{Negative}$$

$$0 = \frac{-10}{35.4} + \phi_{ms}$$

$$\phi_{ms} = \frac{10}{35.4}$$

$$\phi_{m} - \phi_{s} = \frac{10}{35.4}$$

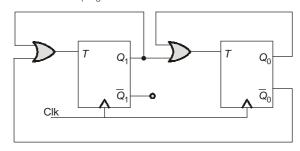
$$\phi_{s} = \phi_{m} - \frac{10}{35.4} = 4.6 - \frac{10}{35.4} = 4.317 \text{ volt}$$

$$q\phi_{s} = 4.317 \approx 4.32 \text{ eV}$$

Work function energy of semiconductor.

End of Solution

Q.40 The sequence of states (Q_1Q_0) of the given synchronous sequential circuit is _



- (a) $11 \to 00 \to 10 \to 01 \to 00$ (b) $00 \to 01 \to 10 \to 00$ (c) $01 \to 10 \to 11 \to 00 \to 01$ (d) $00 \to 10 \to 11 \to 00$

Ans. (a)

 $00 \rightarrow 10 \rightarrow 01 \rightarrow 00$

End of Solution

- Q.41 The radian frequency value(s) for which the discrete time sinusoidal signal x[n] = A $cos(\Omega n + \pi/3)$ has a period of 40 is/are ____
 - (a) 0.15π

(b) 0.3π

(c) 0.45π

(d) 0.225π



11-02-2024

Forenoon Session

Ans. (a, b, c)

$$x[n] = A\cos\left[\Omega n + \frac{\pi}{3}\right]$$

$$N = 40$$

$$\Omega = ?$$

$$\frac{\Omega}{2\pi} = \frac{m}{N}$$

$$\frac{\Omega}{2\pi} = \frac{m}{40}$$

$$\Omega = m \cdot \frac{2\pi}{40} = \pi \cdot m(0.05)$$

$$\Omega = 0.05\pi$$
 $m = 1$
 $\Omega = 0.05\pi$
 $m = 2$
 $\Omega = 0.10\pi$
 $m = 3$
 $\Omega = 0.15\pi$
 $m = 4$
 $\Omega = 0.20\pi$
 $m = 5$
 $\Omega = 0.25\pi$
 $m = 6$
 $\Omega = 0.30\pi$
 $m = 7$
 $\Omega = 0.35\pi$
 $m = 8$
 $\Omega = 0.40\pi$
 $\Omega = 0.45\pi$

End of Solution

- Q.42 Which of the following statements is/are true for a BJT with respect to its DC current gain β ?
 - (a) Under high-level injection condition in forward active mode, β will decrease with increase in the magnitude of collector current.
 - (b) β will be lower when the BJT is in saturation region compared to when it is in active region.
 - (c) Under low-level injection condition in forward active mode, where the current at the emitter-base junction is dominated by recombination-generation process, β will decrease with increase in the magnitude of collector current.
 - (d) A higher value of β will lead To a lower value of the collector-to-emitter breakdown voltage.

Ans. (a, b, d)

End of Solution

Q.43 An NMOS transistor operating in the linear region has I_{DS} of 5 μ A at V_{DS} of 0.1 V. Keeping V_{GS} constant, the V_{DS} is increased to 1.5 V.

Given that $\mu_n C_{ox} \frac{W}{L} = 50 \,\mu\text{A/V}^2$, the transconductance at the new operating point (in $\mu\text{A/V}$, rounded off to two decimal places) is _____.

MADE EASY Group

LAUNCHES

NEET IIT-JEE

MENIIT is a new addition to the MADE EASY Group, which provides coaching for the prestigious NEET and IIT-JEE. As a part of the esteemed MADE EASY Group, MENIIT upholds the same values of academic excellence, integrity and student centricity.











Detailed Solutions

Exam held on:

11-02-2024

Forenoon Session

Ans. (52.5)

For linear region of MOS,

$$I_D = \mu_n C_{ox} \left(\frac{W}{L}\right) \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

$$5 \times 10^{-6} = 50 \times 10^{-6} \left[(V_{GS} - V_T) 0.1 - \frac{1}{2} (0.1)^2 \right]$$

$$\frac{1}{10} = (V_{GS} - V_T) 0.1 - \frac{1}{2} \times 0.1^2$$

$$0.1 + 0.5(0.1)^2 = (V_{GS} - V_T) 0.1$$

$$1 + 0.5(0.1) = (V_{GS} - V_T)$$

$$1.05 \text{ volt} = V_{GS} - V_T$$
Now: $V_{GS} \rightarrow \text{fix}$

$$V_{DS} = 1.5$$

$$V_{DS} > V_{GS} - V_T \implies \text{MOS is in saturation}$$

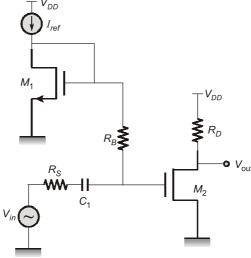
$$g_{m \text{ (sat)}} = \mu_n C_{ox} \left(\frac{W}{L}\right) (V_{GS} - V_T)$$

$$= 50 \times 10^{-6} \times 1.05$$

End of Solution

Q.44 In the circuit shown below, the transistors M_1 and M_2 are biased in saturation. Their small signal transconductances are g_{m1} and g_{m2} respectively. Neglect body effect, channel length modulation and intrinsic device capacitances.

 $= 52.5 \times 10^{-6} \text{ A/V} = 52.5 \text{ } \mu\text{A/V}$



Assuming that capacitor C_1 is a short circuit for AC analysis, the exact magnitude of small signal voltage gain $\left| \frac{V_{out}}{V_{in}} \right|$ is _____.



11-02-2024

Forenoon Session

(a)
$$\frac{g_{m2}R_D(\frac{1}{g_{m1}})}{\frac{1}{g_{m1}} + R_s}$$

(b)
$$g_{m2}R_D$$

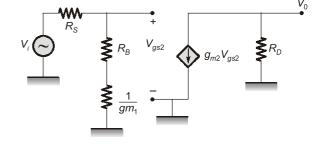
(c)
$$\frac{g_{m2}R_D \left(R_B + \frac{1}{g_{m1}}\right)}{R_B + \frac{1}{g_{m1}} + R_s}$$

(d)
$$\frac{g_{m2}R_{D}\left(R_{B} + \frac{1}{g_{m1}} + R_{s}\right)}{R_{B} + \frac{1}{g_{m1}}}$$

Ans. (c)

$$V_{0} = -g_{m2}V_{gs}R_{D}$$

$$V_{gs} = V_{L}^{i} \times \frac{R_{B} + \frac{1}{g_{m1}}}{R_{S} + R_{B} + \frac{1}{g_{m1}}}$$

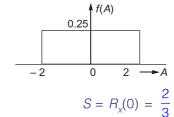


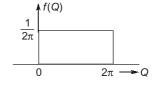
 $\left| \frac{V_0}{V_{in}} \right| = \frac{g_{m2} R_D \left(R_B + \frac{1}{g_{m1}} \right)}{R_S + R_B + \frac{1}{g_{m1}}}$

End of Solution

Q.45 Let $X(t) = A \cos(2\pi f_0 t + \theta)$ be a random process, where amplitude A and phase θ are independent of each other, and are uniformly distributed in the intervals [-2,2] and $[0,2\pi]$, respectively. X(t) is fed to an 8-bit uniform mid-rise type quantizer. Given that the autocorrelation of X(t) is $R_x(\tau) = \frac{2}{3}\cos(2\pi f_0 \tau)$, the signal to quantization noise ratio (in dB, rounded off to two decimal places) at the output of the quantizer is ______.

Ans. (45.15)





$$N_q = \frac{\Delta^2}{12}$$

$$\Delta = \frac{2 - (-2)}{2^8} = \frac{4}{2^8}$$



$$N_q = \frac{4^2}{\frac{2^{16}}{12}} = \frac{2^4}{12 \times 2^{16}} = \frac{1}{12 \times 2^{12}}$$

$$\frac{S}{N_q} = \frac{2}{3} \times \frac{12 \times 2^{12}}{1} = 32,768$$

$$\left(\frac{S}{N_q}\right)_{dB}$$
 = 10 log32768 = 45.15 dB

End of Solution

Q.46 The relationship between any N-length sequence x[n] and its corresponding N-point discrete Fourier transform X[k] is defined as

$$X[k] = F\{x[n]\}.$$

Another sequence y[n] is formed as below

$$y[n] = F\{F\{F\{x[n]\}\}\}\}$$
.

For the sequence $x[n] = \{1, 2, 1, 3\}$, the value of Y[0] is _____.

Ans. (112)

$$y[n] = N^{2}x[n]$$

$$y[n] = N^{2}x[n]$$

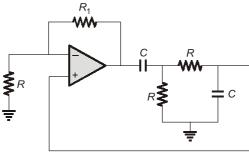
$$Y[k]|_{K=0} = \sum_{n=0}^{3} y[n] = \sum_{n=0}^{3} N^{2}x[n]$$

$$= N^{2}[x[0] + x[1] + x[2] + x[3]]$$

$$= (4)^{2}[1 + 2 + 1 + 3] = 16 \times 7 = 112$$

End of Solution

In the circuit below, the opamp is ideal.



If the circuit is to show sustained oscillations, the respective values of R_1 and the corresponding frequency of oscillation are _____

- (a) 2R and $1/(2\pi\sqrt{6}RC)$
- (b) 29R and $1/(2\pi RC)$
- (c) 2R and $1/(2\pi RC)$
- (d) $29R \text{ and } 1/(2\pi\sqrt{6}RC)$



11-02-2024

Forenoon Session

Ans. (c)

For given circuit, frequency of oscillations is $f_o = \frac{1}{2\pi RC}$.

For sustained oscillations, minimum gain should be 3.

$$1 + \frac{R_1}{R} = 3$$

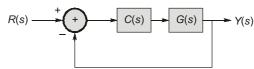
$$R_1 = 2R$$

Answer is option (c)

End of Solution

Q.48 A satellite attitude control system, as shown below, has a plant with transfer function

 $G(s) = \frac{1}{s^2}$ cascaded with a compensator $C(s) = \frac{K(s + \alpha)}{s + 4}$, where K and α are positive real constants.



In order for the closed-loop system to have poles at $-1 \pm j\sqrt{3}$, the value of α must be

(a) 0

(b) 3

(c) 1

(d) 2

Ans. (c)

$$G(S)C(s) = \frac{1}{S^2} \frac{k(S+\alpha)}{(S+4)}$$

Characteristic equation is

$$S^3 + 4S^2 + kS + \alpha = 0$$
 ...(1)

Poles of the system present at = $-1 \pm i\sqrt{3}$

Characteristic equation is

$$(S + a)[(S + 1)^2 + 3] = 0$$

$$(S + a)(S^2 + 2S + 4) = 0$$

$$S^3 + (2 + a)S^2 + (4 + 2a)S + 4a = 0$$
 ...(II)

Compare equation (I) and (II)

$$2 + a = 4$$

$$a = 2$$

$$4 + 2a = k$$

$$k = 8$$

$$k\alpha = 4a$$

$$\alpha = \frac{8}{8} = 1$$

$$\alpha = 1$$



11-02-2024

Forenoon Session

A source transmits a symbol s, taken from (-4, 0, 4) with equal probability, over an Q.49 additive white Gaussian noise channel. The received noisy symbol r is given by r = s + w, where the noise w is zero mean with variance 4 and is independent of s. Using

 $Q(x) = \frac{1}{\sqrt{2\pi}} \int_{x}^{\infty} e^{\frac{-t^2}{2}} dt$, the optimum symbol error probability is _____.

(a) $\frac{4}{3}Q(1)$

(b) $\frac{2}{3}Q(1)$

(c) $\frac{4}{3}Q(2)$

(d) $\frac{2}{3}Q(2)$

Ans. (a)

$$r = s + \omega$$

$$f_{\omega}(\omega) = \frac{1}{\sqrt{2\pi}} e^{\frac{-\omega^2}{2\times 4}} = N(0, 4)$$

transmission of $-4 \rightarrow r = -4 + \omega$

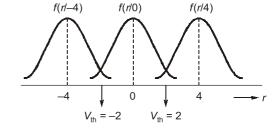
$$f(r/-4) = \frac{1}{\sqrt{2\pi}} e^{\frac{-(r+4)^2}{2\times 4}}$$

transmission of $0 \rightarrow r = \omega$

$$f(r/0) = \frac{1}{\sqrt{2\pi}} e^{-\frac{r^2}{2\times 4}}$$

transmission of $4 \rightarrow r = 4 + n$

$$f(r/4) = \frac{1}{\sqrt{2\pi}} e^{\frac{-(r-4)^2}{2\times 4}}$$



$$P_e = P(-4) \ P_{e-4} + P(0) \ P_{e0} + P(4) P_{e4}$$

Given

$$P(-4) = P(0) = P(4) = \frac{1}{3}$$

$$P_{e-4} = P(r > -2)$$

= 1 - (1 - $F_r(2)$)

where,
$$r = N(-4, 4)$$

$$= 1 - \left(1 - Q\left(\frac{-2+4}{2}\right)\right)$$

$$= Q(1)$$

$$P_{e0} = P(r < -2) + P(r > 2)$$

= $F_r(-2) + \{1 - F_r(2)\}$

where,
$$r = N(0, 4)$$

$$= \left(1 - Q\left(\frac{-2 - 0}{2}\right)\right) + Q\left(\frac{2 - 0}{2}\right)$$

$$= [1 - Q(-1)] + Q(1) = 2Q(1)$$

Corporate Office: 44-A/1, Kalu Sarai, New Delhi - 110016 | Ph: 9021300500



GATE 2024 Engineering

Exam held on:

11-02-2024

Forenoon Session

where, r = N(4, 4)

$$P_{e4} = P(r < 2)$$

$$= F_{r}(2)$$

$$= 1 - Q\left(\frac{2 - 4}{2}\right)$$

$$= 1 - Q(-1)$$

$$= Q(1)$$

$$P_{e} = \frac{1}{3}Q(1) + \frac{2}{3}Q(1) + \frac{1}{3}Q(1)$$

$$= \frac{4}{3}Q(1)$$

End of Solution

Let F_1 , F_2 , and F_3 be functions of (x, y, z). Suppose that for every given pair of points A and B in space, the line integral $\int_C (F_1 dx + F_2 dy + F_3 dz)$ evaluates to the same value along any path C that starts at A and ends at B. Then which of the following is/are true? (a) There exists a differentiable scalar function f(x, y, z) such that

$$F_1 = \frac{\partial f}{\partial x}, F_2 = \frac{\partial f}{\partial y}, F_3 = \frac{\partial f}{\partial z}$$

(b)
$$\frac{\partial F_1}{\partial x} + \frac{\partial F_2}{\partial y} + \frac{\partial F_3}{\partial z} = 0.$$

(c)
$$\frac{\partial F_3}{\partial y} = \frac{\partial F_2}{\partial z}, \frac{\partial F_1}{\partial z} = \frac{\partial F_3}{\partial x}, \frac{\partial F_2}{\partial x} = \frac{\partial F_1}{\partial y}.$$

(d) For every closed path Γ , we have $\oint_{\Gamma} (F_1 dx + F_2 dy + F_3 dz) = 0$.

Ans. (a, c, d)

: Given integral is independent of contour 'C'

$$\int_{C} (F_{1}dx + F_{2}dy + F_{3}dz) = \int_{C} \overline{F} \cdot \overline{dr} \text{ is independent of 'C'}$$

Then \overline{F} is conservative field

$$\therefore \qquad \qquad \overline{F} = \overline{\nabla \phi}$$

$$\Rightarrow \qquad F_1 = \frac{\partial \phi}{\partial x}, \ F_2 = \frac{\partial \phi}{\partial y}, \ F_3 = \frac{\partial \phi}{\partial z}$$

: Option (a) is true.

: \overline{F} is conservative

Then,
$$\nabla \times \overline{F} = 0$$

$$\Rightarrow \begin{vmatrix} i & j & K \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ F_1 & F_2 & F_3 \end{vmatrix} = \vec{0}$$



11-02-2024

Forenoon Session

$$= i \left(\frac{\partial F_3}{\partial y} - \frac{\partial F_2}{\partial z} \right) - j \left(\frac{\partial F_3}{\partial x} - \frac{\partial F_1}{\partial z} \right) + K \left(\frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) = 0 \hat{i} + 0 \hat{j} + 0 \hat{k}$$

Equate on both sides,

$$\frac{\partial F_3}{\partial y} \ = \ \frac{\partial F_2}{\partial z}, \quad \frac{\partial F_3}{\partial x} = \frac{\partial F_1}{\partial z}, \quad \frac{\partial F_2}{\partial x} = \frac{\partial F_1}{\partial y}$$

: Option (c) is true.

If \overline{F} is irrotational then,

$$\oint_C F_1 dx + F_2 dy + F_3 dz = 0$$

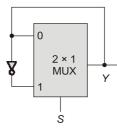
:. Option (d) is also true.

$$\overline{\nabla}\cdot\overline{\digamma}\ =\ \overline{\nabla}\cdot(\overline{\nabla}\phi)\neq 0$$

.. Option (b) is false.

End of Solution

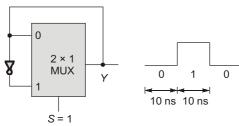
Q.51 The propagation delay of the 2×1 MUX shown in the circuit is 10 ns. Consider the propagation delay of the inverter as 0 ns.



If S is set to 1 then the output Y is _

- (a) constant at 1
- (b) a square wave of frequency 100 MHz
- (c) a square wave of frequency 50 MHz
- (d) constant at 0

Ans. (c)



$$T_c = 10 + 10 = 20 \text{ nsec}$$

$$f_c = \frac{1}{T_c} = \frac{10^9}{20} = 50 \,\text{MHz}$$



- Q.52 A non-degenerate n-type semiconductor has 5% neutral dopant atoms. Its Fermi level is located at 0.25 eV below the conduction band (E_C) and the donor energy level (E_D) has a degeneracy of 2. Assuming the thermal voltage to be 20 mV. The difference between E_C and E_D (in eV, rounded off to two decimal places) is _____.
- Ans. (0.18)

5% neutral donor atoms/dopant atoms means 95% donor atoms are ionized. Concentration of electrons occupying the donor level is given as

$$n_d = \frac{N_d}{1 + \frac{1}{g} \exp\left(\frac{E_D - E_F}{kT}\right)}$$

and $n_d = N_d - N_d^+$ where N_d^+ is ionized donor atoms concentration. according to question

$$n_d = 5\%$$
 of N_d
 $g = 2$ degeneracy factor

$$\frac{5}{100}N_d = \frac{N_d}{1 + \frac{1}{g} \exp\left(\frac{E_D - E_F}{kT}\right)}$$

$$\frac{1}{20} = \frac{1}{1 + \frac{1}{g} \exp\left(\frac{E_D - E_F}{kT}\right)}$$

$$1 + \frac{1}{g} \exp\left(\frac{E_D - E_F}{kT}\right) = 20$$

$$\exp\left(\frac{E_D - E_F}{kT}\right) = 38$$

$$\frac{E_D - E_F}{kT} = \ln (38) \qquad \left\{ \text{given } V_T = \frac{kT}{q} = 20 \text{ mV} \right\}$$

$$E_D - E_F = \ln(38) \times 0.020$$

= 0.07275 eV

given:
$$E_C - E_F = 0.25 \text{ eV}$$

$$E_C - E_D + E_D - E_F = 0.25 \text{ eV}$$

$$E_C - E_D = 0.25 \text{ eV} - (E_D - E_F)$$

$$= 0.25 \text{ eV} - 0.07275 \text{ eV}$$

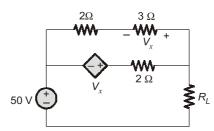
$$= 0.17725 \text{ eV} \approx 0.18 \text{ eV}$$



11-02-2024

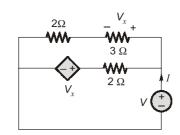
Forenoon Session

Q.53 In the network shown below, maximum power is to be transferred to the load R_{I} .



The value of R_L (in Ω) is _

Ans. (2.5)



$$I = \frac{V - V_x}{2} + \frac{V}{5} = \frac{V}{2} - \frac{V_x}{2} + \frac{V}{5}$$

$$V_x = \frac{V}{5} \times 3$$

:.

$$I = \frac{V}{2} - \frac{1}{2} \times \frac{3V}{5} + \frac{V}{5} = \frac{V}{2} - \frac{3V}{10} + \frac{V}{5}$$

$$I = \frac{5V - 3V + 2V}{10} = \frac{4V}{10}$$

$$\frac{V}{I} = \frac{10}{4} = 2.5 \,\Omega$$

End of Solution

Q.54 A lossless transmission line with characteristic impedance Z_0 = 50 Ω is terminated with an unknown load. The magnitude of the reflection co-efficient is $|\Gamma| = 0.6$. As one moves towards the generator from the load, the maximum value of the input impedance magnitude looking towards the load (in Ω) is ______

Ans. (200)

As we know that

$$Z_{\text{max}} = SZ_0$$

Now,

$$S = \frac{1+|\Gamma|}{1-|\Gamma|} = \frac{1+0.6}{1-0.6} = \frac{1.6}{0.4} = 4$$

$$\therefore \qquad \qquad Z_{\text{max}} = 4 \times 50 = 200 \ \Omega.$$



Q.55 Consider the matrix $\begin{bmatrix} 1 & k \\ 2 & 1 \end{bmatrix}$, where k is a positive real number. Which of the following vectors is/are eigenvector(s) of this matrix?

(a)
$$\left[\frac{1}{\sqrt{2/k}}\right]$$

(b)
$$\begin{bmatrix} 1 \\ -\sqrt{2/k} \end{bmatrix}$$

(c)
$$\begin{bmatrix} \sqrt{2k} \\ -1 \end{bmatrix}$$

(d)
$$\begin{bmatrix} \sqrt{2k} \\ 1 \end{bmatrix}$$

Ans. (a, b)

C Eq is
$$|A-\lambda I| = 0$$

or $\lambda^2 - 2\lambda + (1 - 2K) = 0$

$$\lambda = 1 \pm \sqrt{2K}$$

E vector for $\lambda = 1 \pm \sqrt{2K}$:

$$AX = \lambda X$$
$$(A - \lambda I)X = 0$$

$$\begin{bmatrix} -\sqrt{2K} & K \\ 2 & -\sqrt{2K} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\Rightarrow \qquad -\sqrt{2K}\,x_1 + K\,x_2 = 0$$

$$x_1 = \sqrt{\frac{K}{2}}x_2$$

$$X = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} \sqrt{K/2} \\ 1 \end{bmatrix} \approx \begin{bmatrix} 1 \\ \sqrt{\frac{2}{K}} \end{bmatrix}$$

Similarly other E vector is

$$X = \begin{bmatrix} -\sqrt{\frac{K}{2}} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ -\sqrt{\frac{2}{K}} \end{bmatrix}$$